ZigZag Decoding: Combating Hidden Terminals in Wireless Networks

Shyamnath Gollakota and Dina Katabi
MIT CSAIL

ABSTRACT

This paper presents ZigZag, an 802.11 receiver design that combats hidden terminals. ZigZag's core contribution is a new form of interference cancellation that exploits asynchrony across successive collisions. Specifically, 802.11 retransmissions, in the case of hidden terminals, cause successive collisions. These collisions have different interference-free stretches at their start, which ZigZag exploits to bootstrap its decoding.

ZigZag makes no changes to the 802.11 MAC and introduces no overhead when there are no collisions. But, when senders collide, ZigZag attains the same throughput as if the colliding packets were a priori scheduled in separate time slots. We build a prototype of ZigZag in GNU Radio. In a testbed of 14 USRP nodes, ZigZag reduces the average packet loss rate at hidden terminals from 72.6% to about 0.7%.

Categories and Subject Descriptors C.2.2 [**Computer Systems Organization**]: Computer-Communications Networks

General Terms Algorithms, Design, Performance, Theory
Keywords Wireless, Hidden Terminals, Interference Cancellation

1 Introduction

Collisions and hidden terminals are known problem in 802.11 networks [8, 21, 18, 26, 33]. Measurements from a production WLAN show that 10% of the sender-receiver pairs experience severe packet loss due to collisions [8]. Current 802.11 WLANs rely on carrier sense (CSMA) to limit collisions–i.e., senders sense the medium and abstain from transmission when the medium is busy. This approach is successful in many scenarios, but when it fails, as in the case of hidden terminals, the impact on the interfering senders is drastic; the senders either repeatedly collide and their throughputs plummet, or one sender captures the medium preventing the other from getting packets through [21, 18, 33]. The 802.11 standard proposes the use of RTS-CTS to counter collisions, but experimental results show that enabling RTS-CTS significantly reduces the overall throughput [18, 33, 36, 26], and hence WLAN deployments and access point (AP) manufacturers disable RTS-CTS by default [1, 2]. Ideally, one would like to address this problem without changing the 802.11 MAC or affecting senders that do not suffer from hidden terminals.

We introduce ZigZag, a new 802.11 receiver that increases WLAN's resilience to collisions. ZigZag requires no changes to the 802.11 MAC and introduces no overheard in the case of no collision. In fact, in the absence of collisions, ZigZag acts like a typical 802.11 receiver. But, when senders collide, ZigZag achieves the same performance as if the colliding packets were a priori scheduled in separate time slots.

ZigZag exploits a subtle opportunity for resolving collisions, an opportunity that arises from two basic characteristics of 802.11:

1. An 802.11 sender retransmits a packet until it is acked or timed out, and hence when two senders collide they tend to collide again on the same packets.

2. 802.11 senders jitter every transmission by a short random interval,[1] and hence collisions start with a random stretch of interference free bits.

To see how ZigZag works, consider the hidden terminal scenario in Fig. 1, where Alice and Bob, unable to sense each other, transmit simultaneously to the AP, causing collisions. When Alice's packet collides with Bob's, both senders retransmit their packets causing a second collision, as shown in Fig. 2. Further, because of 802.11 random jitters, the two collisions are likely to have different offsets, i.e., $\Delta_1 \neq \Delta_2$. Say that the AP can compute these offsets (as explained in §5.1), the AP can then find a chunk of bits that experience interference in one collision but is interference-free in the other, such as chunk 1 in Fig. 2. A ZigZag AP uses this chunk to bootstrap its decoder. In particular, since chunk 1 is interference-free in the first collision, the AP can decode it using a standard decoder. The AP then subtracts chunk 1 from the second collision to decode chunk 2. Now, it can go back to the first collision, subtract chunk 2, decode chunk 3, and proceed until both packets are fully decoded.

ZigZag's key contribution is a novel approach to resolving interference, different from prior work on interference cancellation [31, 16] and joint decoding [29]. Basic results on the capacity of the multiuser channel show that if the two hidden terminals transmit at the rate supported by the medium in the absence of interference, i.e., rate R in Fig. 3, the aggregate information rate in a collision, being as high as $2R$, exceeds capacity, precluding any decoding [29, 11]. Thus, state-of-the-art interference cancellation and joint decoding, designed for cellular networks with non-bursty traffic and known users [31, 4], have a fundamental limitation when applied in 802.11 networks: they require a sender to change the way it modulates and codes a packet according to whether the packet will collide or not. This leaves 802.11 senders with the following tradeoff: either they tune to a suboptimal rate that works in the presence of collision, though not every packet will collide, or they send at the best rate in the absence of collision, but accept that the network cannot use these methods to resolve collisions. In contrast, with ZigZag, the senders need not make such a tradeoff. ZigZag allows the senders

---
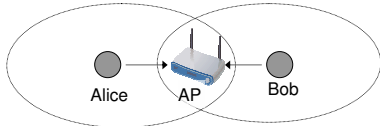[1]Each transmission picks a random slot between 0 and *CW* [34].
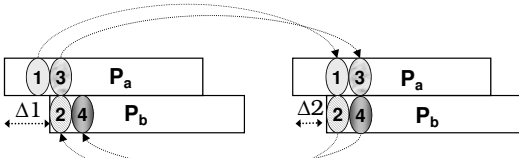
Figure 1: A Hidden Terminals Scenario.

Figure 2: ZigZag Decoding. ZigZag decodes first chunk 1 in the first collision, which is interference free. It subtracts chunk 1 from the second collision to decode chunk 2, which it then subtract from the first collision to decode chunk 3, etc.

to transmit at the best rate supported by the medium in the absence of collisions. However, if collisions occur, ZigZag decodes pairs of collisions that contain the same packets. The average information rate in such a collision pair is $2R/2 = R$. This rate is both decodable and as efficient as if the two packets were scheduled in separate time slots.

ZigZag has the following key features.

- *It is modulation-independent:* In ZigZag, every chunk is first rid of interference then decoded. Hence, ZigZag can employ a standard 802.11 decoder as a black-box, which allows it to work with collisions independent of their underlying modulation scheme (i.e., bit rate), and even when the colliding packets are modulated differently.

- *It is backward compatible:* A ZigZag receiver can operate with unmodified 802.11 senders and requires no changes to the 802.11 protocol (see §7 for how to send acks).

- *It generalizes to more than a pair of colliding packets*, as explained in §8 and experimentally demonstrated in §10.6.

We have implemented a ZigZag prototype in GNU Radio, and evaluated it in a 14-node testbed, where 10% of the sender-receiver pairs are hidden terminals, 10% sense each other partially, and 80% sense each other perfectly. Our results reveal the following findings.

- The loss rate averaged over scenarios with partial or perfect hidden terminals decreases from 72.6% to less than 0.7%, with some severe cases where the loss rate goes down from 100% to zero.

- Averaging over all sender-receiver pairs, including those that do not suffer from hidden terminals, we find that ZigZag improves the average throughput by 25.2% when compared to current 802.11.

- Our BPSK GNURadio implementation and our 4-QAM and 16-QAM simulations show that ZigZag and collision-free decoding achieve the same bit error (BER) for comparable SNRs. Surprisingly, at BPSK and 4-QAM, ZigZag has a slightly lower BER than if the two packets were collision-free. This is because, in ZigZag, every bit is received twice, once in every collision, improving its chances of being correctly decoded.

2 Related Work

Related work falls in the following two areas.

(a) Collisions in WLAN and Mesh Networks. Recent work [14, 15] advocates the use of successive interference cancellation (SIC) and joint decoding to resolve 802.11 collisions. As explained in §1, these schemes work only when the colliding senders transmit at a
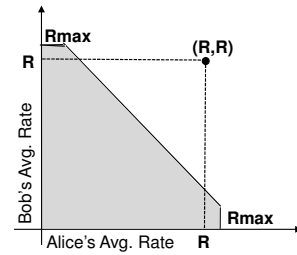

Figure 3: Standard Interference Cancellation and Joint Decoding Require Inefficient Rates. The figure shows the capacity region of the multiuser channel. If Alice and Bob transmit close to the best rate supported by the medium in the absence of interference, R, their combined rates will be (R, R), which is outside the capacity region, and hence cannot be decoded.

bit rate (i.e., information rate) significantly lower than allowed by their respective SNRs and code redundancy. The authors have built a Zigbee prototype of successive interference cancellation [15]. Since ZigBee has no rate adaptation and employs a high redundancy code (every 4 bits are expanded to 32 bits), it experiences scenarios in which the bit rate is significantly below what can be supported by the SNR and the code rate. In such scenarios, SIC could significantly improve the throughput. In contrast, ZigZag works even when a sender uses a bit rate that matches its channel's SNR and the redundancy of its code (as would be the case for systems with proper rate adaptation). In that respect, ZigZag provides an attractive alternative to SIC.

Our work is also related to analog network coding (ANC) [20]. An ANC receiver however can decode collisions only if it already knows one of the two colliding packets. It cannot deal with general collisions or hidden terminals. In principle, one can combine ANC and ZigZag to create a system both addresses hidden terminals, and collects network coding gains.

Additionally, prior works have studied wireless interference [27, 13, 8, 21, 18, 26, 33], and proposed MAC modifications to increase resilience to collisions [37, 10, 19, 5, 25]. In comparison, this paper presents mechanisms that decode collisions rather than avoiding them, and works within the 802.11 MAC rather than proposing a new MAC.

(b) Communication and Information Theory: The idea of decoding interfering users has received much interest in information and communications theories [29, 31, 7, 30, 32]. The main feature that distinguishes ZigZag from prior works in those areas is that ZigZag resolves 802.11 collisions without requiring any scheduling, power control, synchronization assumptions, or coding.

