

# CSE 403

Software Engineering

Winter 2023

**Program analysis**

# This week: Program analysis

- Reasoning about programs (Today)
- Statistical fault localization (Wednesday)
- In-class exercise (Friday)

# Recap: Delta Debugging

# Recap: Delta Debugging

Step	Test case									
1	$\Delta_1 = \nabla_2$	1	2	3	4	.	.	.	.	Testing $\Delta_1, \Delta_2$
2	$\Delta_2 = \nabla_1$	.	.	.	.	5	6	7	8	$\Rightarrow$ Increase granularity
3	$\Delta_1$	1	2	.	.	.	.	.	.	Testing $\Delta_1, \dots, \Delta_4$
4	$\Delta_2$	.	.	3	4	.	.	.	.	
5	$\Delta_3$	.	.	.	.	5	6	.	.	
6	$\Delta_4$	.	.	.	.	.	.	7	8	
7	$\nabla_1$	.	.	3	4	5	6	7	8	Testing complements
8	$\nabla_2$	1	2	.	.	5	6	7	8	$\Rightarrow$ Reduce to $c'_x = \nabla_2$ ; continue with $n = 3$
9	$\Delta_1$	1	2	.	.	.	.	.	.	Testing $\Delta_1, \Delta_2, \Delta_3$
10	$\Delta_2$	.	.	.	.	5	6	.	.	* same <i>test</i> carried out in an earlier step
11	$\Delta_3$	.	.	.	.	.	.	7	8	
12	$\nabla_1$	.	.	.	.	5	6	7	8	Testing complements
13	$\nabla_2$	1	2	.	.	.	.	7	8	$\Rightarrow$ Reduce to $c'_x = \nabla_2$ ; continue with $n = 2$
14	$\Delta_1 = \nabla_2$	1	2	.	.	.	.	.	.	Testing $\Delta_1, \Delta_2$
15	$\Delta_2 = \nabla_1$	.	.	.	.	.	.	7	8	$\Rightarrow$ Increase granularity
16	$\Delta_1$	1	.	.	.	.	.	.	.	Testing $\Delta_1, \dots, \Delta_4$
17	$\Delta_2$	.	2	.	.	.	.	.	.	
18	$\Delta_3$	.	.	.	.	.	.	7	.	
19	$\Delta_4$	.	.	.	.	.	.	.	8	
20	$\nabla_1$	.	2	.	.	.	.	7	8	Testing complements
21	$\nabla_2$	1	.	.	.	.	.	7	8	$\Rightarrow$ Reduce to $c'_x = \nabla_2$ ; continue with $n = 3$
22	$\Delta_1$	1	.	.	.	.	.	.	.	Testing $\Delta_1, \dots, \Delta_3$
23	$\Delta_2$	.	.	.	.	.	.	7	.	
24	$\Delta_3$	.	.	.	.	.	.	.	8	
25	$\nabla_1$	.	.	.	.	.	.	7	8	Testing complements
26	$\nabla_2$	1	.	.	.	.	.	.	8	
27	$\nabla_3$	1	.	.	.	.	.	7	.	Done
Result		1	.	.	.	.	.	7	8	

