

# System energy consumption is a multi-player game

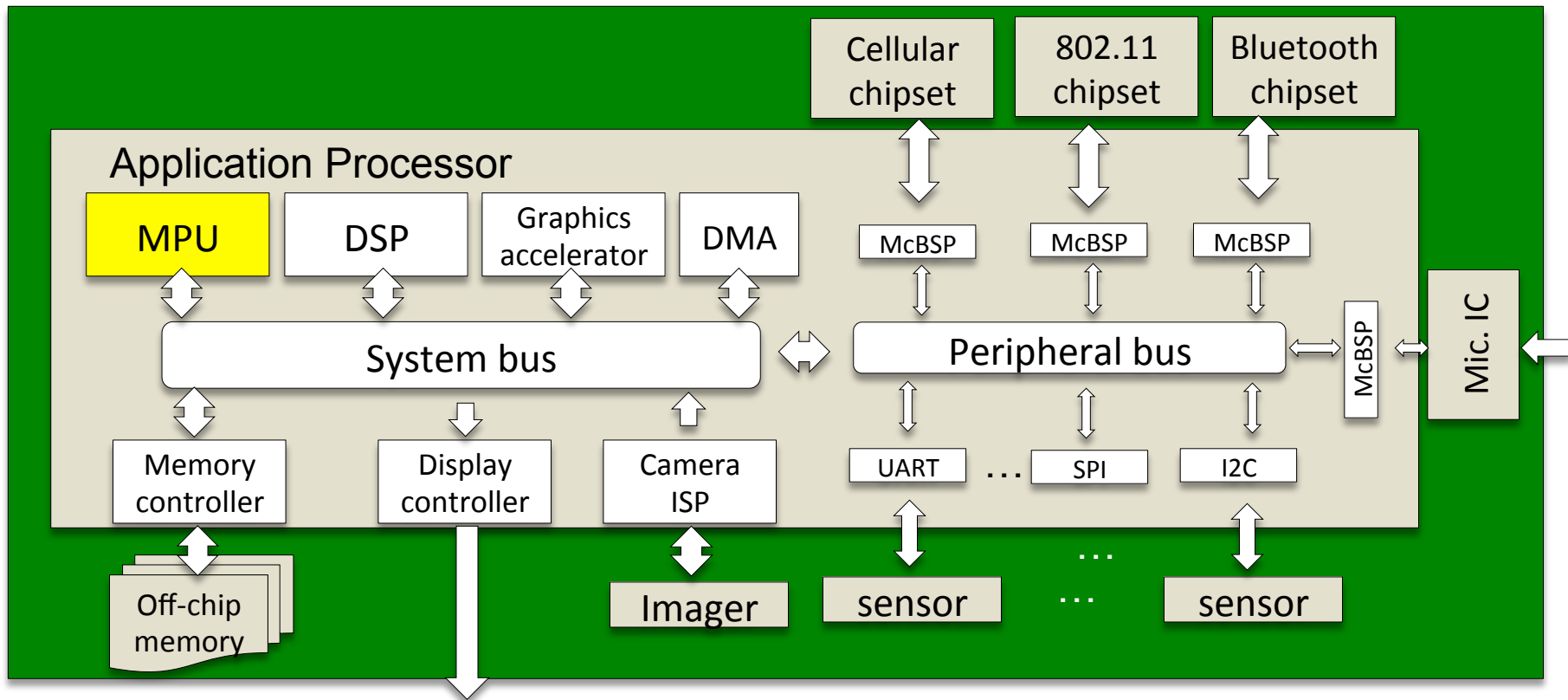
Mian Dong, Tian Lan and *Lin Zhong*

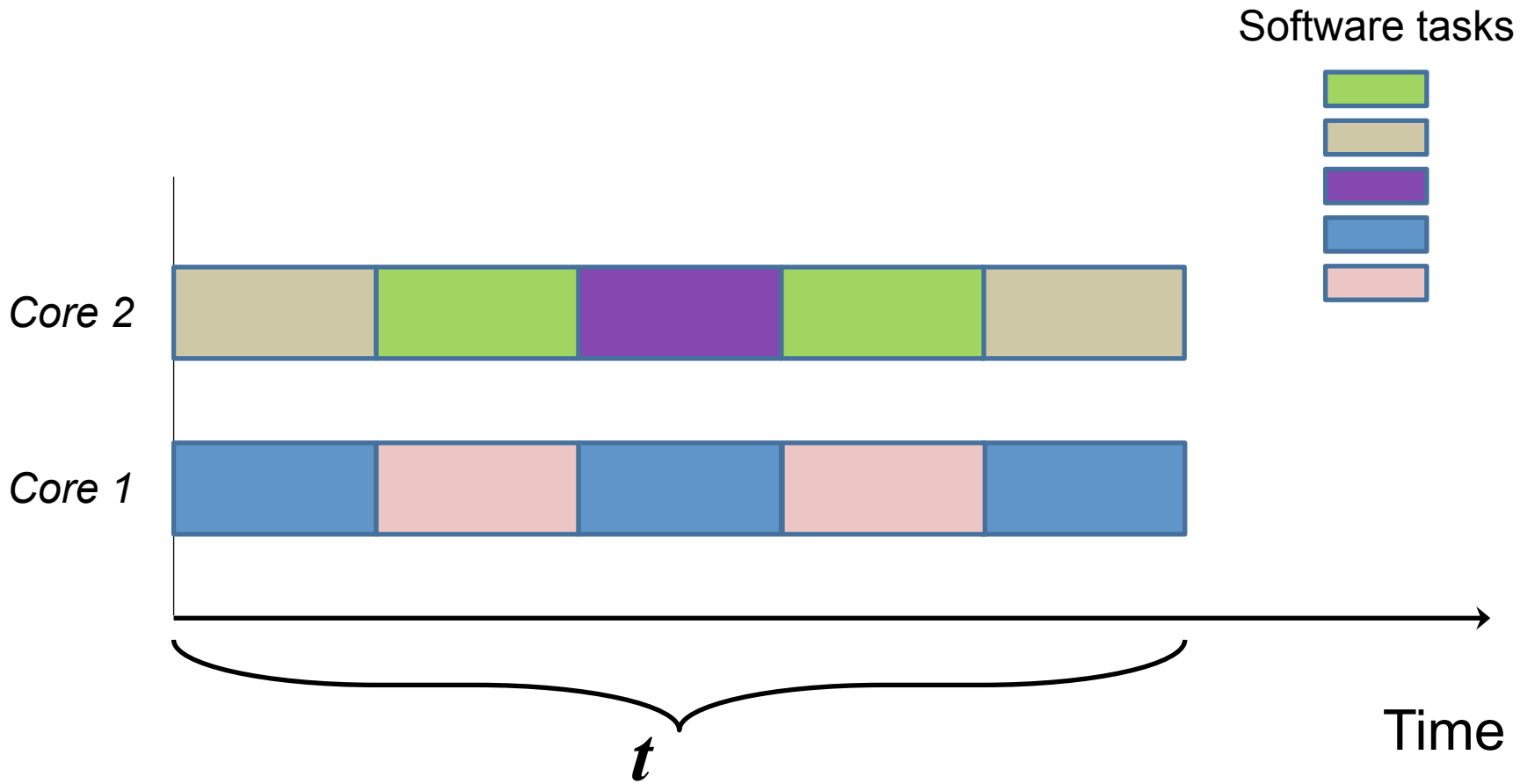
# Energy accounting by software

How much energy does a process contribute given a time interval?