Among the deployed systems, CDMA receivers decode a user by treating all other users as noise [7]. A CDMA solution for hidden terminals in WLANs, however, would require major changes to 802.11 including the use of power control and special codes [4, 7]. Furthermore, CDMA is known to be highly suboptimal in high SNR regimes (e.g., worse than TDMA [29]), which are typical in WLANs.

Finally, successive interference cancellation (SIC) has been used to decode interfering users in CDMA cellular networks [4]. SIC requires the interfering senders to have significantly different powers [31], or different levels of coding [16, 29]. It also requires tight control from the base station to ensure that the total information rate stays below capacity. Conceptually, SIC may be perceived as a special case of ZigZag, in which a chunk is a full packet, i.e., a full packet is decoded and subtracted from the collision signal to decode the other packet. However, by iterating over strategically-picked chunks, ZigZag can resolve interference even when the colliding senders have similar SNRs, are not coordinated, and do not use special codes.
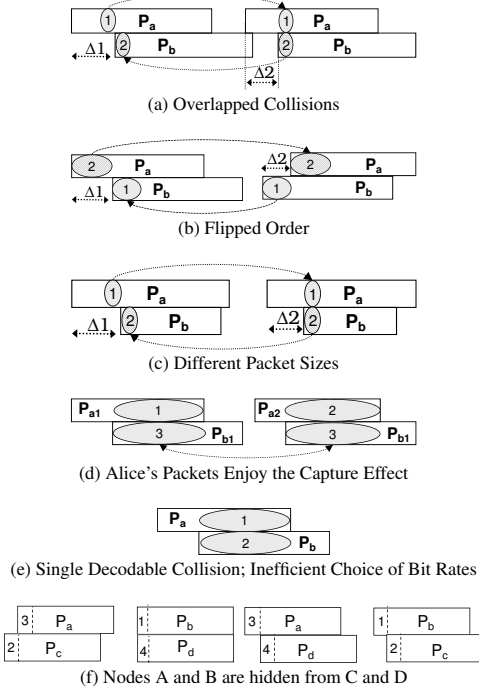
(a) Overlapped Collisions

(b) Flipped Order

(c) Different Packet Sizes

(d) Alice's Packets Enjoy the Capture Effect

(e) Single Decodable Collision; Inefficient Choice of Bit Rates

(f) Nodes A and B are hidden from C and D

Figure 4: ZigZag applies to various collision patterns. Subscripts refer to a packet's sender and id, e.g., P_{a1} is Alice's first packet. The top three patterns are decoded chunk-by-chunk. The forth pattern may occur when Alice's SNR is significantly higher than Bob's. The fifth pattern occurs when Alice's SNR is higher than Bob's, and the bit rates are too low for the SNRs. The last pattern occurs when two groups of nodes are hidden from each other.

3 Scope

ZigZag is an 802.11 receiver design that decodes collisions. It focuses on hidden terminals in WLANs. ZigZag's benefits extend to mesh networks, where having receivers that can decode collisions could enable more concurrent transmissions and hence higher spatial reuse. Exploring mesh benefits is, however, beyond the scope of this paper.

ZigZag adopts a best effort design; in the absence of collisions it acts like current 802.11 receivers, but when collisions occur it tries to decode them. Of course there are collision patterns that ZigZag cannot decode and there are cases where, though the pattern is decodable, decoding may fail because of insufficient SNR. However, since ZigZag does not introduce any overhead for the case of no collision, its presence can only increase the throughput of the WLAN. In §7, we explain how one can deploy ZigZag in a WLAN by changing only the access points and without modifying the clients.

ZigZag resolves a variety of collision patterns. The main idea underlying its decoding algorithm is to find a collision free chunk, which it exploits to bootstrap the decoding process. Once the decoder is bootstrapped the process is iterative and at each stage it produces a new interference-free chunk, decodable using standard decoders. For example, as explained in §1, ZigZag can decode the pattern in Fig. 2 by decoding first chunk 1 in the first collision, and subtracting it from the second collision, obtaining chunk 2, which it decodes and subtracts from the first collision, etc. Using the same principle, ZigZag can decode other patterns like those in Fig. 4. In particular, it can decode patterns where the collisions overlap as in Fig. 4a, and patterns in which colliding packets change order as in Fig. 4b, or even patterns where the packets have different sizes, as in Fig. 4c.

ZigZag also exploits collision patterns that arise from capture ef-

fects. Say that Alice's power at the AP is significantly higher than Bob's, and hence her packets enjoy the capture effect [33]. Currently such a scenario translates into significant unfairness to Bob whose packets do not get through [21, 18, 33]. Like current APs, a ZigZag AP decodes every packet from Alice, the high power sender. Unlike current APs however, ZigZag subtracts Alice's packet from the collision signal and try to decode Bob's packet. However, if Alice's power is excessively high, even a small imperfection in subtracting her signal would contribute a significant noise to Bob's, preventing correct decoding of his packets. In this case, the next collision will involve a new packet from Alice and Bob's retransmission of the same packet, as shown in Fig. 4d. ZigZag decodes Alice's new packet and subtracts it to obtain a second version of Bob's packet, which may also contain errors. ZigZag however combine the two faulty versions of Bob's packet to correct the errors. This is done using Maximal Ratio Combining (MRC) [6], a classic method for combining information from two receptions to correct for bit errors.

In addition, whenever the powers permit, ZigZag decodes patterns that involve a single collision like those in Fig. 4e. This occurs when Alice's power is significantly higher than Bob's, and both senders happen to transmit at a bit rate lower than the best rate supported by the channel. In this case, ZigZag can apply standard successive interference cancellation [31], i.e., ZigZag decodes P_a and subtracts it from the received signal to decode P_b, decoding both packets using a single collision. As explained in §2, successive interference cancellation is a special case of ZigZag, in which a chunk is a full packet. This special case applies only when the bit-rate is too low given the senders' SNRs, and one of the senders has significantly more SNR than the other.

ZigZag can also decode patterns that involve more than two nodes, like that in Fig. 4f. This pattern may occur when two groups of nodes cannot sense each other. For example, nodes *A* and *B*, which are in the same room, can sense each other, but cannot sense nodes *C* and *D*, which happen to be in a different room.

ZigZag can also decode collisions that involve more than a pair of packets, which we discuss in detail §8.

4 A Communication Primer

A wireless signal is typically represented as a stream of discrete complex numbers [24]. To transmit a packet over the wireless channel, the transmitter maps the bits into complex symbols, in a process called modulation. For example, the BPSK modulation (used in 802.11 at low rates) maps a "0" bit to $e^{j\pi} = -1$ and a "1" bit to $e^{j0} = 1$. The transmitter generates a complex symbol every T seconds. In this paper, we use the term $\mathbf{x}[n]$ to denote the complex number that represents the nth transmitted symbol.

The received signal is also represented as a stream of complex symbols spaced by the sampling interval T. These symbols differ, however, from the transmitted symbols, both in amplitude and phase. In particular, if the transmitted symbol is $\mathbf{x}[n]$ the received symbol can be approximated as:

$$\mathbf{y}[n] = \mathbf{H}\mathbf{x}[n] + \mathbf{w}[n], \tag{1}$$

where $\mathbf{H} = he^{\gamma}$ is also a complex number, whose magnitude h refers to channel attenuation and its angle γ is a phase shift that depends on the distance between the transmitter and the receiver, and $\mathbf{w}[n]$ is a random complex noise.[2]

---

[2]This models flat-fading quasi-static channels.

If Alice and Bob transmit concurrently their signals add up, and the received signal can be expressed as:

$$\mathbf{y}[n] = \mathbf{y}_A[n] + \mathbf{y}_B[n] + \mathbf{w}[n],$$

where $\mathbf{y}_A[n] = \mathbf{H}_A\mathbf{x}_A[n]$ and $\mathbf{y}_B[n] = \mathbf{H}_B\mathbf{x}_B[n]$ refer to Alice's and Bob's signals after traversing their corresponding channels to the AP. Note that the above does not mean that we assume the nth symbol from Alice combines with the nth symbol from Bob. The notation is only to keep the exposition clear.

4.1 Practical Issues

A few practical issues complicates the process of estimating the transmitted symbols from the received symbols: frequency offset, sampling offset, and inter-symbol interference. Typically, a decoder has built-in mechanisms to deal with these issues [24].

(a) Frequency Offset and Phase Tracking: It is virtually impossible to manufacture two radios centered at the same exact frequency. Hence, there is always a small frequency difference, δf, between transmitter and receiver. The frequency offset causes a linear displacement in the phase of the received signal that increases over time, i.e.,

$$\mathbf{y}[n] = \mathbf{H}\mathbf{x}[n]e^{j2\pi n\delta fT} + \mathbf{w}[n].$$

Typically, the receiver estimates δf and compensates for it.

(b) Sampling Offset: The transmitted signal is a sequence of complex samples separated by a period T. However, when transmitted on the wireless medium, these discrete values have to be interpolated into a continuous signal. The continuous signal is equal to the original discrete samples, only if sampled at the exact same positions where the discrete values were. Due to lack of synchronization, a receiver cannot sample the received signal exactly at the right positions. There is always a sampling offset, μ. Further, the drift in the transmitter's and receiver's clocks results in a drift in the sampling offset. Hence, decoders have algorithms to estimate μ and track it over the duration of a packet.

(c) Inter-Symbol Interference (ISI) While Eq. 1 makes it look as if a received symbol $\mathbf{y}[n]$ depends only on the corresponding transmitted symbol $\mathbf{x}[n]$, in practice, neighboring symbols affect each other to some extent. Practical receivers apply linear equalizers [22] to mitigate the effect of ISI.