Subsets

# Recap: Delta Debugging

Step	Test case									
1	$\Delta_1 = \nabla_2$	1	2	3	4	.	.	.	.	Testing $\Delta_1, \Delta_2$
2	$\Delta_2 = \nabla_1$	.	.	.	.	5	6	7	8	$\Rightarrow$ Increase granularity
3	$\Delta_1$	1	2	.	.	.	.	.	.	Testing $\Delta_1, \dots, \Delta_4$
4	$\Delta_2$	.	.	3	4	.	.	.	.	
5	$\Delta_3$	.	.	.	.	5	6	.	.	
6	$\Delta_4$	.	.	.	.	.	.	7	8	
7	$\nabla_1$	.	.	3	4	5	6	7	8	Testing complements
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9	$\Delta_1$	1	2	.	.	.	.	.	.	Testing $\Delta_1, \Delta_2, \Delta_3$
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11	$\Delta_3$	.	.	.	.	.	.	7	8	
12	$\nabla_1$	.	.	.	.	5	6	7	8	Testing complements
13	$\nabla_2$	1	2	.	.	.	.	7	8	$\Rightarrow$ Reduce to $c'_x = \nabla_2$ ; continue with $n = 2$
14	$\Delta_1 = \nabla_2$	1	2	.	.	.	.	.	.	Testing $\Delta_1, \Delta_2$
15	$\Delta_2 = \nabla_1$	.	.	.	.	.	.	7	8	$\Rightarrow$ Increase granularity
16	$\Delta_1$	1	.	.	.	.	.	.	.	Testing $\Delta_1, \dots, \Delta_4$
17	$\Delta_2$	.	2	.	.	.	.	.	.	
18	$\Delta_3$	.	.	.	.	.	.	7	.	
19	$\Delta_4$	.	.	.	.	.	.	.	8	
20	$\nabla_1$	.	2	.	.	.	.	7	8	Testing complements
21	$\nabla_2$	1	.	.	.	.	.	7	8	$\Rightarrow$ Reduce to $c'_x = \nabla_2$ ; continue with $n = 3$
22	$\Delta_1$	1	.	.	.	.	.	.	.	Testing $\Delta_1, \dots, \Delta_3$
23	$\Delta_2$	.	.	.	.	.	.	7	.	
24	$\Delta_3$	.	.	.	.	.	.	.	8	
25	$\nabla_1$	.	.	.	.	.	.	7	8	Testing complements
26	$\nabla_2$	1	.	.	.	.	.	.	8	
27	$\nabla_3$	1	.	.	.	.	.	7	.	Done
Result		1	.	.	.	.	.	7	8	

Granularity

# Recap: Delta Debugging

Step	Test case								
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2	$\Delta_2 = \nabla_1$	.	.	.	.	5	6	7	8
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4	$\Delta_2$	.	.	3	4	.	.	.	.
5	$\Delta_3$	.	.	.	.	5	6	.	.
6	$\Delta_4$	.	.	.	.	.	.	7	8
7	$\nabla_1$	.	.	3	4	5	6	7	8
8	$\nabla_2$	1	2	.	.	5	6	7	8
9	$\Delta_1$	1	2	.	.	.	.	.	.
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12	$\nabla_1$	.	.	.	.	5	6	7	8
13	$\nabla_2$	1	2	.	.	.	.	7	8
14	$\Delta_1 = \nabla_2$	1	2	.	.	.	.	.	.
15	$\Delta_2 = \nabla_1$	.	.	.	.	.	.	7	8
16	$\Delta_1$	1	.	.	.	.	.	.	.
17	$\Delta_2$	.	2	.	.	.	.	.	.
18	$\Delta_3$	.	.	.	.	.	.	7	.
19	$\Delta_4$	.	.	.	.	.	.	.	8
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Result		1	.	.	.	.	.	7	8

Complements

Testing  $\Delta_1, \Delta_2$

$\Rightarrow$  Increase granularity

Testing  $\Delta_1, \dots, \Delta_4$

Testing complements

$\Rightarrow$  Reduce to  $c'_x = \nabla_2$ ; continue with  $n = 3$

Testing  $\Delta_1, \Delta_2, \Delta_3$

\* same *test* carried out in an earlier step

Testing complements

$\Rightarrow$  Reduce to  $c'_x = \nabla_2$ ; continue with  $n = 2$

Testing  $\Delta_1, \Delta_2$

$\Rightarrow$  Increase granularity

Testing  $\Delta_1, \dots, \Delta_4$

Testing complements

$\Rightarrow$  Reduce to  $c'_x = \nabla_2$ ; continue with  $n = 3$

Testing  $\Delta_1, \dots, \Delta_3$

Testing complements

Done

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Result		1	.	.	.	.	.	7	8	

Reduce

# Recap: Delta Debugging

Step	Test case		
1	$\Delta_1 = \nabla_2$	1	2 3 4 . . . .
2	$\Delta_2 = \nabla_1$	.	. . . . 5 6 7 8
3	$\Delta_1$	1	2 . . . . .
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Testing  $\Delta_1, \Delta_2$

