1. Exercises

1.1 Running AutoBayes

1.1.1 Exercise 1

Run the norm.ab example and inspect generated code and derivation. If possible, generate the latex version of the derivation.

```
1 model normal_simple as 'NORMAL MODEL WITHOUT PRIORS'.
2
3 double mu.
4 double sigma_sq as 'SIGMA SQUARED'.
5 where 0 < \text{sigma_sq}.
6
7 const nat n as '# DATA POINTS'.
8 where 0 < n.
9
10 data double x(0..n-1) as 'KNOWN DATA POINTS'.
11 x(_) \sim \text{gauss}(\text{mu, sqrt}(\text{sigma_sq})).
12
13 max pr(x \mid \{\text{mu, sigma_sq}\}) for \{\text{mu, sigma_sq}\}.
```

Listing 1.1: norm.ab

1.1.2 Exercise 2

Generate multiple versions for this problem. Note: use the appropriate flags to allow AUTOBAYES to generate numerical optimization algorithms: (schema_control_arbitrary_init_values)

1.1.3 Exercise 3

Modify the "norm" example to use a different probability density function. Note that some of them do have a different number of parameters. Inspect the generated code and derivation. Can the problem be solved symbolically for all PDFs?

Hint: use vonmises1, poisson, weibull, cauchy

1.1.4 Exercise 4

Generate multiple versions for the mixture-of-gaussians example. What are the major differences between the different synthesized programs.

Note: the specification is mog.ab in the models_manual directory.

Generate a sampling data generator (autobayes -sample) for this specification.

In AutoBayes generate 1000 data points that go into 3 different classes. Then run the different programs and see how good they estimate the parameters.

Note: the generated functions require column-vectors, so, e.g., give the means as [1,2,3]'

Listing 1.2: calling the synthesized code in Octave

1.1.5 Exercise 5

Run a change-point detection model (e.g., climb_transition.ab and look at generated code and derivation. How does AUTOBAYES find the maximum?

1.1.6 Exercise 6

Add the Pareto distribution to the built-in transitions. Get the formulas from wikipedia.

Try the following simple model:

```
1 model pareto as 'NORMAL MODEL WITHOUT PRIORS'.
2
3 double alpha.
           where 3 < alpha.
4
<sup>5</sup> const double xm.
    where 0 < xm.
6
7
8 const nat n as '# DATA POINTS'.
    where 0 < n.
9
10
11 data double x(0..n-1) as 'KNOWN DATA POINTS'.
           where 0 < x(_).
12
```

13 where xm < x(_).
14
15 x(_) ~ pareto(xm, alpha).
16
17 max pr(x | {alpha}) for {alpha}.</pre>

Listing 1.3: Specification for Pareto distribution

```
1 octave -3.4.0:2> xm=5;
2 octave -3.4.0:3> alpha=15;
3 octave -3.4.0:4> x=xm*(1./(1-rand(10000,1)).^(1/alpha));
4 octave -3.4.0:5> alpha_est = pareto(x,5)
5 alpha_est = 15.081
```

Listing 1.4: Generate Pareto-distributed random numbers