5 ZigZag Decoding

We explain ZigZag decoding using the hidden terminal scenario in Fig. 6, where Alice and Bob, not able to sense each other, transmit simultaneously to the AP, creating repeated collisions. Later in §8, we extend our approach to a larger number of colliding senders.

Like current 802.11, when a ZigZag receiver detects a packet it tries to decode it, assuming no collision, and using a typical decoder. If decoding fails (e.g., the decoded packet does not satisfy the checksum), the ZigZag receiver will check whether the packet has suffered a collision, and proceed to apply ZigZag decoding.

5.1 Is It a Collision?

To detect a collision, the AP exploits that every 802.11 packet starts with a known preamble [34]. The AP detects a collision by correlating the known preamble with the received signal. Correlation is a popular technique in wireless receivers for detecting known signal patterns [7]. Say that the known preamble is L samples. The AP

aligns these L samples with the first L received samples, computes the correlation, shifts the alignment by one sample and re-computes the correlation. The AP repeats this process until the end of the packet. The preamble is a pseudo-random sequence that is independent of shifted versions of itself, as well as Alice's and Bob's data. Hence the correlation is near zero except when the preamble is perfectly aligned with the beginning of a packet. Fig. 5 shows the correlation as a function of the position in the received signal. The measurements are collected using GNURadios (see §10). Note that when the correlation spikes in the middle of a reception, it indicates a collision. Further, the position of the spike corresponds to the beginning of the second packet, and hence shows Δ, the offset between the colliding packets.

The above argument is only partially correct because the frequency offset can destroy the correlation, unless the AP compensates for it. Assume that Alice's packet starts first and Bob's packet collides with it starting at position Δ. To detect Bob's colliding packet, the AP has to compensate for the frequency offset between Bob and itself. The frequency offset does not change over long periods, and thus the AP can maintain coarse estimates of the frequency offsets of active clients as obtained at the time of association. The AP uses these estimates in the computation.

Mathematically, the correlation is computed as follows. Let $\mathbf{y}$ be the received signal, which is the sum of the signal from Alice, $\mathbf{y}_A$, the signal from Bob, $\mathbf{y}_B$, and the noise term $\mathbf{w}$. Let the samples $\mathbf{s}[k], 1 \leq k \leq L$, refer to the known preamble, and $\mathbf{s}^*[k]$ be the complex conjugate. The correlation, Γ, at position Δ is:

$$
\begin{aligned}
\Gamma(\Delta) &= \sum_{k=1}^{L} \mathbf{s}^*[k]\mathbf{y}[k+\Delta] \\
&= \sum_{k=1}^{L} \mathbf{s}^*[k](\mathbf{y}_A[k+\Delta] + \mathbf{y}_B[k] + \mathbf{w}[k])
\end{aligned}
$$

The preamble, however, is independent of Alice's data and the noise, and thus the correlation between the preamble and these terms is about zero. Since Bob's first L samples are the same as the preamble, we obtain:

$$
\begin{aligned}
\Gamma(\Delta) &= \sum_{k=1}^{L} \mathbf{s}^*[k]\mathbf{y}_B[k] \\
&= \sum_{k=1}^{L} \mathbf{s}^*[k]\mathbf{H}_B\mathbf{s}[k]e^{j2\pi k\delta f_BT} \\
&= \mathbf{H}_B \sum_{k=1}^{L} |\mathbf{s}[k]|^2 e^{j2\pi k\delta f_BT}
\end{aligned}
$$

Since a frequency offset exists between Bob and the AP, i.e., $\delta f_B \neq 0$, the terms inside the sum have different angles and may cancel each other. Thus, the AP should compute the value of the correlation after compensating for the frequency offset, which we call Γ'. At position Δ this value becomes:

$$
\begin{aligned}
\Gamma'(\Delta) &= \mathbf{H}_B \sum_{k=1}^{L} |\mathbf{s}[k]|^2 e^{j2\pi k\delta f_BT} \times e^{-j2\pi k\delta f_BT} \\
&= \mathbf{H}_B \sum_{k=1}^{L} |\mathbf{s}[k]|^2.
\end{aligned}
$$

The magnitude of $\Gamma'(\Delta)$ is the sum of energy in the preamble, and thus it is significantly large, i.e., after compensating for the frequency offset, the magnitude of the correlation spikes when the preamble aligns with the beginning of Bob's packet, as shown in Fig. 5. Imposing a threshold enables us to detect whether the AP received a collision signal and where exactly the second packet starts.
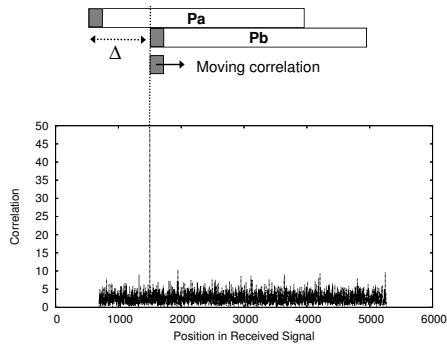
Figure 5: Detecting Collisions by Correlation with the Known Preamble. The correlation spikes when the correlated preamble sequence aligns with the preamble in Bob's packet, allowing the AP to detect the occurrence of a collision and where it starts.
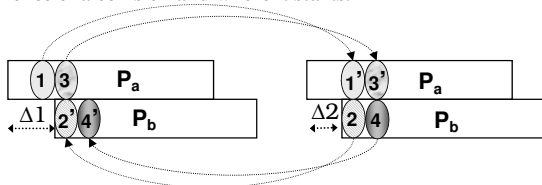

Figure 6: ZigZag decodes then re-encodes a chunk. Before subtracting a decoded chunk, like chunk 1, ZigZag needs to re-encode the bits to create an image of chunk 1', as received in the second collision.

5.2 Did the AP Receive Two Matching Collisions?

Now that it is clear that the received signal is the result of collision, the AP searches for a matching collision, i.e., a collision of the same two packets. The AP stores recent unmatched collisions (i.e., stores the received complex samples). It is sufficient to store the few most recent collisions because, in 802.11, colliding sources try to retransmit a failed transmission as soon as the medium is available [34].

We use the same correlation trick to match the current collision against prior collisions. Assume the AP is trying to match two collisions (P_1, P_2), and (P'_1, P'_2). Without loss of generalization, let us focus on checking whether P_2 is the same as P'_2. The AP already knows the offset in each collision, i.e., Δ and Δ'. The AP aligns the two collisions at the positions where P_2 and P'_2 start. If the two packets are the same, the samples aligned in such a way are highly dependent (they are the same except for noise and the retransmission flag in the 802.11 header), and thus the correlation spikes. If P_2 and P'_2 are different, their data is not correlated and the correlation does not spike at that alignment.

5.3 How Does the AP Decode Matching Collisions?

Say that the AP found a pair of matching collisions like those in Fig. 6. Note that Fig. 6 is the same as Fig. 2 in the introduction except that we distinguish between two images of the same chunk that occur in different collisions, e.g., chunk 1 and chunk 1'. By now the AP knows the offsets Δ_1 and Δ_2, and hence it can identify all interference-free symbols and decode them using a standard decoder.

Next, the AP performs ZigZag decoding, which requires identifying a *bootstrapping chunk*, i.e., a sequence of symbols marred by interference in one collision and interference-free in the other. Say that the first collision has the larger offset, i.e., $\Delta_1 > \Delta_2$, the bootstrapping chunk then is located in the first collision starting at position Δ_2 and has a length of $\Delta_1 - \Delta_2$ samples. This is chunk 1 in Fig. 6.

The rest of the decoding works iteratively. In each iteration, the AP decodes a chunk, re-encodes the decoded symbols and subtract them from the other collision. For example, in Fig. 6, the AP decodes chunk 1 from the first collision, re-encodes the symbols in chunk 1 to create an image of chunk 1', which it subtracts from the second collision to obtain chunk 2. The AP iterates on the rest of the chunks as it did on chunk 1, until it is done decoding all chunks in the colliding packets.

(a) The Decoder. ZigZag can use any standard decoder as a black box. Specifically, the decoder operates on a chunk after it has been rid from interference, and hence can use standard techniques. This characteristic allows ZigZag to directly apply to any modulation scheme as it can use any standard decoder for that modulation as a black box. Further, the two colliding packets may use different modulation (different bit rates) without requiring any special treatment.

(b) Re-Encoding a Chunk. Now that the AP knows the symbols that Alice sent in chunk 1, it uses this knowledge to create an estimate of how these symbols would look after traversing Alice's channel to the AP, i.e., to create an image of chunk 1', which it can subtract from the second collision.

In §5.4 we explain how the AP computes channel parameters, but for now, let us assume that the AP knows Alice's channel, i.e., $\mathbf{H}_A$, δf_A, and μ_A. Denote the symbols in chunk 1 by $\mathbf{x}_A[n] \ldots \mathbf{x}_A[n+K]$. A symbol that Alice sends, $\mathbf{x}_A[n]$, is transformed by the channel to $\mathbf{y}_A[n]$ where:

$$\mathbf{y}_A[n] = \mathbf{H}_A \mathbf{x}_A[n] e^{j2\pi\delta f_A T}.$$

The AP would have received $\mathbf{y}_A[n]$ had it sampled the signal exactly at the same locations as Alice. Because of sampling offset, the AP samples the received signal μ_A seconds away from Alice's samples. Thus, given the samples $\mathbf{y}_A[n] \ldots \mathbf{y}_A[n+K]$, the AP has to interpolate to find the samples at $\mathbf{y}_A[n+\mu_A] \ldots \mathbf{y}_A[n+K+\mu_A]$.