# Modern mobile systems are multiprocessing

More cores, more types of cores, and more specialized cores





# Model-driven policy

$$E = \beta_0 + \beta_1 x_1 + \dots + \beta_p x_p$$

Predictors  $x_j$ : System status variables

$n$  tasks contribute to the predictors

$$\begin{array}{r} x_1 = x_{1,1} + \dots + x_{1,n} \\ \vdots \\ x_p = x_{p,1} + \dots + x_{p,n} \end{array}$$

Energy contribution by process  $i$

$$\phi_i = \beta_1 x_{1,i} + \dots + \beta_p x_{p,i}$$

# Problems

$$E = \beta_0 + \beta_1 x_1 + \dots + \beta_p x_p$$

**Predictors** must be software accountable

**Model** must be linear

**Constant factor** ( $\beta_0$ )

# Lone-wolf policy

$\phi_i = E(\mathbf{S} \cup \{i\}) - E(\mathbf{S})$  often  $\mathbf{S}$  is an idle system

*Problem:*  $\phi_i + \phi_j \neq E(\mathbf{S} \cup \{i, j\})$

Lin Zhong and Niraj K. Jha, "Graphical user interface energy characterization for handheld computers", in *Proc. Int. Conf. on Compilers, Architectures & Synthesis for Embedded Systems (CASES)*, Oct. 2003.

How can we evaluate an energy accounting policy?



# How to split the utility bill?



# How to split the profit?



$N = \{1, 2, \dots, n\}$

set of players

$S$

subset of  $N$  (coalition)

$v(S)$

game surplus when  $S$  plays

$\phi_i(S)$

surplus received by player  $i$

# Shapley Value

How to determine the contribution of each individual player in a multi-player game?

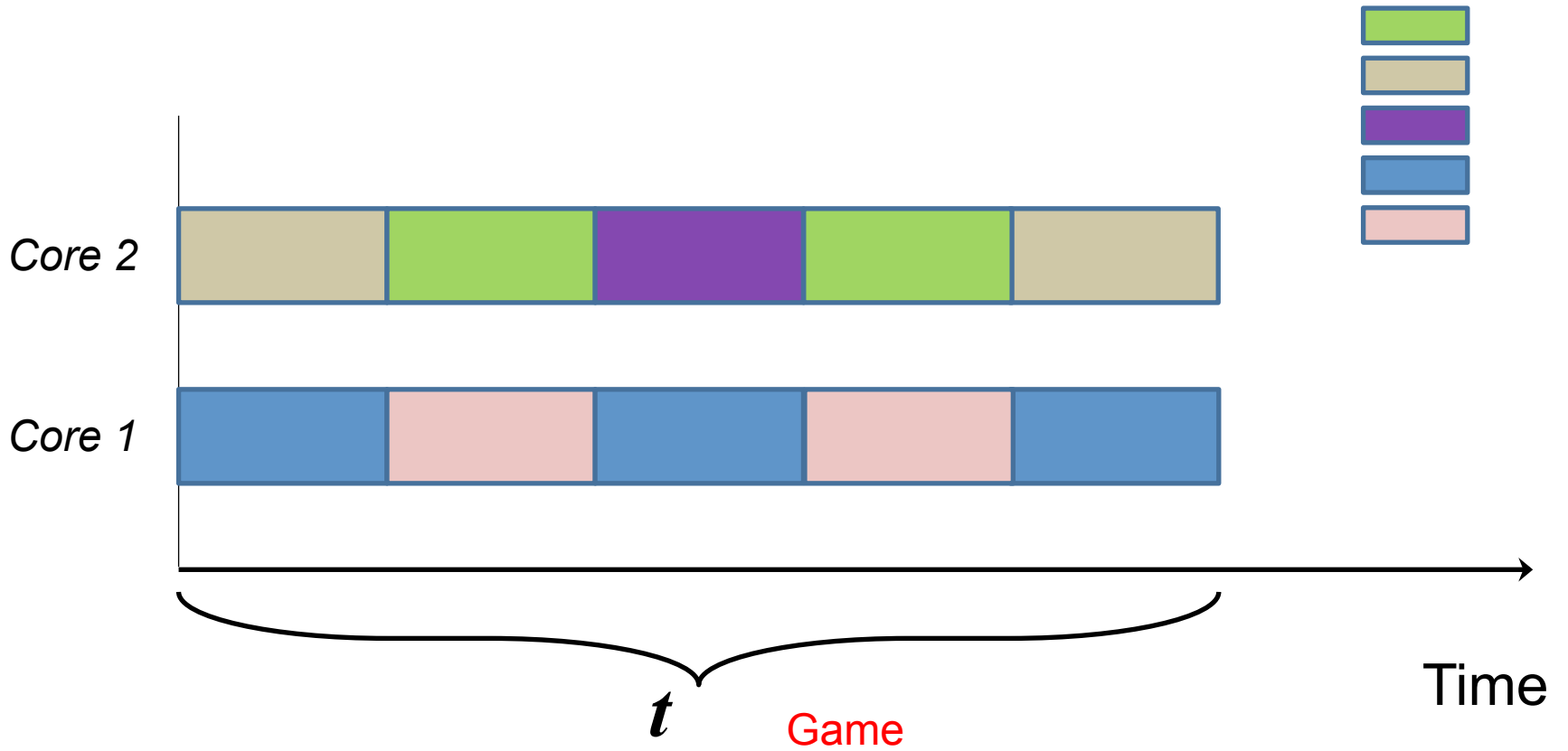
Four axioms determines a unique distribution

L. S. Shapley, *A value for  $n$ -person games*: In Contributions to the Theory of Games, volume II, Annals of Mathematical Studies v. 28, pp. 307–317, Princeton Univ. Press, 1953.

