

# Modeling program semantics in an automated program verifier

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# Dafny

Programming language  
designed for *reasoning*

Language features drawn from:

Imperative programming

*if, while, :=, class, ...*

Functional programming

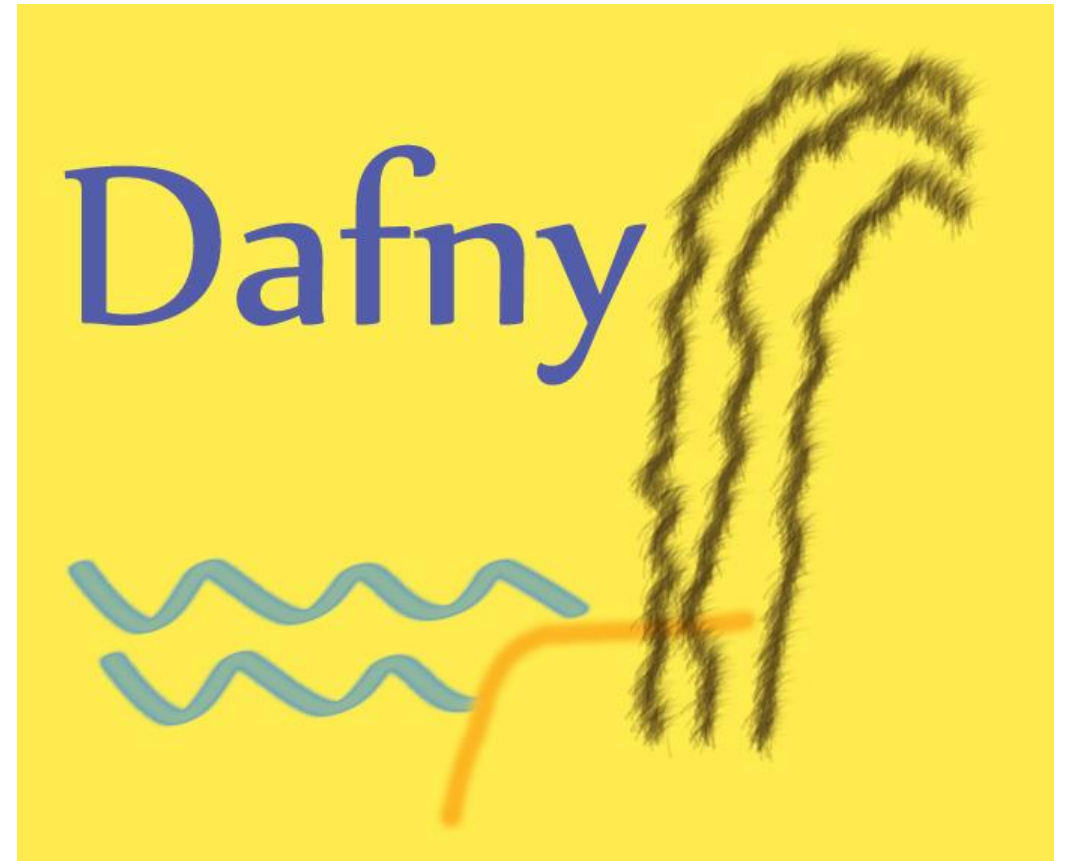
*function, datatype, codatatype, ...*

Proof authoring

*Lemma, calc, refines, inductive  
predicate, ...*

Program verifier

Integrated development  
environment (IDE)



# Uses of Dafny

In projects

ExpressOS [ASPLOS 2013]

CloudMake algorithms [FM 2014]

Ironclad Apps [OSDI 2014]

IronFleet [SOSP 2015]