To do so, we leverage the fact that we have a band-limited signal sampled according to the Nyquist criterion. Nyquist says that under these conditions, one can interpolate the signal at any discrete position, e.g., $n+\mu_A$, with complete accuracy, using the following equation [24]:

$$\mathbf{y}_A[n+\mu_A] = \sum_{i=-\infty}^{\infty} \mathbf{y}_A[i] sinc(\pi(n+\mu_A - i)),$$

where *sinc* is the sinc function. In practice, the above equation is approximated by taking the summation over few symbols (about 8 symbols) in the neighborhood of n.

Now that the AP has an image of chunk 1' as received, it subtracts it from the second collision to obtain chunk 2, and proceeds to repeat the same process on this latter chunk.

5.4 Estimating and Tracking System Parameters

The receiver estimates the system's parameters using the preamble in Alice's and Bob's packets. Without loss of generality, we focus on Bob, i.e., we focus on the sender that starts second. This is the harder case since the preamble in Bob's packet, typically used for channel estimation, is immersed in noise. We need to learn $\mathbf{H}_B$, μ_B, and δf_B.

(a) Channel. Again we play our correlation trick, i.e., we correlate the received samples with the known preamble. Recall that the correlation at the peak is:

$$\Gamma'(\Delta) = \mathbf{H}_B \sum_{k=1}^{L} |\mathbf{s}[k]|^2.$$

The AP knows the magnitude of the transmitted preamble i.e., it knows $|\mathbf{s}[k]|^2$. Hence, once it finds the maximum value of the correlation over the collision, it substitutes in the above equation to compute $\mathbf{H}_B$.
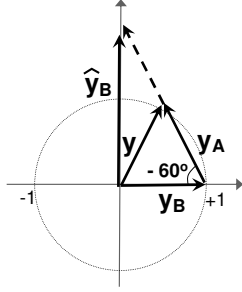
Figure 7: Errors Die Exponentially Fast. The error causes the AP to sum $\mathbf{y}_A$ instead of subtracting it. Hence, the error propagates from $\mathbf{y}_A$ to the estimate $\hat{\mathbf{y}}_B$, i.e., from one chunk to the next, only when the angle between the two vectors is smaller than 60°, which occurs with probability $\frac{1}{3}$.

(b) Frequency Offset. The frequency offset does not change significantly. Since decoders already estimate the frequency offset, an initial coarse estimate can be computed using any prior interference free packet from the client (e.g., the association packet).

This coarse estimate, however, is not sufficient since any residual errors in estimating δf translate into linear displacement in the phase that accumulates over the duration of a packet. Any typical decoder tracks the signal phase and corrects for the residual errors in the frequency offset. Since ZigZag uses a typical decoder as a black box, it need not worry about tracking the phase while decoding. However, as it reconstructs an image of a received chunk, ZigZag tracks the phase. Consider as an example, reconstructing an image of chunk 1'. First we reconstruct the image using the current estimate of the frequency offset, as explained in §5.3(b). Next we subtract that image from the second collisions to get chunk 2. Now, we reconstruct chunk 2 and subtracted from the second collision, creating an estimate of chunk 1', which we term chunk 1". We compare the phases in chunk 1' and chunk 1". The difference in the phase is caused by the residual error in our estimate of the frequency offset. We update our estimate of the frequency offset as follows:

$$\delta f = \delta f + \alpha \delta\phi / \delta t,$$

where α is just a small multiplier, $\delta\phi$ is the phase error which accumulated over a period δt.

(c) Sampling Offset. The procedure used to update and track the sampling offset is fairly similar to that used to update and track the frequency offset. Namely, the black-box decoder tracks the sampling offset when decoding a chunk. When reconstructing the image of a chunk, like chunk 1', we use the differences between chunk 1' and 1" to estimate the residual error in the sampling offset and track it.[3]

(d) Inter-Symbol Interference. When we reconstruct a chunk to subtract it from the received signal, we need to create as close an image of the received version of that chunk as possible. This includes any distortion that the chunk experienced because of multipath effects, hardware distortion, filters, etc. To do so, we need to invert the linear filter (i.e., the equalizer) that a typical decoder uses to remove these effects. The filter takes as input the decoded symbols before removing ISI, and produces their ISI-free version, as follows:

$$\mathbf{x}[i] = \sum_{l=-L}^{L} h_l \, \mathbf{x}_{ISI}[i+l],$$

where the h_l's are known as the filter taps. For our purpose, we can take the filter from the decoder and invert it. We apply the inverse filter to the symbols $\mathbf{x}[n]$ before using them in Eq. 5.3 to ensure that our reconstructed image of a chunk incorporates these distortions.

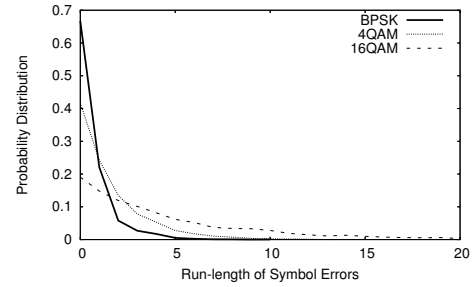[3]We use the Muller-and-Muller algorithm [24] to estimate sampling offset errors.

Figure 8: The probability of error propagation dies fast.

6 Dealing with Errors

Up to now, we have described the system assuming correct decoding. But what happens if the AP makes a mistake in decoding a symbol? For example, in Fig. 6, say the AP mistakenly decodes the first bit in chunk 1 as a "0" bit, when it is actually a "1" bit. Since chunk 1 is subtracted from the second collision to obtain chunk 2, the error will affect the first symbol in chunk 2. This in turn will affect the first symbol in chunk 3, and so on. We will show the following:

- If a symbol error occurs while decoding, it may affect later chunks, but this propagation does not persist. It dies exponentially fast.
- The errors can be further reduced by appling ZigZag in both the forward and backward directions and combining the results.

(a) Errors Die Exponentially Fast. Intuitively, say the AP made a random error in decoding a symbol; the error will propagate to subsequent symbols making them random. However, any modulation scheme has only a few possible symbol values (e.g., a BPSK symbol can be either "0" or "1"). Even when a symbol is randomly decoded, there is a reasonable chance the randomly picked value is correct. Thus, a decoding mistake propagates for a stretch of symbols until it is corrected by chance, at which point it stops affecting subsequent symbols. Assume the probability of randomly picking the right symbol is p, the errors dies at a rate $\frac{1}{p}$.

We formalize the above argument for the case of BPSK, which maps a "0" bit to -1 and a "1" bit to +1. Assume the AP makes a mistake in decoding some symbol $\mathbf{y}_A$, and tries to use the erroneous symbol to decode $\mathbf{y}_B$ by subtracting the decoded vector from the received signal $\mathbf{y} = \mathbf{y}_A + \mathbf{y}_B$.[4] In the worst case, and as shown in Fig. 7, the error causes the AP to add the vector instead of subtracting it, and hence the AP estimates $\hat{\mathbf{y}}_B$ as $\mathbf{y}_B + 2\mathbf{y}_A$. In BPSK, the AP will decode $\mathbf{y}_B$ to the wrong bit value only if the estimate $\hat{\mathbf{y}}_B$ has the opposite sign of the original vector. This will happen only if the angle between the two vectors $\mathbf{y}_B$ and $\mathbf{y}_A$ is less than -60°. The frequency offset between Alice and Bob means that the vectors $\mathbf{y}_B$ and $\mathbf{y}_A$ can have any angle with respect to each other. Thus, the error propagates with probability less than $\frac{60}{180} = \frac{1}{3}$, i.e., in BPSK, errors die exponentially fast at a rate $\frac{2}{3}$.

Fig 8 shows a simulation of error propagation in ZigZag. We insert a decoding error by randomly mistaking a symbol as one of its neighbors in the constellation. We compute the number of subsequent symbols that are affected by this error. The figure shows that errors die exponential quickly. The figure however shows that errors die faster in BPSK and 4-QAM than in 16-QAM, and hence ZigZag performs better in these modulation schemes.

(b) Forward and Backward Decoding. The ZigZag algorithm described so far decodes forward. In Fig. 2, it starts with chunk 1 in the first collision and proceeds until both packets are decoded.

---

[4]We ignore the noise term $\mathbf{w}$ since it has a random effect on the error and can equally emphasize it or correct it.
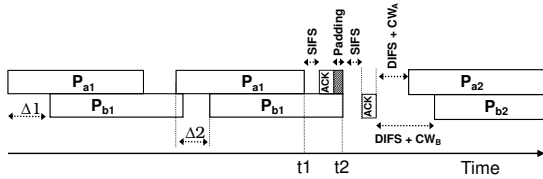
Figure 9: How ZigZag sends 802.11 synchronous acks.

Figure 10: Applying ZigZag to Three Collisions.

However, clearly the figure is symmetric. The AP could wait until it received all samples, then decode backward. If the AP does so, it will have two estimates for each symbol. ZigZag combines these estimates to both combat error propagation and reduce the overall errors. To do so, ZigZag builds on prior results in diversity combining [35, 6]; whenever there is a mismatch between forward and backward decoding, ZigZag uses the soft values of the decoded symbols as a confidence measure. It picks the results of forward or backward decoding depending on which one has a higher confidence (the details are in [12]).

In practice, instead of decoding all the way forward and then backward, one can do it on a chunk-by-chunk basis, using the most recently decoded chunk as a bootstrapping chunk for backward decoding.