System energy consumption ( $E$ ): game surplus ( $v$ )

Players ( $N$ )

Software tasks



# **Axiom 1: Efficiency**

*The sum of the energy contributions by all tasks equals the system energy consumption.*

## **Axiom 2: Symmetry**

*If replacing one with another will not change the system energy consumption under any circumstances, two tasks should have the same energy contributions.*

## **Axiom 3: Null Player**

*If adding a task under any circumstances does not increase system energy consumption, this task should have zero energy contribution.*



## **Axiom 4: Additivity**

*The same energy attribution policy should work for all the time intervals.*

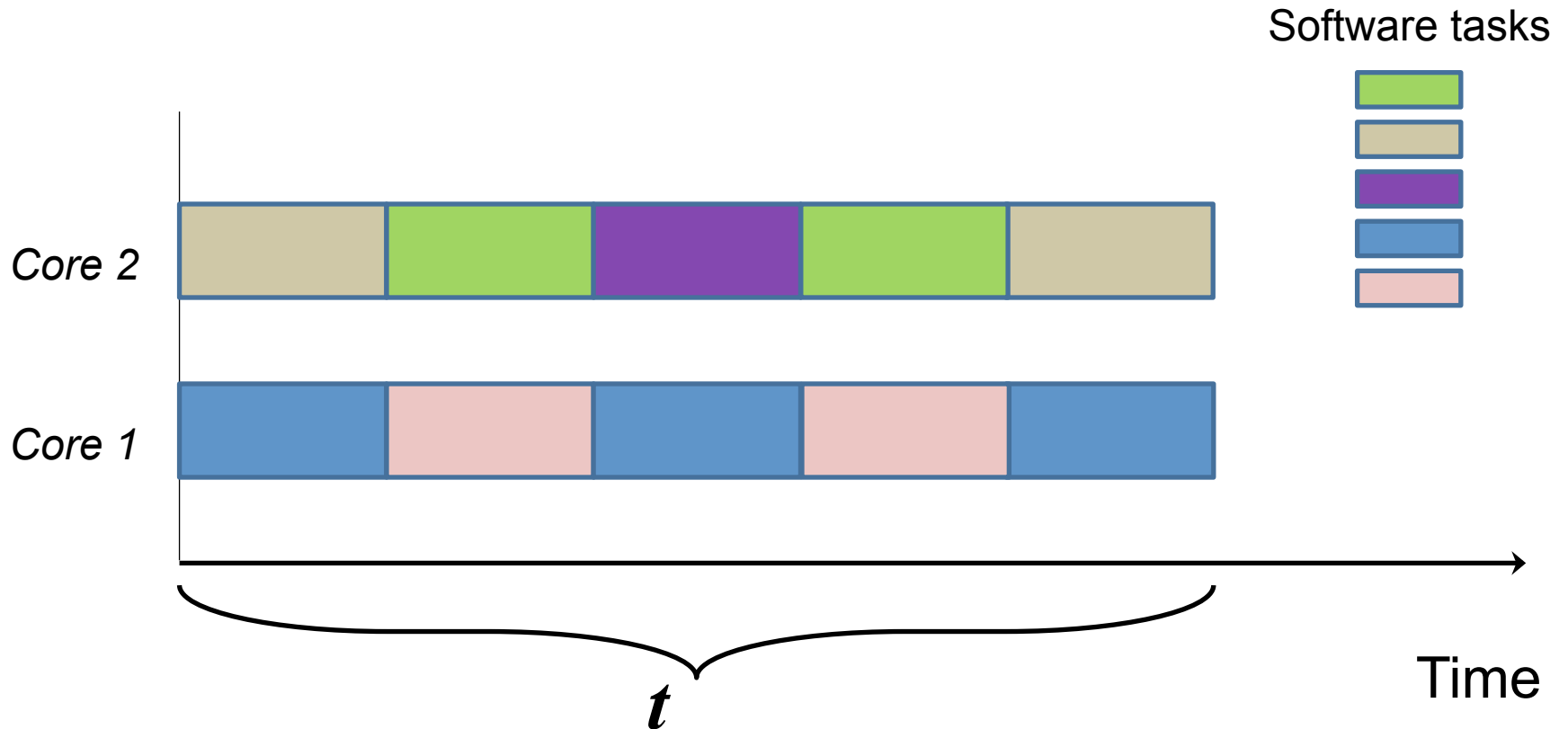
# Shapley Value

$$\phi_i(E(\mathbf{N})) = \sum_{\mathbf{S} \subseteq \mathbf{N} \setminus \{i\}} \frac{E(\mathbf{S} \cup \{i\}) - E(\mathbf{S})}{(|\mathbf{N}| - |\mathbf{S}|) \binom{|\mathbf{N}|}{|\mathbf{S}|}}$$