$\Rightarrow$  Increase granularity

Testing  $\Delta_1, \dots, \Delta_4$

Testing complements

$\Rightarrow$  Reduce to  $c'_x = \nabla_2$ ; continue with  $n = 3$

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Testing complements

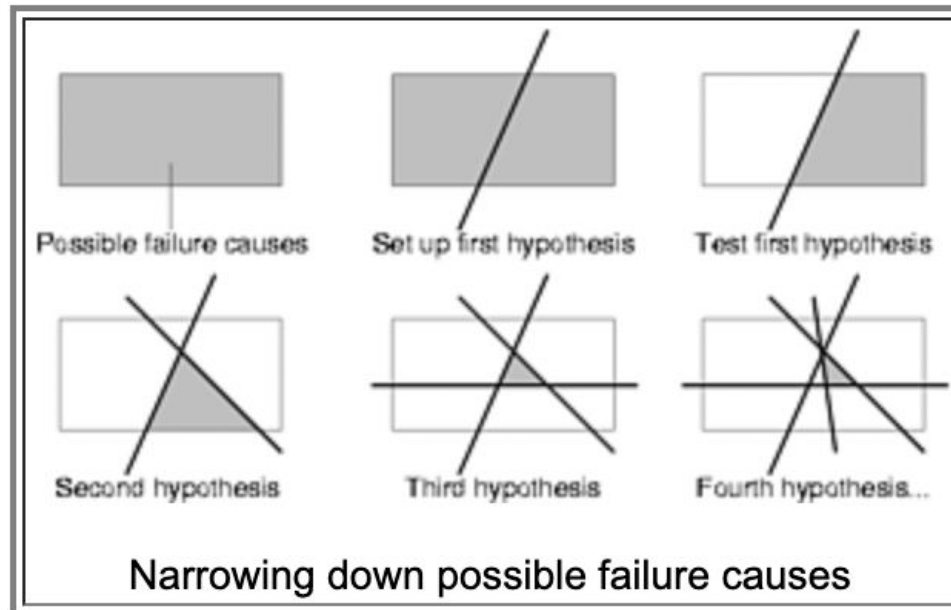
Done





# Delta debugging: discussion

- Applicability: Is this useful (as a concept and/or automated tool)?
- Optimality: minimal vs. minimum test case.
- Complexity: Best-case vs. worst-case.
- Assumptions: monotonicity and determinism.



# Reasoning about programs

# Reasoning about programs

## Use cases

- Verification/testing: ensure code is correct
- Prove facts to be true, e.g.:
  - x is never null
  - y is always greater than 0
  - input array a is sorted
- Debugging: understand why code is incorrect

# Reasoning about programs

## Use cases

- Verification/testing: ensure code is correct
- Prove facts to be true, e.g.:
  - x is never null
  - y is always greater than 0
  - input array a is sorted
- Debugging: understand why code is incorrect

## Approaches

- Testing (403)
- (Delta) Debugging (403)
- Fault localization (403)
- Abstract interpretation (primer in 403, covered in 503)
- Theorem proving (primer in 403, covered in 507)
- ...

# Forward vs. backward reasoning

## Forward reasoning

- Knowing: **a fact that is true before execution.**
- Reasoning: **what must be true after execution.**
- Given a precondition, what postcondition(s) are true?



# Forward vs. backward reasoning

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- Knowing: **a fact that is true before execution.**
- Reasoning: **what must be true after execution.**
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## Backward reasoning

- Knowing: **a fact that is true after execution.**
- Reasoning: **what must have been true before execution.**
- Given a postcondition, what precondition(s) must hold?

**What are the pros and cons for each approach?**

# Forward vs. backward reasoning

## **Forward reasoning**

- More intuitive for most people
- Helps understand what will happen (simulates the code)
- Introduces facts that may be irrelevant to the goal
- Set of current facts may get large
- Takes longer to realize that the task is hopeless

## **Backward reasoning**

- Usually more helpful
- Helps understand what should happen
- Given a specific goal, indicates how to achieve it
- Given an error, gives a test case that exposes it

# **Pre/Post-conditions and Invariants**



# Terminology

## **Pre-condition** (to a function)

- A condition that must be true when entering (the function)
- May include expectations about the arguments

## **Post-condition** (to a function)

- A condition that must be true when leaving (the function)

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## **Loop invariant**

- A condition that must be true for every loop iteration
- Must be true at the beginning and end of the loop body

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## **Loop invariant**

- A condition that must be true for every loop iteration
- Must be true at the beginning and end of the loop body

Pre-conditions define execution validity. Post-conditions and loop invariants define expected properties of a correct implementation, given a valid execution.