Program verification competitions

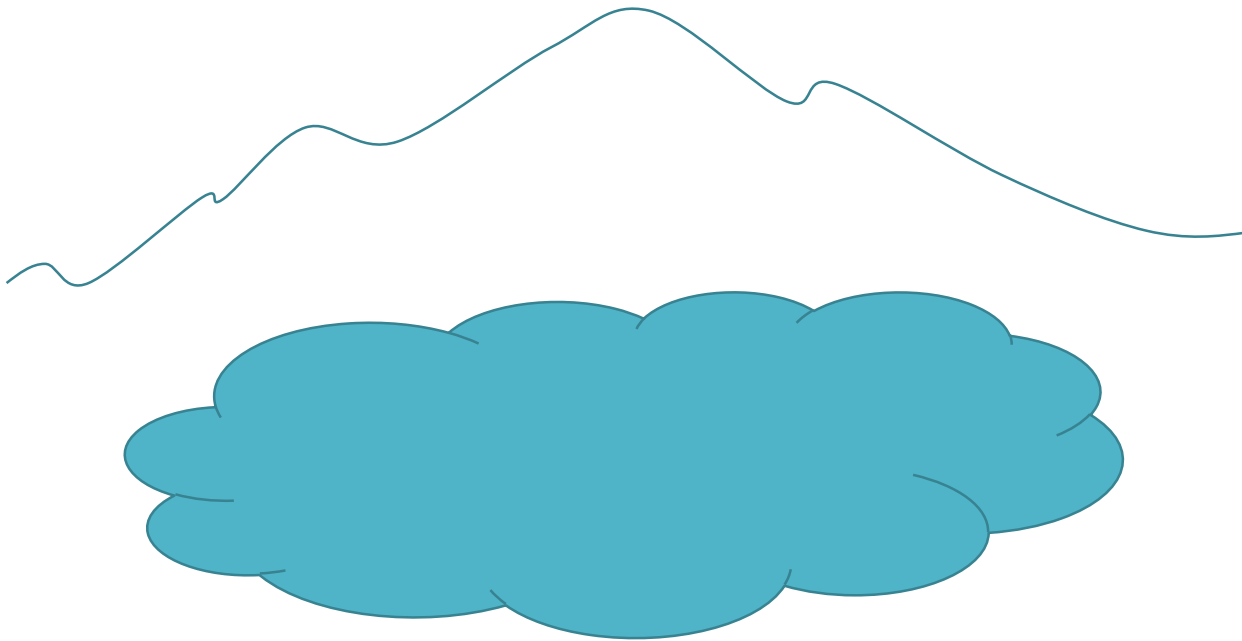
VerifyThis

VS Comp

In teaching

At over 30 universities (including UW 😊)

# Everest expedition: Everest Verified End-to-end Secure Transport



Verified,  
Performant,  
Deployed  
HTTPS

# What's in it for PL peeps?

“Can I prove the soundness of my language semantics?”

# Semantics of INC

Cmd ::= Inc | Cmd ; Cmd | Repeat(Cmd)

$$\frac{t = s+1}{(\text{Inc}, s) \rightarrow t}$$

$$\frac{(c0, s) \rightarrow s' \quad (c1, s') \rightarrow t}{(c0 ; c1, s) \rightarrow t}$$

$$\frac{t = s}{(\text{Repeat}(body), s) \rightarrow t}$$

$$\frac{(body, s) \rightarrow s' \quad (\text{Repeat}(body), s') \rightarrow t}{(\text{Repeat}(body), s) \rightarrow t}$$

# Semantics of INC

Cmd ::= Inc | Cmd;<sup>□</sup>Cmd | Repeat(Cmd)

$$\frac{t = s+1}{(\text{Inc}, s) \rightarrow t}$$

$$\frac{\exists s'. (c0, s) \rightarrow s' \quad (c1, s') \rightarrow t}{(c0;<sup>□</sup>c1, s) \rightarrow t}$$

$$\frac{t = s}{(\text{Repeat}(body), s) \rightarrow t}$$

$$\frac{\exists s'. (body, s) \rightarrow s' \quad (\text{Repeat}(body), s') \rightarrow t}{(\text{Repeat}(body), s) \rightarrow t}$$

# Demo

## INC

```
datatype cmd = Inc | Seq(cmd, cmd) | Repeat(cmd)
type state = int

inductive predicate BigStep(c: cmd, s: state, t: state)
{
  match c
  case Inc =>
    t == s + 1
  case Seq(c0, c1) =>
    exists s' :: BigStep(c0, s, s') && BigStep(c1, s', t)
  case Repeat(body) =>
    s == t ||
    exists s' :: BigStep(body, s, s') && BigStep(c, s', t)
}

inductive lemma Monotonic(c: cmd, s: state, t: state)
  requires BigStep(c, s, t)
  ensures s <= t
{
  match c
  case Inc =>
    // trivial
  case Seq(c0, c1) =>
    var s' :| BigStep(c0, s, s') && BigStep(c1, s', t);
    Monotonic(c0, s, s');
    Monotonic(c1, s', t);
  case Repeat(body) =>
    if s == t {
      // trivial
    } else {
      var s' :| BigStep(body, s, s') && BigStep(c, s', t);
      Monotonic(body, s, s');
      Monotonic(c, s', t);
    }
}
```



# Conclusions

Dafny is a programming language and program verifier

Dafny now supports inductive/co-inductive predicates

Encoded in a first-order induction-unaware fixpoint-unaware IVL/SMT\*

Do your language semantics in Dafny!

Also, see Nada Amin's talk "How to write your next POPL paper using Dafny"

Try Dafny online: [rise4fun.com/dafny](http://rise4fun.com/dafny)

Sources: [dafny.codeplex.com](http://dafny.codeplex.com)

[research.microsoft.com/verificationcorner](http://research.microsoft.com/verificationcorner)

\*) ask me how