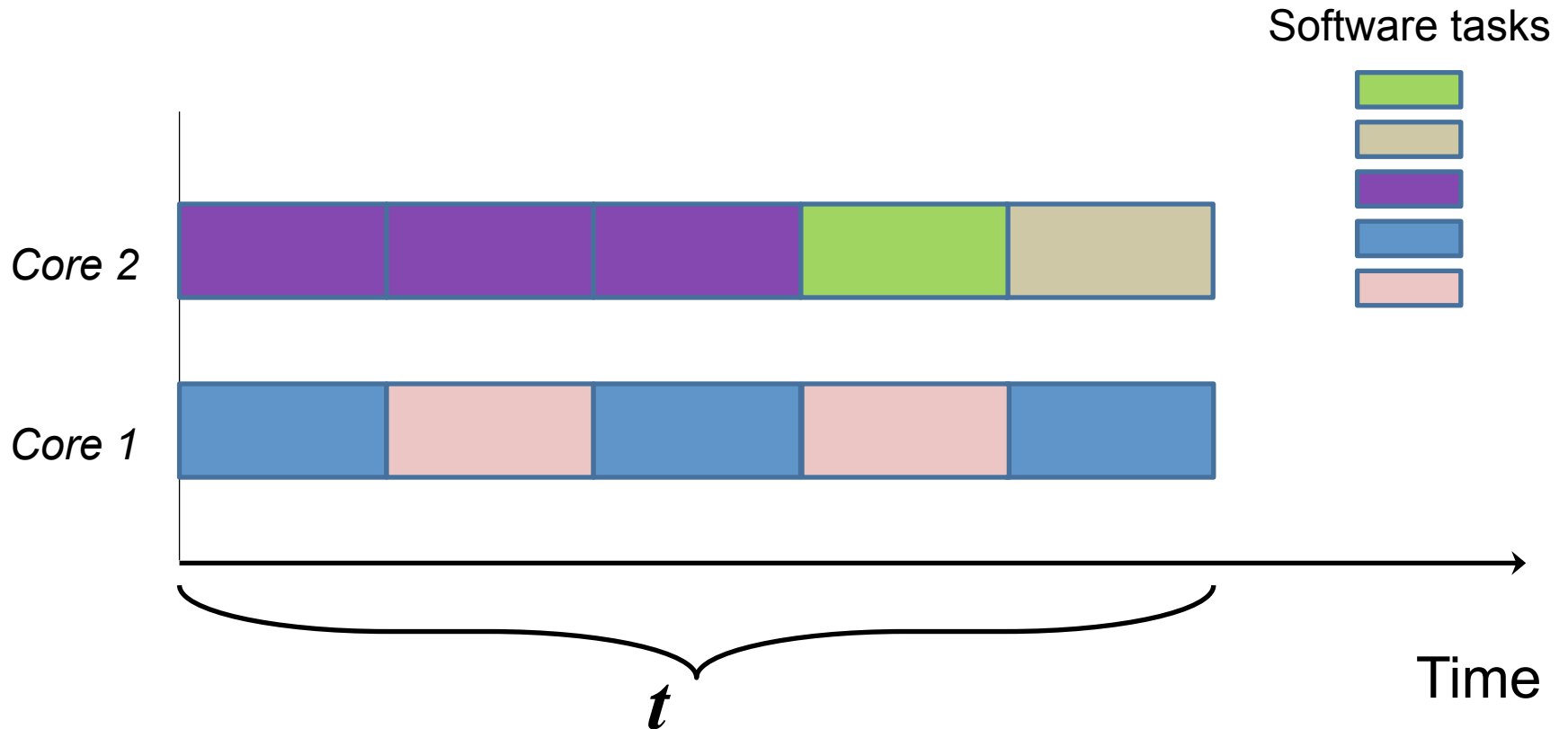
# Systems challenges

- $E(\mathbf{S})$  is highly random
- $E(\mathbf{S})$  not available for many  $\mathbf{S}$