# Pre-conditions and post-conditions



```
1 double avgAbs(double[] nums) {  
2   int n = nums.length;  
3   double sum = 0;  
4  
5   int i = 0;  
6   while (i != n) {  
7     if(nums[i]>0) {  
8       sum = sum + nums[i];  
9     } else {  
10      sum = sum - nums[i];  
11    }  
12    i = i + 1;  
13  }  
14  
15  return sum / n;  
16 }
```

Entry point

Exit point

What are pre-conditions  
and post-conditions of  
this method (at the entry  
and exit points)?

# Pre-conditions and post-conditions

```
1 double avgAbs(double[] nums) {
2   int n = nums.length;
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5   int i = 0;
6   while (i != n) {
7     if(nums[i]>0) {
8       sum = sum + nums[i];
9     } else {
10      sum = sum - nums[i];
11    }
12    i = i + 1;
13  }
14
15  return sum / n;
16 }
```

## Pre-conditions

- `nums` is not null
- `nums.length > 0`

## Post-conditions

- `nums` has not changed
- `n > 0`
- `sum >= 0`
- `return value >= 0`
- ...

# (Loop) invariants



```
1 double avgAbs(double[] nums) {
2   int n = nums.length;
3   double sum = 0;
4
5   int i = 0;
6   while (i != n) {
7     if(nums[i]>0) {
8       sum = sum + nums[i];
9     } else {
10      sum = sum - nums[i];
11    }
12    i = i + 1;
13  }
14
15  return sum / n;
16 }
```

Does this loop terminate?  
What are pre-conditions,  
post-conditions,  
and loop invariants?

# Summary

## **Pre-condition** (to a function)

- A condition that must be true when entering (the function)
- May include expectations about the arguments

## **Post-condition** (to a function)

- A condition that must be true when leaving (the function)

## **Loop invariant**

- A condition that must be true for every loop iteration
- Must be true at the beginning and end of the loop body

**How are these related to software testing and debugging?**

# **Dynamic vs. static analysis**



# Dynamic vs. static analysis: overview

## **Dynamic analysis**

- Reason about the program based on some program executions.
- Observe concrete behavior at run time.
- Improve confidence in correctness.

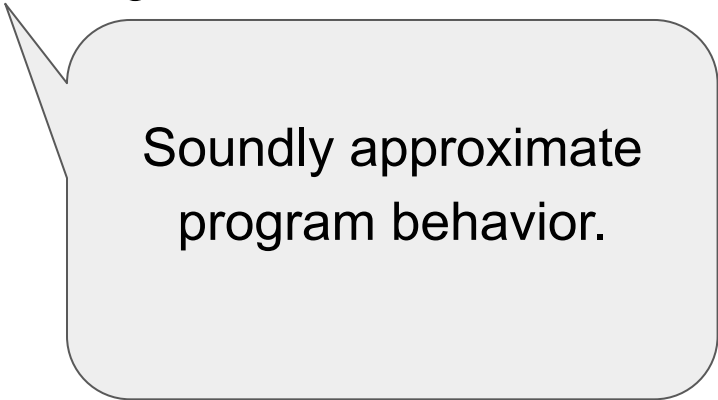
# Dynamic vs. static analysis: overview

## Dynamic analysis

- Reason about the program based on some program executions.
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## Static analysis

- Reason about the program without executing it.
- Build an abstraction of run-time states.
- Reason over abstract domain.
- Prove a property of the program.



Soundly approximate  
program behavior.

# Dynamic vs. static analysis: overview

## Dynamic analysis

- Reason about the program based on some program executions.
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- Reason about the program without executing it.
- Build an abstraction of run-time states.
- Reason over abstract domain.
- Prove a property of the program.