7 Backward Compatibility

It would be beneficial if ZigZag requires no changes to senders. In this case, one can improve resilience to interference in a WLAN by purely changing the APs, and without requiring any modifications to the clients (e.g., laptops, PCs, PDAs). Compatibility with unmodified 802.11 senders requires a ZigZag receiver to ack the colliding senders once it decoded their packets; otherwise the senders will retransmit again unnecessarily. Recall that an 802.11 sender expects the ack to follow the packet, separated only by a short interval called SIFS [34]; Can a ZigZag receiver satisfy such requirement?

The short answer is "yes, with a high probability." To see how, consider again the example where Alice and Bob are hidden terminals, and say that the AP uses ZigZag to decode two of their packets, P_{a1} and P_{b1}, as shown in Fig. 9. The AP acks the packets according to the scheme outlined in Fig. 9. Specifically, by time t_1, the AP has fully decoded both P_{a1} and P_{b1}. Even more, by t_1 the AP has performed both forward-decoding and backward decoding for all bits transmitted so far, i.e., all bits except the few bits at the end of P_{b1}.[5] Thus, at t_1 the AP declares both packets decoded. It waits for a SIFS and acks packet P_{a1}. Though the ack collides with the tail of packet P_{b1}, the ack will be received correctly because Alice cannot hear Bob's transmission. Bob too will not be disturbed by the AP's ack to Alice because practical transmitters cannot receive and transmit at the same time. The AP then transmits some random signal to prevent Alice from transmitting her next packet, P_{a2}, before Bob's packet is acked. The AP knows how long this padding signal should be since it already has a decoded version of Bob's packet and knows its length. After Bob finishes his transmission the AP acks him as well.

One question remains, however, would the offset between the two colliding packets suffice to send an ack? Said differently, in Fig. 9, how likely is it that $t_2 - t_1 > SIFS + ACK$. One can show that, given 802.11 timing, the likelihood that the time offset between the two packets is sufficient to send an ack is quite high. In particular, for the common deployment of backward compatible 802.11g, we prove in [12] the following.

---

[5]This assumes the receiver tries in parallel to use standard decoding and ZigZag, and takes whichever satisfies the checksum.
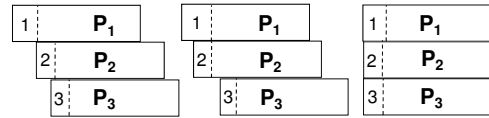
Lemma 7.1 *In 802.11g, the probability that the time offset between two colliding packets is sufficient for sending an ACK is higher than 93.7%.*

There exist however patterns that ZigZag can decode but cannot ack synchronously. For example, in Fig. 4, with a high probability, we can synchronously ack the first four patterns. However, the last two patterns require asynchronous acks. ZigZag always prefers to use synchronous acks. Specifically, the AP identifies ZigZag-aware senders during association. It always tries to send synchronous acks but if that fails and the sender is ZigZag-aware, the AP sends the ack asynchronously in a manner similar to [35]. In practice, however, most collisions tend to involve two terminals and the autorate algorithm matches the bit rate to the SNR. Thus, we believe that even if the AP does not implement asynchronous acks, it can still resolve the majority of the collisions that occur in practice.

8 Beyond Two Interferers

Our description, so far, has been limited to a pair of colliding packets. ZigZag, however, can resolve a larger number of colliding senders. Consider the scenario in Fig. 10, where we have three collisions from three different senders. We refer to the colliding packets by P_1, P_2 and P_3, and collision signals by C_1, C_2 and C_3. The figure shows a possible decoding order. We can start by decoding chunk 1 in the first collision, C_1, and subtract it from C_2 and C_3. As a result, chunk 2 in C_2 becomes interference-free and thus decodable. Next, we subtract chunk 2 from both C_1 and C_3. Now, chunk 3 in C_3 becomes interference-free; so we decode it and subtract it from both C_1 and C_2. Thus, the idea is to find a decoding order such that, at each point, at least one collision has an interference-free chunk ready for decoding.

The following linear-time algorithm provides a chunk-decoding order for any number of collisions.

- **Step 1:** For each of the collisions, decode all the overhanging chunks that are interference-free.
- **Step 2:** Subtract the known chunks wherever they appear in all collisions.
- **Step 3:** Decode all the new chunks that become interference free as a result of Step 2.
- **Step 4:** Repeat the last two steps until all the chunks from all the packets are decoded.

We would like to estimate how often this linear-time algorithm succeeds in resolving collisions, i.e., the probability that it will not get stuck before fully decoding all symbols. To do so, we simulate the behavior of the 802.11 MAC. Specifically, we have n nodes, all hidden from each other, and all want to transmit a packet at $t = 0$. Each node maintains a congestion window cw, which is initialized to 32 slots. Each node randomly picks a slot in its congestion window to transmit the packet. If a collision occurs and the AP fails to decode the packet, the sender doubles its congestion window, up to a maximum of 1024 slots. The experiment is repeated 10,000 times for each value of n. Fig. 11 shows the probability that the greedy decoder fails to decode n packets given n collisions. It shows that this probability ranges between .01%– 1%, and hence is negligible in practice.
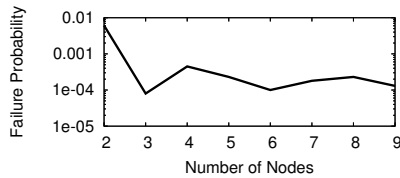
Figure 11: Failure probability of our linear-time decoder as a function of the number of colliding nodes.

Figure 12: Testbed Topology.

Intuitively, one may think of the system of n collisions of n packets as a linear system of n equations and n unknowns. The collisions are the linear equations, whereas the packets are the unknowns. Such system is solvable if the equations are linearly independent, i.e., the packets combine differently in different collisions. A general system of linear equations, however, is not always solvable in linear-time (it requires a matrix inversion). But the equations in the case of collisions have a special structure because the symbols in a packet appear in all collisions in the same order. Fig. 11 shows that for such a structure a linear-time decoder is quite powerful. Indeed, for three collisions (or less) we can show that our linear-time algorithm is as powerful as a non-linear decoder. Specifically, we prove in [12] that:

Lemma 8.1 *Given three collisions of three packets, if for any packet pair P_i and P_j, there exists 2 collisions such that this pair has combined differently (in terms of offsets) in these 2 collisions, the above greedy algorithm always succeeds in decoding all symbols in all colliding packets.*

Finally, note that Fig. 11 is an upper bound on the performance of our linear decoder. In practice, imperfections in the implementation of the decoder limit the maximum number of colliding senders that can be correctly decoded. In §10.6, we show experimental results for scenarios with three interfering senders.

9 Complexity

ZigZag is linear in the number of colliding senders. In comparison to current decoders, ZigZag requires only two parallel decoding lines so that it can decode two chunks in the same time that it would take a current decoder to decode one chunk. Most of the components that ZigZag uses are typical to wireless receivers. ZigZag uses the decoders and the encoders as black-boxes. Correlation, tracking, and channel estimation are all typical functionalities in a wireless receiver [24, 7].

10 Experimental Environment

We evaluate ZigZag in a 14-node GNURadio testbed. The topology is shown in Fig. 12. Each node is a commodity PC connected to a USRP GNU radio [17].
(a) Hardware and Software Environment. We use the Universal Software Radio Peripheral (USRP) [17] for our RF frontend. We use the RFX2400 daughterboards which operate in the 2.4 GHz range. The software for the signal processing blocks is from the open source GNURadio project [9].
(b) Modulation. ZigZag uses the modulation/demodulation module as a black-box and works with a variety of modulation schemes. Our implementation, however, uses Binary Phase Shift Keying, *BPSK*, which is the modulation scheme that 802.11 uses at low rates.
(c) Configuration Parameters. We use the default GNURadio configuration, i.e., on the transmitter side, the DAC rate is $128e6$ samples/s, the interpolation rate is 128, and the number of samples per symbol is 2. On the receiver side, the ADC rate is $64e6$ samples/s and
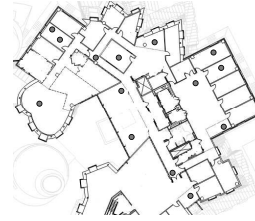
the decimation rate is 64. Given the above parameters and a BPSK modulation, the resulting bit rate is 500kb/s. Each packet consists of a 32-bit preamble, a 1500-byte payload, and 32-bit CRC.
(d) Implementation Flow Control. On the sending side, the network interface pushes the packets to the GNU software blocks with no modifications. On the receiving side, the packet is first detected using standard methods built in the GNURadio software package. Second, we try to decode the packet using the standard approach (i.e., using the BPSK decoder in the GNURadio software). If standard decoding fails, we use the algorithm in §5.1 to detect whether the packet has experienced a collision, and where exactly the colliding packet starts. If a collision is detected, the receiver matches the packet against any recent reception, as explained in §5.2. If no match is found, the packet is stored in case it helps decoding a future collision. If a match is found, the receiver performs chunk-by-chunk decoding on the two collisions, as explained in §5.3. Note that even when the standard decoding succeeds we still check whether we can decode a second packet with lower power (i.e., a capture scenario).
(e) Compared Schemes. We compare the following:

- **ZigZag:** This is a ZigZag receiver as described in §5 augmented with the backward-decoding described in §6.
- **802.11:** This approach uses the same underlying decoder as ZigZag but operates over individual packet.
- **Collision-Free Scheduler:** This approach also uses the same basic decoder but prevents interference altogether by scheduling each sender in a different time slot.