- $E(\mathbf{S})$  depends on hardware configuration

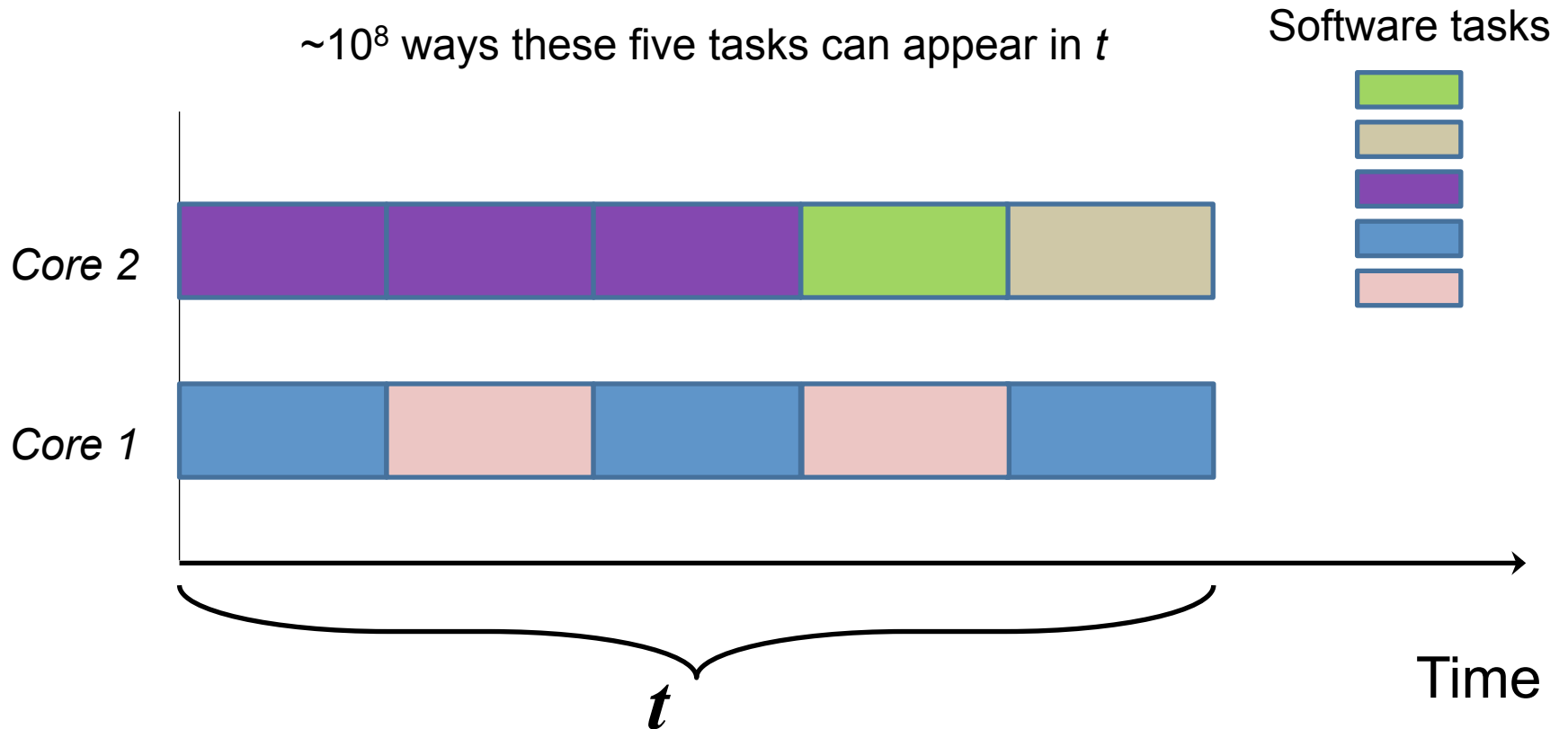
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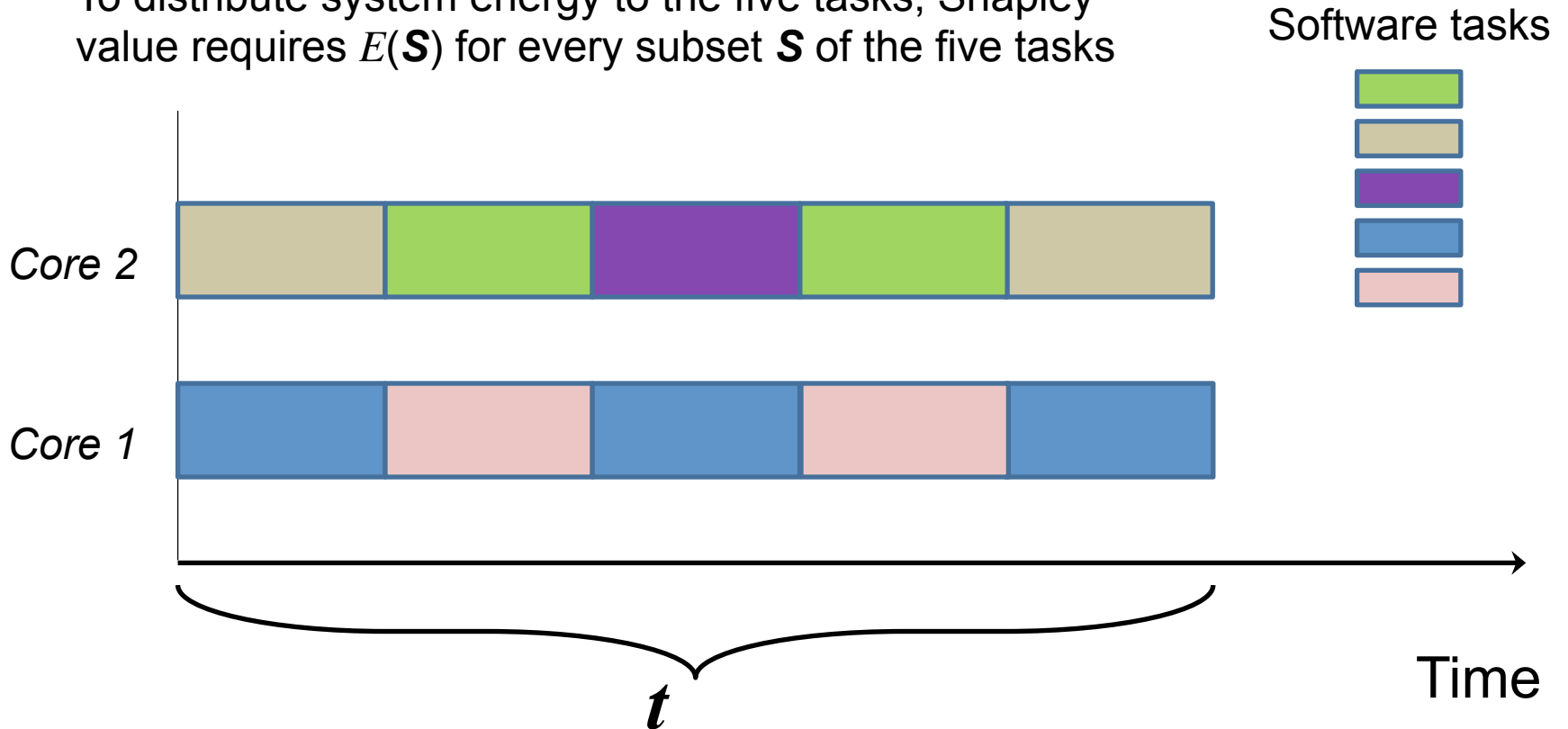