*[y:=2, x:=2]*

**y = x++**

*[y:=2, x:=3]*

# Dynamic vs. static analysis: overview

## Dynamic analysis

- Reason about the program based on some program executions.
- Observe concrete behavior at run time.
- Improve confidence in correctness.

## Static analysis

- Reason about the program without executing it.
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- Reason over abstract domain.
- Prove a property of the program.

*<y is even, x is even>*

**y = x++**

*<y is even, x is odd>*

# Dynamic vs. static analysis: overview

## Dynamic analysis

- Reason about the program based on some program executions.
- Observe concrete behavior at run time.
- Improve confidence in correctness.

## Static analysis

- Reason about the program without executing it.
- Build an abstraction of run-time states.
- Reason over abstract domain.
- Prove a property of the program.

The statement “**f returns a non-negative value**” is weaker (but easier to establish) than the statement “**f returns the absolute value of its argument**”.

# Dynamic analysis: examples

## Software testing

```
double avg(double[] nums) {  
    int n = nums.length;  
    double sum = 0;  
  
    int i = 0;  
    while (i < n)  
        sum = sum + nums[i];  
        i = i + 1;  
  
    double avg = sum / n;  
  
    return avg;  
}
```

## A test for the avg function:

```
@Test  
public void testAvg() {  
    double nums =  
        new double[]{1.0, 2.0, 3.0};  
    double actual = Math.avg(nums);  
    double expected = 2.0;  
    assertEquals(expected, actual, EPS);  
}
```

# Static analysis: examples

```
static OSStatus
SSLVerifySignedServerKeyExchange(...) {
    OSStatus err;
    ...
    if ((err = SSLHashSHA1.update(&hashCtx, &clientRandom)) != 0)
        goto fail;
    if ((err = SSLHashSHA1.update(&hashCtx, &serverRandom)) != 0)
        goto fail;
    if ((err = SSLHashSHA1.update(&hashCtx, &signedParams)) != 0)
        goto fail;
        goto fail;
    if ((err = SSLHashSHA1.final(&hashCtx, &hashOut)) != 0)
        goto fail;
    err = sslRawVerify(ctx, ctx->peerPubKey, dataToSign, dataToSignLen, signature, signatureLen);
    if(err) {
        sslErrorLog("SSLDecodeSignedServerKeyExchange: sslRawVerify returned %d\n", (int)err);
        goto fail;
    }
    fail:
        SSLFreeBuffer(&signedHashes);
        SSLFreeBuffer(&hashCtx);
        return err;
}
```

Anything wrong with  
this code?

# Static analysis: examples

```
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    OSStatus err;
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    if ((err = SSLHashSHA1.update(&hashCtx, &clientRandom)) != 0)
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    }
    fail:
        SSLFreeBuffer(&signedHashes);
        SSLFreeBuffer(&hashCtx);
        return err;
}
```

Apple's "goto fail" bug:  
a security vulnerability  
for 2 years!



# Static analysis: examples

Rule/pattern-based analysis (PMD, Findbugs, Error Prone, etc.)

```
double avg(double[] nums) {  
    int n = nums.length;  
    double sum = 0;  
  
    int i = 0;  
    while (i < n)  
        sum = sum + nums[i];  
        i = i + 1;  
  
    double avg = sum / n;  
  
    return avg;  
}
```

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        i = i + 1;  
    }  
    double avg = sum / n;  
  
    return avg;  
}
```

# Static analysis: examples

## Compiler: type checking

```
double avg(double[] nums) {  
    int n = nums.length;  
    double sum = 0;  
  
    int i = 0.0;  
    while (i < n) {  
        sum = sum + nums[i];  
        i = i + 1;  
    }  
    double avg = sum / n;  
  
    return avg;  
}
```

```
double avg(double[] nums) {  
    int n = nums.length;  
    double sum = 0;  
  
    int i = 0;  
    while (i < n) {  
        sum = sum + nums[i];  
        i = i + 1;  
    }  
    double avg = sum / n;  
  
    return avg;  
}
```

# Dynamic vs. static analysis: summary

## **Dynamic analysis**

- Concrete domain
- Does not generalize
- Slow if exhaustive

## **Static analysis**

- Abstract domain
- Sound but imprecise
- Slow if precise