(f) Metrics. We employ the following metrics:

- *Bit Error Rate (BER):* The percentage of incorrect bits averaged over every 100 packets.
- *Packet Loss Rate (PER):* This is the percentage of incorrectly received packets. We consider a packet to be correctly received if the BER in that packet is less than 10^{-3}. This is in accordance with typical wireless design, which targets a maximum BER of 10^{-3} before coding (and 10^{-5} after coding) [3, 28].[6]
- *Throughput:* This is the number of delivered packets normalized by the GNU Radio transmission rate. Again a packet is considered delivered if the uncoded BER is less than 10^{-3}. In comparison to packet loss rate, the throughput is more resilient to hidden terminals in scenarios that exhibit capture effects. This is because the terminal that captures the medium transmits at full rate and gets its packets through, causing unfairness to the other sender, but little impact on the overall throughput.

10.1 Setup

Since ZigZag acts exactly like current 802.11 receivers except when a collision occurs, our evaluation focuses on scenarios with hidden terminals, except in §10.5 where we experiment with various nodes in the testbed irrespective of whether they are hidden terminals. In

---

[6]For example, 802.11a target packet error rate (PER) is 0.1 for a packet size of 8000 bits. Given a maximum uncoded BER of 10^{-3}, practical channel codes like BCH Code(127,99) and BCH Code(15,5) achieve the desired PER.

Table 1: Micro-Evaluation of ZigZag's components

Correlation	False Positives	3.1%	
	False Negatives	1.9%	
Frequency	Pkt size(Bytes)	800	1500
&	Success With	99.6%	98.2%
Phase Tracking	Success Without	89%	0%
ISI Filter	SNR	10dB	20dB
	Success With	99.6%	100%
	Success Without	47%	96%

(a) Error Distribution due to Residual δf.

(b) ISI Prone Symbols

Figure 13: Effects of Residual Frequency Offset and ISI.

every run, two (or three) senders transmit 500 packets to an access point. The AP (i.e., the receiver) logs the received signal and the logs are processed offline with the evaluated receiver designs.

Software radios are incapable of accurately timing their carrier sense activity (CSMA) because they perform all signal processing in user mode on the PC. To approximate CSMA, we take the following measures. First, we setup an 802.11a node next to each of our USRP nodes. The objective is to create an 802.11a testbed that matches the topology in our USRP testbed but uses standard 802.11a cards, and copy the results of carrier sense from it to our USRP testbed.
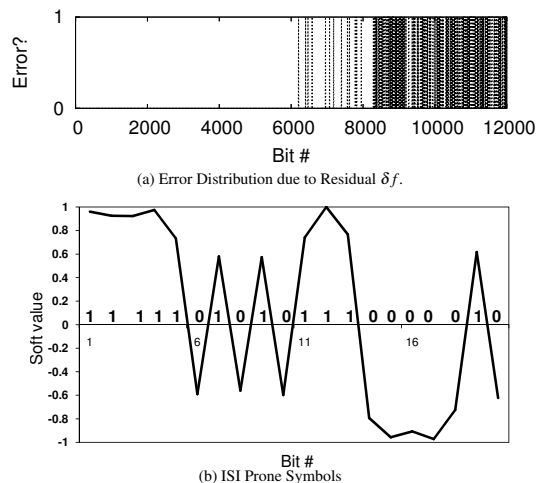
For each USRP experiment, we check whether the corresponding 802.11a nodes can carrier sense each other. Specifically, we make each pair of the 802.11 nodes transmit at full speed to a third node considered as an AP, log the packets, and measure the percentage of packets each of them delivers to the AP. Next, we try to mimic the same behavior using the USRP nodes, where each packet that was delivered in the 802.11 experiments results in a packet delivery in the USRP experiments between the corresponding sender-receiver USRP pairs. Lost 802.11 packets are divided into two categories: collisions and errors. Specifically, a lost 802.11 packet that we can match with a loss from the concurrent sender is considered a collision loss. Other losses are considered as medium errors and ignored. We try to make each USRP experiment match the collisions that occurred in the corresponding 802.11a experiment by triggering as many collisions as observed in the 802.11a traces. The USRP experiments are run without CSMA. Each run matches an 802.11 run between the corresponding nodes. Each sender first transmits the same number of packets that the corresponding 802.11 correctly delivered in the matching 802.11 run. Then both senders transmit together as many packets as there were collision packets in the matching 802.11 run.

Software radios also cannot time 802.11 synchronous acks. Given the 802.11a traces, we know when a collision occurs, and that the sender should retry the packet, in which case the sender transmits each packet twice. However, if the ZigZag AP manages to decode using a single collision, we ignore the retransmission and do not count it against the throughput. This prototype implementation does not include the acking scheme described in §7.

10.2 Micro-Evaluation

We examine the role of various components of ZigZag.

(a) Correlation as a Collision Detector: We estimate the effectiveness of the correlation-based algorithm (§5.1) in detecting the occurrence of collisions. Our implementation sets the threshold to $\Gamma'(Delta) > \beta \times L \times SNR$, where β is a constant, L is the length of the preamble and SNR is a coarse estimate of the SNR of the colliding sender, which could be obtained from any previously decoded packets or from one of the sender's interference free chunks. For our testbed, $\beta = 0.6$-0.7 balances false positives with false negatives. Higher values eliminate false positives but make ZigZag miss some

collisions, whereas lower values trigger collision-detection on clean packets. Note that neither false positives nor false negatives produce end-to-end errors. The harm of false positive is limited to computational resources, because in ZigZag marking a packet as a collision does not prevent correct decoding of that packet. The algorithm behaves as if the packet suffered capture effect and hence is decodable despite being marred by collision. False negatives, on the other hand, make ZigZag miss opportunities for decoding collisions but do not produce incorrect decoding. Our evaluation sets $\beta = 0.65$.

For SNRs in [6-20]dB, we run the collision detector on sets of 500 non-collision packets and 500 collisions, and report the results in Table 10.1. The average false positive rate (packets mistaken as collisions) is 3.1% and the average false negative rate (missing collisions) is 1.9%. Thus, the collision detector is pretty accurate for our purpose.

(b) Frequency and Phase Tracking: We evaluate the need for the frequency and phase tracking described in §5.4b. We disable our tracking algorithm (but leave the decoder unchanged) and provide the encoder with an initially accurate estimate of the frequency offset (as estimated by the decoder). We run ZigZag with and without tracking on 500 collision-pairs of 1500B packets. We find that without tracking none of the colliding packets is decodable (BER $> 10^{-3}$), whereas with tracking enabled, 98.2% of the colliding packets are decodable.

Fig. 13(a) explains this behavior. It plots the error as a function of the bit index in one of the colliding packets (black shades refer to errors). It shows that the first 6000 bits are decoded correctly, but as we go further the bits start getting flipped, and eventually most of the bits are in error. This is expected since even a small residual error in the frequency offset causes a phase rotation that increases linearly with time. Hence after some time the phase becomes completely wrong causing high decoding error rates. This effect is particularly bad for long packets since the errors accumulate over time. Table 10.1 shows that while ZigZag can decode 89% of the 800Byte packets without phase tracking, none of the 1500Byte packets is successfully decoded unless we enable phase tracking.

(c) Effect of ISI: Fig. 13(b), shows a snapshot of the ISI-affected received bits in our testbed. Recall that BPSK represents a "0" bit with -1 and a "1" bit with +1. The figure shows that the value of a received bit depends on the value of its neighboring bits. For example, a "1" bit tends to take a higher positive value if it is preceded by another "1", than if the preceding bit is a "0" bit.

We evaluate the importance of compensating for these distortions

(a) Alice's Throughput

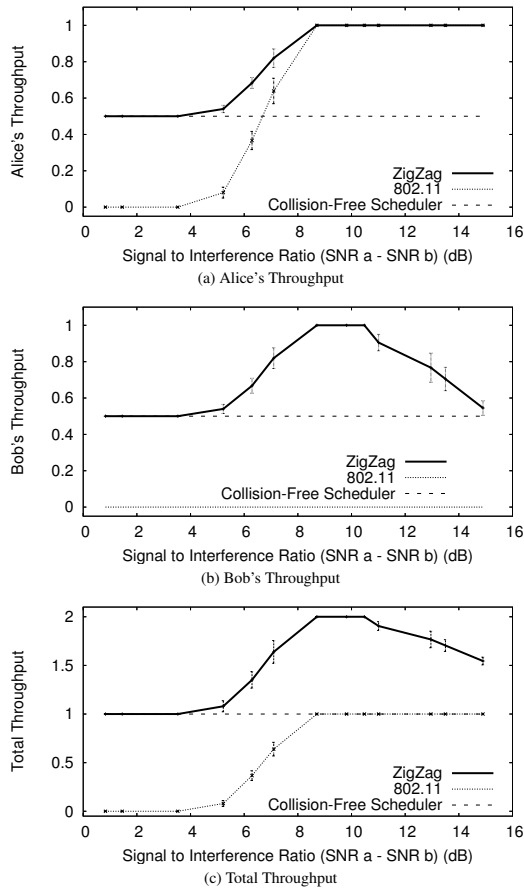(b) Bob's Throughput

(c) Total Throughput

Figure 14: Impact of SINR. The figure plots the throughput of the hidden terminals Alice and Bob, as Alice moves closer to the AP, i.e., as $SINR \approx SNR_A - SNR_B$ increases. It shows that ZigZag achieves higher throughput than both 802.11 and the Collision-Free Scheduler. ZigZag is also fairer than 802.11, where Bob cannot get any packets through.

using the inverse filter described in §5.4d. We try to decode 500 collision pairs at different SNRs, with the filter on and off. Table 10.1 shows that, while the filter is not important at high SNRs, i.e., $20dB$, it is necessary at low SNRs. This is expected as at low SNRs, the decoder has to combat both higher noise and ISI distortions.

