CSE531: Complexity Theory	April 24, 2020
Homework 2	
Anup Rao	Due: May 1, 2020

Read the fine print¹. Each problem is worth 10 points:

- 1. Prove that $L \neq \mathsf{DTIME}(n^{\log n})$.
- 2. Show that if $3SAT \in DTIME(2^{\log^2(n)})$, then $NP \neq EXP$.
- 3. Given an integer $m \times n$ matrix A and an integer column vector b of length m, the 0-1 Integer Programming function is defined as follows:

$$\mathbf{IP}(A,b) = \begin{cases} 1 & \text{if there is a length } n \text{ binary vector } x \text{ that satisfies } Ax \ge b \\ 0 & \text{otherwise.} \end{cases}$$

Here $Ax \geq b$ means that every coordinate of Ax is at least as large as the corresponding coordinate of b. Prove that **IP** is **NP**-complete, by reducing **3SAT** to it.

4. Let HALT be the halting function we defined in class (i.e. $HALT(\alpha, x) = 1$ iff $M_{\alpha}(x)$ halts). Show that HALT is **NP**-hard. Is it **NP**-complete?

¹In solving the problem sets, you are allowed to collaborate with fellow students taking the class, but **each** submission can have at most one author. If you do collaborate in any way, you must acknowledge, for each problem, the people you worked with on that problem. The problems have been carefully chosen for their pedagogical value, and hence might be similar to those given in past offerings of this course at UW, or similar to other courses at other schools. Using any pre-existing solutions from these sources, for from the web, constitutes a violation of the academic integrity you are expected to exemplify, and is strictly prohibited. Most of the problems only require one or two key ideas for their solution. It will help you a lot to spell out these main ideas so that you can get most of the credit for a problem even if you err on the finer details. Please justify all answers. Some other guidelines for writing good solutions are here: http://www.cs.washington.edu/education/courses/cse421/08wi/guidelines.pdf.