# Challenge I: Shapley value only cares about IF a player participates in a game but not HOW



# Challenge II: Not all combinations of tasks have been observed

To distribute system energy to the five tasks, Shapley value requires  $E(\mathbf{S})$  for every subset  $\mathbf{S}$  of the five tasks

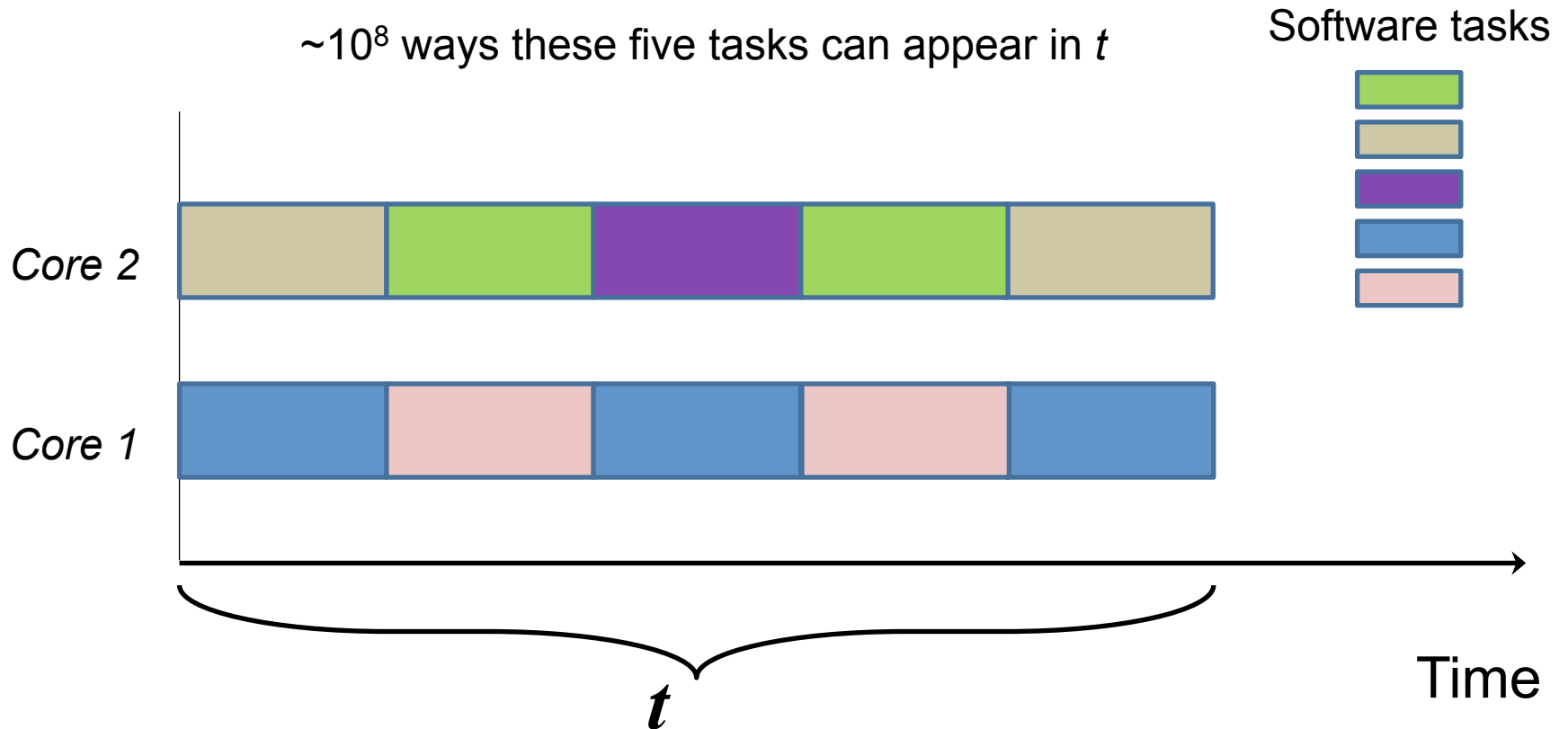


# Solutions

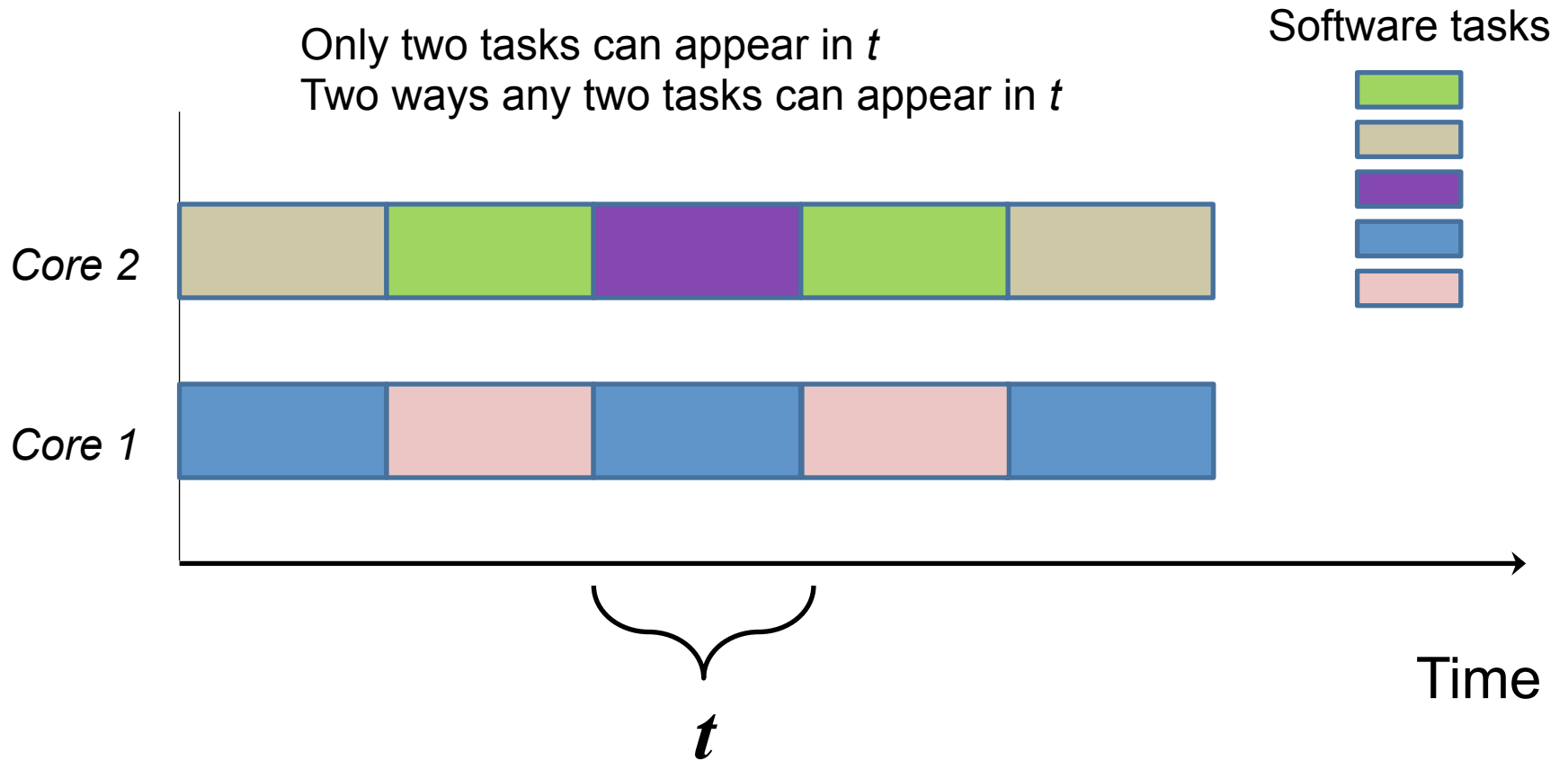
- $E(\mathbf{S})$  is highly random
- $E(\mathbf{S})$  not available for all  $\mathbf{S}$ 
  - Estimate  $E$  for short time interval (10 ms)
- $E(\mathbf{S})$  depends on hardware configuration