10.3 Does ZigZag Work?

We would like to understand the impact of the signal-to-interference ratio (SINR) on ZigZag's performance. We want to check that ZigZag does not suffer from the same restrictions as traditional interference cancellation, i.e., it works even when the colliding senders have comparable SNRs. We also want to check that ZigZag continues to work as the SNR difference becomes large, i.e., in scenarios that may cause capture effects [23, 18].

We consider the hidden terminal scenario in Fig. 1, where Alice and Bob cannot sense each other and hence transmit simultaneously to the AP. We start from a setting where both senders are at equal distance from the AP, i.e., $SNR_A = SNR_B$, and hence $SINR = 0$. Gradually, we move Alice closer to the AP. As Alice moves closer, her SNR at the AP increases with respect to Bob's, making it easier for the AP to capture Alice's signal. We plot the results of this experiment in Fig. 14, for when the nodes use a Collision-Free Scheduler, 802.11, and ZigZag.

Fig. 14 shows that ZigZag improves both throughput and fairness. In 802.11, when Alice and Bob are equal distance from the AP, their

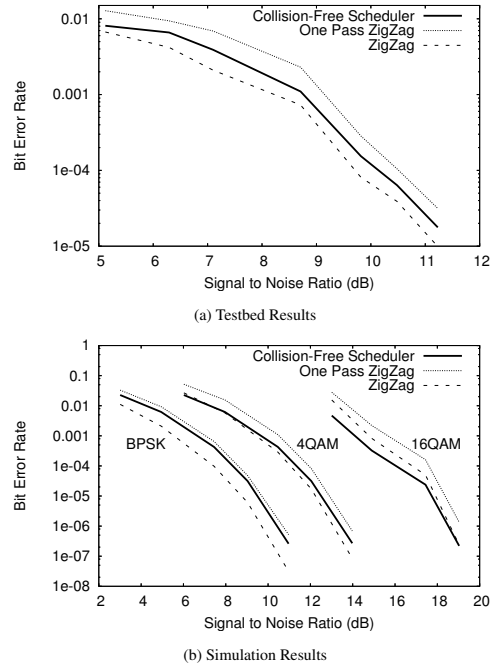(a) Testbed Results

(b) Simulation Results

Figure 15: Comparison of Bit Error Rate (BER). For all modulation schemes, ZigZag and the Collision-Free Scheduler achieve the same BER for comparable SNRs (+/- 1 dB of each other).

signals collide, and neither can be received. As Alice moves closer, her signal improves with respect to Bob's. When Alice's signal is 4-6 dB higher than Bob's, the capture effect starts, and we see a slight increase in Alice's throughput. As Alice gets even closer, Bob's signal becomes irrelevant. Note, however, that at all times Bob is never received at the AP with 802.11. In contrast, with the Collision-Free Scheduler, both Alice and Bob get a fair chance at accessing the AP. But the scheduler cannot exploit that as Alice gets closer, the capacity increases [29], making it possible to decode both Alice and Bob.

ZigZag outperforms both current 802.11 and the Collision-Free Scheduler. When Alice and Bob are equal distance from the AP, it ensures that they are both received, as if they were allocated different time slots. As Alice moves closer to the AP, the capture effect starts kicking off. As a result, the AP can decode Alice's signal without the need for a second collision. The AP then subtracts Alice's signal from the collision and decode Bob's packet, and thus the total throughput becomes twice as much as the radio transmission rate. As Alice gets even closer, her signal completely covers Bob's signal making it impossible to decode Bob's packet.

Thus, this experiment reveals the following:

- At low SINRs, ZigZag significantly outperforms 802.11 and is similar to a Collision-Free Scheduler, i.e., it delivers the same throughput as if the colliding packets were scheduled in separate time slots.
- At high SINR, ZigZag can outperform both 802.11 and the Collision-Free Scheduler. This is because neither 802.11 nor the Collision-Free Scheduler can benefit from scenarios where the network capacity is higher than the sum of the rates of the two senders. In contrast, ZigZag can exploit such scenarios to double the throughput of the network, decoding both hidden terminals using a single collision. Furthermore, ZigZag does not need to be explicitly informed of the capacity of the network to exploit it. It naturally transitions to exploit the increased capacity as the SNR increases.
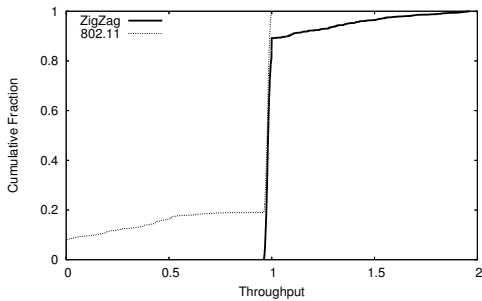
Figure 16: Normalized Throughput for the Whole Testbed. The figure shows a CDF of the throughputs in our testbed for pairs of competing flows, for both hidden and non-hidden terminal scenarios. ZigZag improves the average throughout in our testbed by 25.2%.
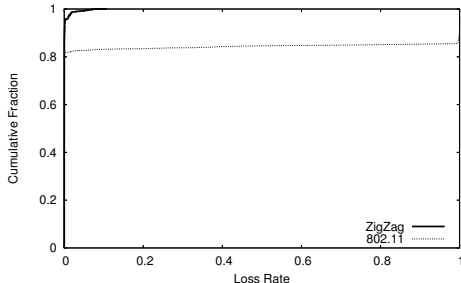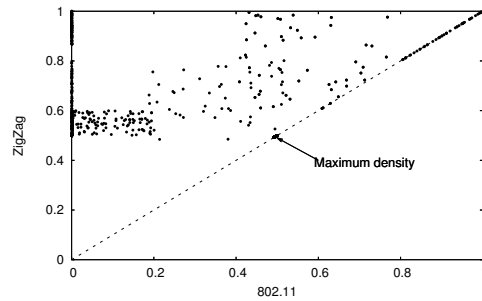

Figure 18: Scatter Plot of Flow Throughputs. The figure shows a scatter plot of ZigZag and 802.11 throughputs for each sampled sender-receiver pairs. ZigZag helps when there are hidden terminals and never hurts.
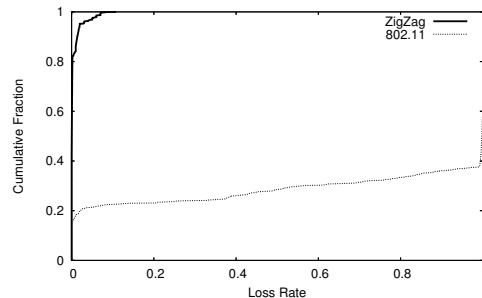

Figure 17: Loss Rate for the Whole Testbed. The figure shows a CDF of the packet loss rate in our testbed for pairs of competing flows, for both hidden and non-hidden terminal scenarios. ZigZag improves the average loss rate in our testbed from 15.8% to 0.2%.

Figure 19: CDF of Loss Rate at Hidden Terminals. The figure zooms on scenarios with full or partial hidden terminals. ZigZag reduces the average loss rate for hidden terminals in our testbed from 72.6% to about 0.7%.

10.4 The Impact of the SNR

The standard performance metric for a receiver is the BER as a function of the SNR [28, 3, 29], and the ultimate test for a design that resolves collisions is whether it can match the uncoded BER of a collision-free reception at every SNR, and for every modulation scheme.

To test performance under various SNRs and modulation schemes, we consider the scenario where Alice and Bob cannot sense each other and hence transmit simultaneously to the AP. In contrast to §10.3 however, Alice and Bob stay at a fixed and equal distance from the AP. We control their transmission powers to ensure that they have the same SNR, and plot the BER as a function of the SNR. Our GNURadio prototype employs BPSK but to check performance with other modulation schemes (e.g., 4-QAM, 16-QAM), we use simulations. The simulations are based on an additive white Gaussian noise (AWGN) channel [29]. Other parameters (e.g., the packet size and frequency offset) are set to their values in the testbed.

Figs. 15a and 15b plot the BER as a function of the SNR, both in the testbed and in simulations.[7] The plots are only for ZigZag and the Collision-Free Scheduler because, in this scenario, 802.11 performed extremely poorly with BER close to 50%. The figures show:

- For all modulation schemes, ZigZag and the Collision-Free Scheduler achieve the same BER for comparable SNRs, i.e., the required SNRs are within 1 dB of each other.
- At BPSK and 4-QAM, ZigZag has a slightly better BER than if the two packets were received collision-free. This is because, in ZigZag, every bit is received twice, once in every collision, improving its chances of being correctly decoded. This impact is countered by error propagation (see §6). Since errors propagate

---
[7]As expected BPSK in the testbed works at slightly higher SNR than in simulations because of hardware and software imperfections.

further in denser modulations, ZigZag's performance is slightly worse at 16-QAM.

10.5 Testbed Throughput and Loss Rate

In this section, we use the testbed in Fig. 12 as a case study to investigate how ZigZag affects various sender-receiver pairs. The testbed has 14 nodes that form a variety of line-of-sight and non-line-of-sight topologies. While up to now we have focused only on scenarios with hidden terminals, in this section, we experiment with various testbed nodes irrespective of whether they are hidden terminals. Specifically, we pick two senders randomly. We pick an AP randomly from the nodes reachable by both senders. We mimic CSMA as explained in §10.1 and make each sender transmit 100 packets to the AP. We repeat the experiment with random set of sender pairs and different choice of APs. Among the sender pairs that we sampled 10% are perfect hidden terminals, 10% can sense each other partially, and 80% can sense each other perfectly.

