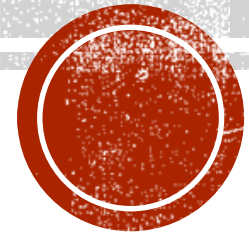


# ERROR-CORRECTING CODES

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# AGENDA

- What are Error-Correcting Codes?
- How do they work?
- Example: Hamming Codes (7,4)
- Types of Error-Correcting Codes
- Applications



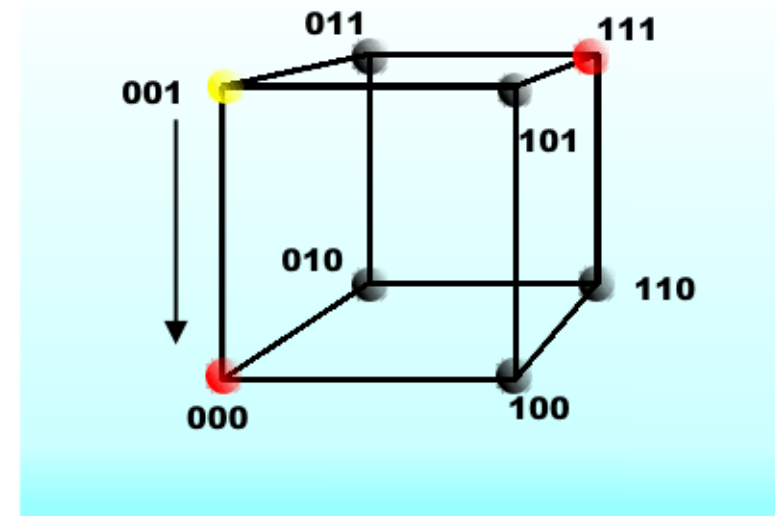
# WHAT ARE ERROR-CORRECTING CODES?

- Basic idea: add redundant bits
- Code Rate: Proportion of data-stream that is useful
  - Denoted as  $\text{Code}(n, k)$ ,  $n > k$ , generates  $n$  bits for every  $k$  bits
  - Code Rate =  $k / n$
- Error Detection Vs Error Correction
- How much errors can be corrected?
  - Shannon Limit 1948:
    - The theoretical maximum information transfer rate of the channel
    - **Shannon theorem:** "Given a noisy channel with channel capacity  $C$  and information transmitted at a rate  $R$ , then if  $R < C$  there exist codes that allow the probability of error at the receiver to be made arbitrarily small"

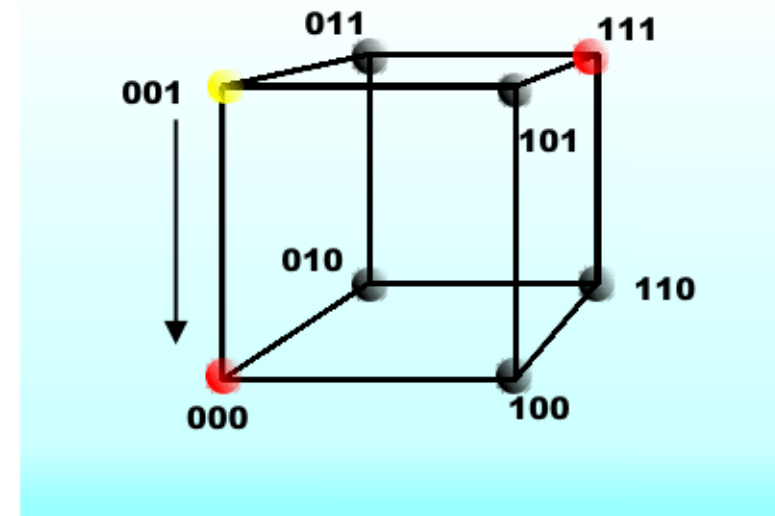


# HOW IT WORKS?

Triplet received	Interpreted as
000	0 (error free)
001	0
010	0
100	0
111	1 (error free)
110	1
101	1
011	1

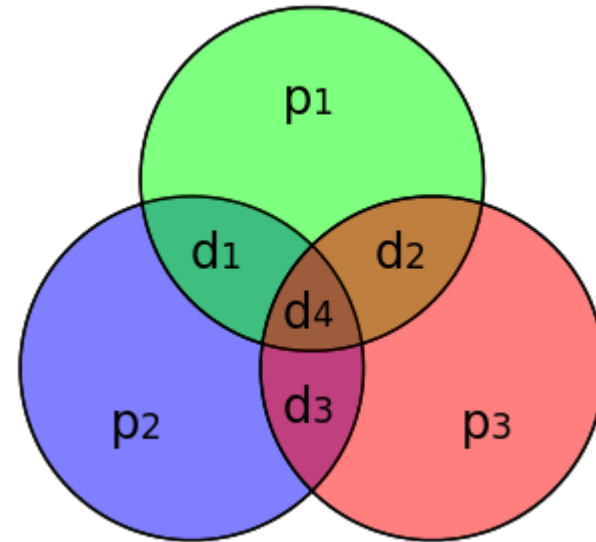


- In general, to correct  $m$  bits, each valid symbol has to be surrounded by a sphere of radius  $m+1$  of invalid codes.



# EXAMPLE: HAMMING CODE (7,4)

- Introduced by Richard Hamming in 1950, then was frustrated with the error-prone punched card reader
- For every 4 bits of data: d1, d2, d3, d4
- Add 3 parity bits: p1, p2, p3
- Transmit: p1 p2 d1 p3 d2 d3 d4



# TYPES OF ERROR-CORRECTING CODES

- Convolutional Codes:
  - Sliding window on bit streams of arbitrary length
  - Most often decoded with the Viterbi algorithm
- Block Codes:
  - Work on fixed-size blocks of bits
  - Generally decoded in polynomial time to their block length
  - E.g. Reed-Solomon Code, Golay, BCH, Multidimensional parity, and Hamming codes.
- Turbo Codes:
  - Combines two or more relatively simple convolutional codes and an interleaver to produce a block code



# APPLICATIONS

- Convolutional codes used in:
  - both CDMA and GSM digital cellular
  - dial-up modems
  - Satellite and deep-space communications
  - 802.11 wireless LANs
- Reed-Solomon coding has widespread use on the Compact disc, the DVD, and in hard disk drives
- Hamming ECC is commonly used to correct single level cell NAND flash memory errors





# APPLICATIONS (2)

- LDPC codes are now used in many recent high-speed communication standards:
  - [DVB-S2](#) (Digital video broadcasting)
  - [WiMAX](#) (IEEE 802.16e standard for microwave communications)
  - High-Speed Wireless LAN (IEEE 802.11n)
  - [10GBase-T Ethernet](#) (802.3an)
  - [G.hn/G.9960](#) (ITU-T Standard for networking over power lines, phone lines and coaxial cable).
- Turbo coding [CDMA2000 1x](#) and EV-DO
  - Digital cellular technology developed by [Qualcomm](#) and sold by [Verizon Wireless](#), [Sprint](#), and other carriers.



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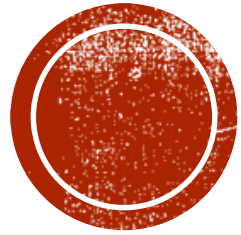
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# THANK YOU

Questions?