# Challenge I: Shapley value only cares about IF a player participates in a game but not HOW

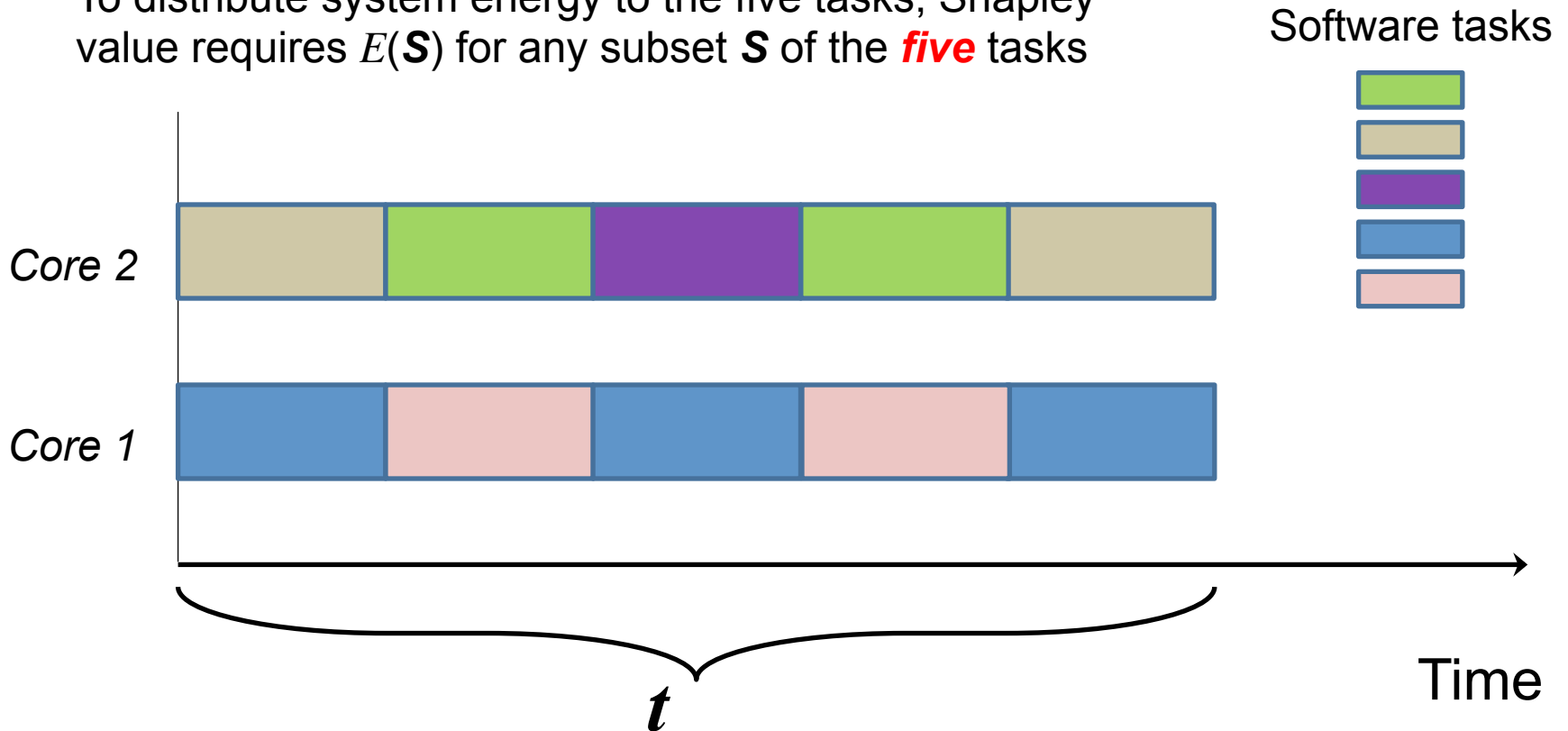


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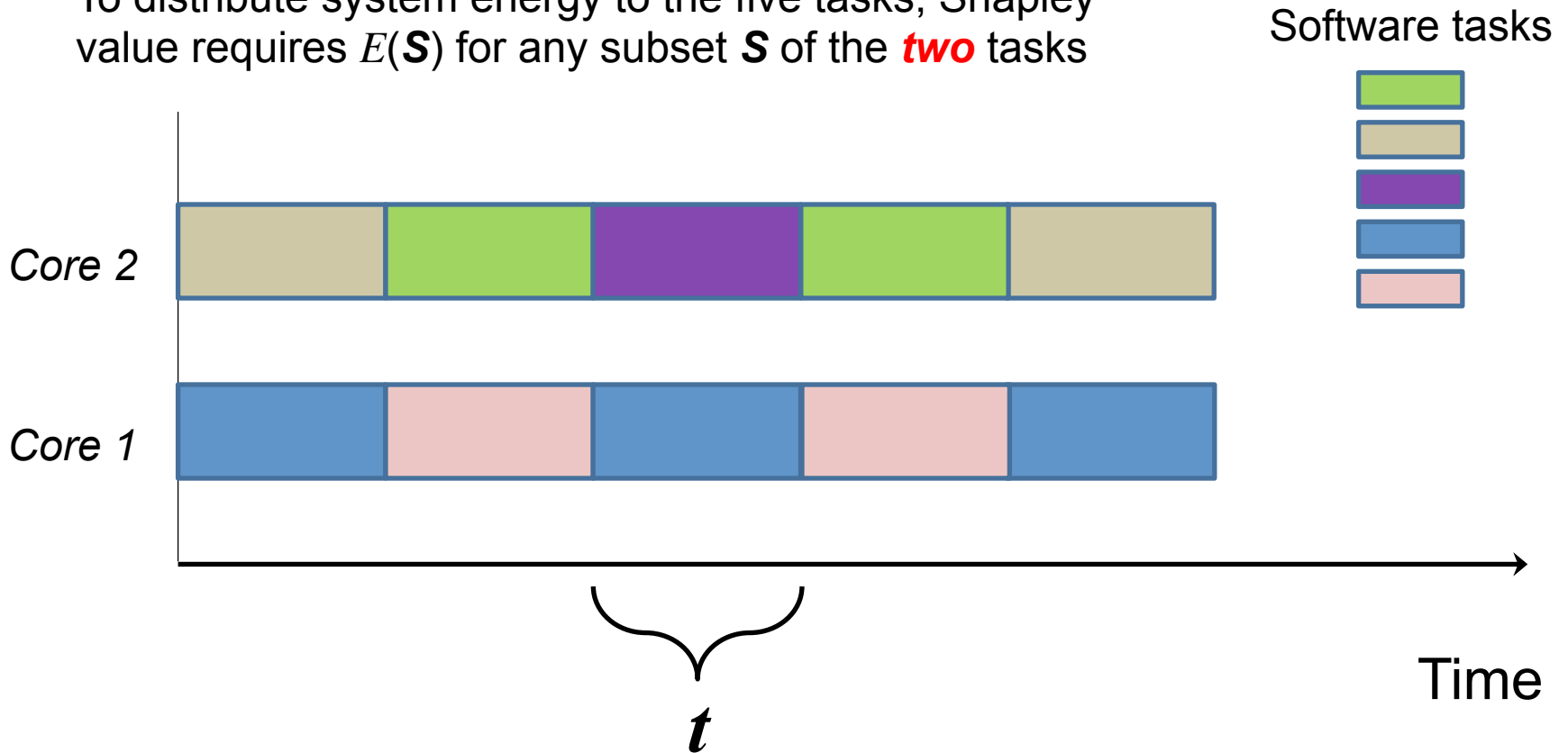
# Challenge II: Not all combinations of tasks have been observed

To distribute system energy to the five tasks, Shapley value requires  $E(\mathbf{S})$  for any subset  $\mathbf{S}$  of the **five** tasks



# Challenge II: Not all combinations of tasks have been observed

To distribute system energy to the five tasks, Shapley value requires  $E(\mathbf{S})$  for any subset  $\mathbf{S}$  of the **two** tasks



# Solutions

- $E(\mathbf{S})$  is highly random
- $E(\mathbf{S})$  not available for all  $\mathbf{S}$ 
  - Estimate  $E$  for short time interval (10 ms)
  - Estimate  $E$  *in situ*
- $E(\mathbf{S})$  depends on hardware configuration

# Smart battery interface

- Machine learning techniques (~80%)
  - *Dong and Zhong (MobiSys 2011)*
- Improved hardware/software (~95%)

# Solutions

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  - Use the crowd
- $E(\mathbf{S})$  depends on hardware configuration