First, we compare the throughput and loss rate under current 802.11 and ZigZag, for the whole network. Fig. 16 plots a CDF of the aggregate throughput, i.e., the sum of the throughput of each pair of concurrent senders. The figure shows that in our testbed, ZigZag increases the average throughput by 25.2%. This improvement arises from two factors. For all cases where the normalized aggregate throughput is less than 1, the improvement comes purely from ZigZag's ability to resolve successive collisions. For cases where the aggregate throughput is higher than 1, the improvement is caused by a combination of being able to resolve a single collision whenever possible, and successive collisions otherwise. Note that traditional interference cancellation applies only to cases whose throughputs are between 1.5 and 2, which are very few. Fig. 17 plots a CDF of the loss rates of individual sender-receiver pairs, i.e., the flows we experimented with.
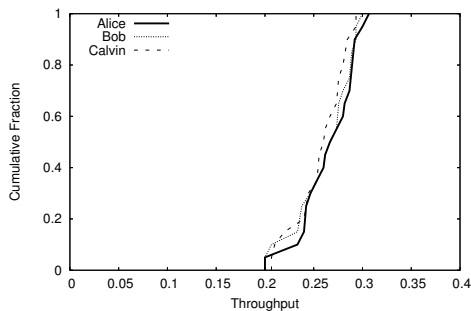
Figure 20: ZigZag's Performance with Three Hidden Terminals. Cumulative distribution of the throughput of three hidden terminals.

The figure shows that in our testbed, ZigZag reduces the average packet loss rate from 15.8% to 0.2%.

Next, we check that a ZigZag AP is always a conservative choice and does not hurt any flow. Fig. 18 shows a scatter plot of the throughout of every sender-receiver pair in our experiments, both under 802.11 and ZigZag. The figure shows that ZigZag consistently improves the throughput and does not hurt any sender-receiver pair.

Next, we zoom on the hidden terminals in our testbed, which we define as sender pairs that fail to sense each other fully or partially. Fig. 19 shows a CDF of the packet loss rate in transfers that suffered such hidden terminal scenarios. The figure shows that ZigZag improves the average loss rate for hidden terminals in our testbed from 72.6% to 0.7%. Furthermore, for some severe cases, the packet loss rate goes down from 99-100% to about zero.

10.6 Many Hidden Terminals

In §8 we generalized ZigZag to deal with many colliding sources. Here, we evaluate how ZigZag performs on three collisions. In this experiment, we have three hidden terminals that transmit concurrently to a random AP. Fig. 20 shows the CDF of the throughput under ZigZag. The figure shows that all three senders see a fair throughput that is about one third of the medium throughput. Thus, even with more than a pair of colliding senders, ZigZag performs almost as if each of the colliding senders transmitted in a separate time slot.

11 Conclusion

This paper presents ZigZag, a receiver that can decode collisions. Our core contribution is a new form of interference cancellation that iteratively decodes strategically picked chunks, exploiting asynchrony across successive collisions. We show via a prototype implementation and testbed evaluation that ZigZag addresses the hidden terminal problem in WLANs, improving the throughput and loss rate.

We identify two research issues worth of further exploration. First, our prototype works with pre-coded bits. Most wireless systems however use some form of forward error correction (FEC). We envision that jointly decoding collisions and the FEC in the packets could provide better performance. Second, collision signals have more power and a wider dynamic range than individual transmissions. Wireless hardware typically employs automatic gain control (AGC) to adjust the dynamic range. It is important to study the AGC design in systems that decode collisions.

We believe ZigZag has wider implications for wireless design than explored in this paper. It motivates a more aggressive MAC that exploits concurrent transmissions in order to increase spatial reuse and network throughput. Further, ZigZag can decode ANC packets [20], presenting a modulation-independent decoder for analog network

coding. It seems plausible that one may combine ZigZag with the ideas in the ANC paper into one system that improves concurrency, addresses hidden terminals, and collects network coding gains.

References

[1] Broadcom Wireless LAN Adapter User Guide.

[2] Reference Manual for the NETGEAR ProSafe 802.11g Wireless AP WG102.

[3] ISL3873: Wireless LAN Integrated Medium Access Controller with Baseband Processor, 2000.

[4] J. Andrews. Interference cancellation for cellular systems: A contemporary overview. *IEEE Wireless Communications*, 2005.

[5] V. Bharghavan, A. J. Demers, S. Shenker, and L. Zhang. MACAW: A Media Access Protocol for Wireless LAN's. In *ACM SIGCOMM 1994*.

[6] D. G. Brennan. On the Maximal Signal-to-Noise Ratio Realizable from Several Noisy Signals. *Proc. IRE*, 43:1530, October 1955.

[7] P. Castoldi. *Multiuser Detection in CDMA Mobile Terminals*. Artech house Publishers, 2002.

[8] Y.-C. Cheng, J. Bellardo, P. Benk, A. C. Snoeren, G. M. Voelker, and S. Savage. Jigsaw: solving the puzzle of enterprise 802.11 analysis. In *SIGCOMM*, 2006.

[9] G. FSF. GNU Radio - GNU FSF Project.

[10] C. L. Fullmer and J. J. Garcia-Luna-Aceves. Solutions to Hidden Terminal Problems in Wireless Networks. In *SIGCOMM*, pages 39–49, 1997.

[11] R. G. Gallager. A Perspective on Multiaccess Channels. *IEEE Transactions on Information Theory*, IT-31(2), march 1985.

[12] S. Gollakota and D. Katabi. Zigzag decoding: Combating hidden terminals in wireless networks. Technical Report MIT-CSAIL-TR-2008-018, MIT, 2008.

[13] R. Gummadi, D. Wetherall, B. Greenstein, and S. Seshan. Understanding and Mitigating the Impact of RF Interference on 802.11 Networks. In *SIGCOMM*, 2007.

[14] D. Halperin, J. Ammer, T. Anderson, and D. Wetherall. Interference Cancellation: Better Receivers for a New Wireless MAC. In *Hotnets*, 2007.

[15] D. Halperin, T. Anderson, and D. Wetherall. Practical interference cancellation for wireless lans. In *Proc. of ACM MOBICOM 2008*.

[16] J. Hou, J. Smee, H. D. Pfister, and S. Tomasin. Implementing Interference Cancellation to Increase the EV-DO Rev A Reverse Link Capacity. *IEEE Communication Magazine*, February 2006.

[17] E. Inc. Universal software radio peripheral. http://ettus.com.

[18] G. Judd and P. Steenkiste. Using Emulation to Understand and Improve Wireless Networks and Applications. In *NSDI*, 2005.

[19] P. Karn. MACA–A New Channel Access Method for packet Radio. *9th Computer Networking Conf.*, 1990.

[20] S. Katti, S. Gollakota, and D. Katabi. Embracing Wireless Interference: Analog Network Coding. In *ACM SIGCOMM*, 2007.

[21] S. Khurana, A. Kahol, and A. P. Jayasumana. Effect of Hidden Terminals on the Performance of IEEE 802.11 MAC Protocol, 1998.

[22] E. A. Lee and D. G. Messerschmitt. *Digital Communications*. Boston: Kluwer Academic, 1988.

[23] J. Lee, W. Kim, S.-J. Lee, D. Jo, J. Ryu, T. Kwon, and Y. Choi. An Experimental Study on the Capture Effect in 802.11a Networks, 2007.

[24] H. Meyr, M. Moeneclaey, and S. A. Fechtel. *Digital Communication Receivers: Synchronization, Channel Estimation, and Signal Processing*. John Wiley & Sons, 1998.

[25] A. Muqattash and M. Krunz. CDMA-Based MAC Protocol for Wireless Ad Hoc Networks. In *ACM MOBIHOC*, 2003.

[26] P. C. Ng, S. C. Liew, K. C. Sha, and W. T. To. Experimental Study of Hidden node Problem in IEEE 802.11 Wireless Networks. In *Sigcomm Poster*, 2005.

[27] C. Reis, R. Mahajan, M. Rodrig, D. Wetherall, and J. Zahorjan. Measurement-Based Models of Delivery and Interference. In *SIGCOMM*, 2006.

[28] J. K. Tan. An Adaptive Orthogonal Frequency Division Multiplexing Baseband Modem for Wideband Wireless Channels. Master's thesis, MIT, 2006.

[29] D. Tse and P. Vishwanath. *Fundamentals of Wireless Communications*. Cambridge University Press, 2005.

[30] D. Tse, P. Viswanath, and L. Zheng. Diversity-Multiplexing Tradeoff in Multiple Access Channels. *IEEE Transaction on Information Theory*, 2004.

[31] S. Verdu. *Multiuser Detection*. Cambridge University Press, 1998.

[32] A. J. Viterbi. Very Low Rate Convolutional Codes for Maximum Theoretical Performance of Spread-Spectrum Multiple-Access Channels. *IEEE JSAC*, May 1990.

[33] C. Ware, J. Judge, J. Chicharo, and E. Dutkiewicz. Unfairness and capture behaviour in 802.11 adhoc networks. volume 1, pages 159–163 vol.1, 2000.

[34] I. . WG. Wireless lan medium access control (mac) and physical layer (phy) specifications. *Standard Specification,IEEE, 1999.*

[35] G. Woo, P. Kheradpour, and D. Katabi. Beyond the Bits: Cooperative Packet Recovery Using PHY Information. In *ACM MobiCom*, 2007.

[36] K. Xu, M. Gerla, , and S. Bae. Effectiveness of RTS/CTS Handshake in IEEE 802.11 Based Ad Hoc Networks. *In Ad Hoc Network Journal*, 2003.

[37] J. Zhu, X. Guo, S. Roy, and K. Papagiannaki. CSMA Self-Adaptation based on Interference Differentiation. In *IEEE Globecom*, 2007.