# Solutions

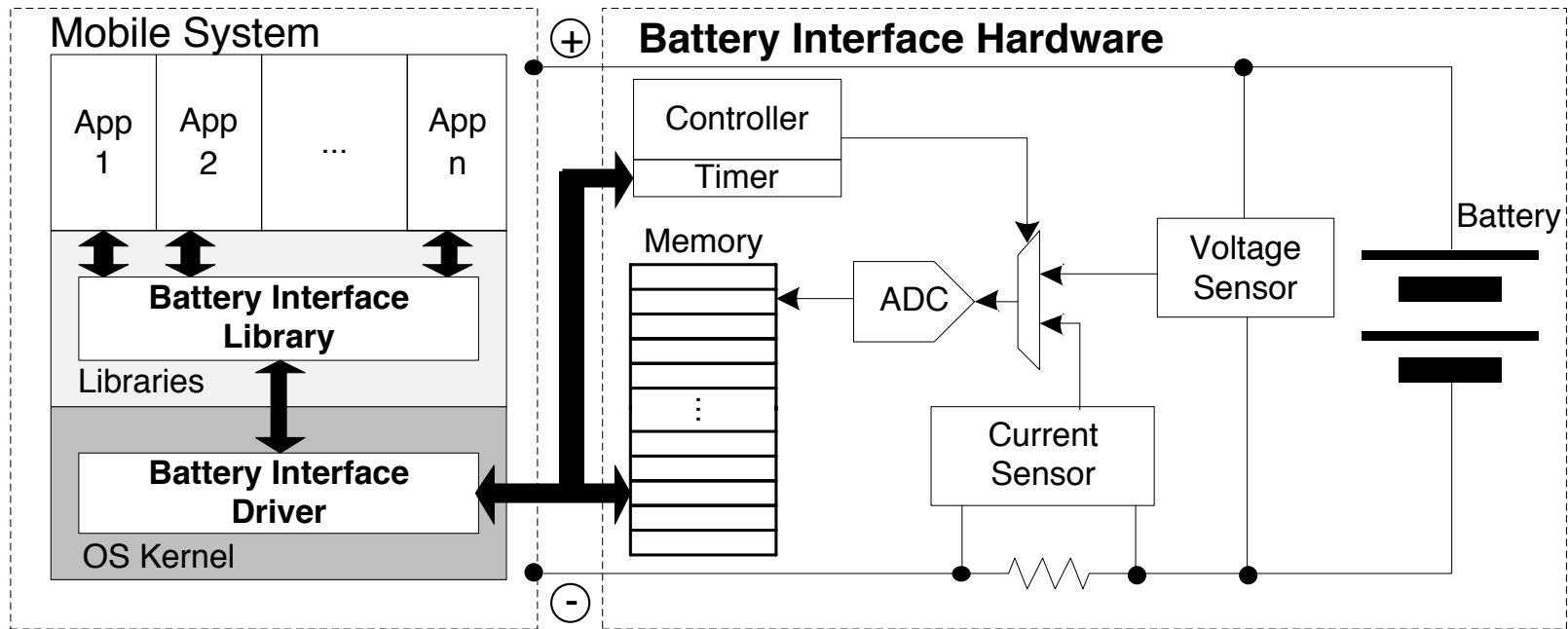
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  - Use the crowd
  - Extend Shapley Value framework
- $E(\mathbf{S})$  depends on hardware configuration



# Extend Shapley Value framework

- Approximate unknown  $E(\mathbf{S})$  by their per-task energy cost allocations
- Example
  - Tasks:  $\{1, 2, 3\}$
  - $E(\mathbf{S})$  known for  $\mathcal{S} = \{1,2,3\}, \{2,3\}, \{1\}, \{2\}$
  - $E(\mathbf{S})$  can be recursively estimated for others
    - $\hat{E}(\{3\}) = E(\{1,2,3\}) - E(\{1\}) - E(\{2\})$
    - $\hat{E}(\{1,2\}) = E(\{1\}) + E(\{2\})$
    - $\hat{E}(\{1,3\}) = E(\{1\}) + E(\{3\})$

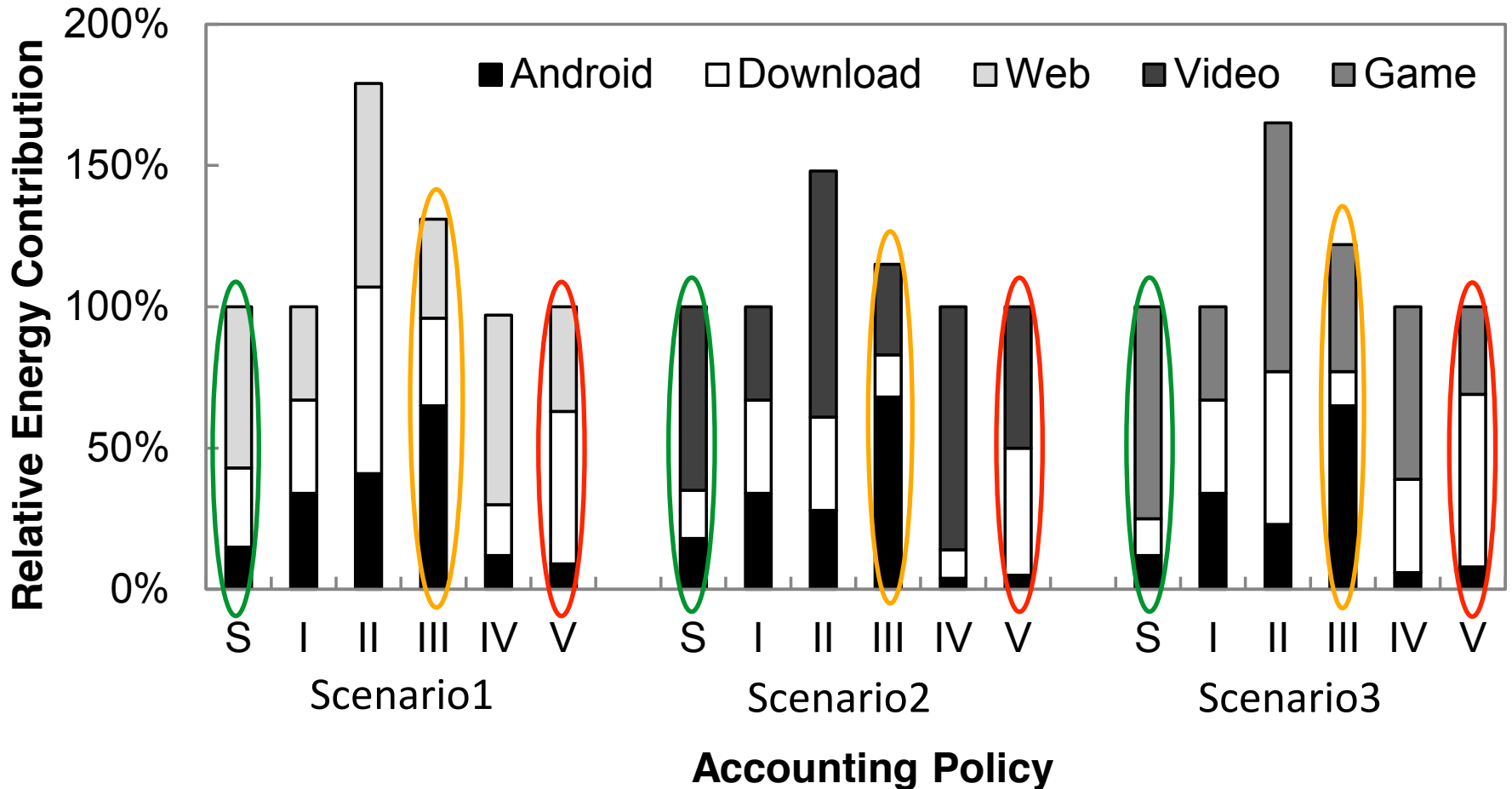
# Prototype implementation



Texas Instruments Pandaboard  
(OMAP4430) with Android

MAXIM DS2756 battery fuel  
gauge

# Evaluating existing policies



III = Lone-Wolf

V = Model-driven

# Conclusions

- Shapley value as ground truth for energy accounting
- System challenges can be addressed