## **CSE 403**

Software Engineering

Advanced program analysis

# A primer on solver-aided reasoning and verification



## What is a SAT solver?

#### What is a SAT solver?

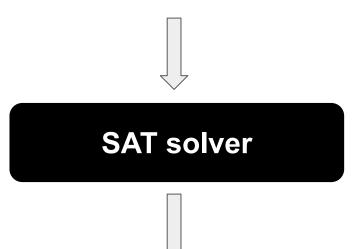
• Takes a formula (propositional logic) as input.

$$(X1 \ V \ X2) \ \land \ (\neg X1 \ V \ X3) \ \land \ (X1 \ V \ \neg X3) \ \land \ (\neg X2 \ V \ \neg X3)$$

#### What is a SAT solver?

- Takes a formula (propositional logic) as input.
- Returns a model (an assignment that satisfies the formula).

$$(X1 \ V \ X2) \ \land \ (\neg X1 \ V \ X3) \ \land \ (X1 \ V \ \neg X3) \ \land \ (\neg X2 \ V \ \neg X3)$$



$$X = \{X1, X2, X3\} = \{T, F, T\}$$

- An SMT (Satisfiability Modulo Theories) solver.
  - Supports formulas for more complex data types
  - Theories for Integers, Strings, Arrays, etc.

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  - Supports formulas for more complex data types
  - Theories for Integers, Strings, Arrays, etc.
  - Examples for Integers:
    - a \* 1 = a (identity element)
    - $\blacksquare$  a + 0 = a (identity element)

- An SMT (Satisfiability Modulo Theories) solver.
- Uses a standard language (SMT-LIB).
  - Print to the screen.
  - Declare variables and functions.

```
(echo "Running Z3...")
(declare-const a Int)
```

- An SMT (Satisfiability Modulo Theories) solver.
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  - Define constraints.

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```

- An SMT (Satisfiability Modulo Theories) solver.
- Uses a standard language (SMT-LIB).
  - Print to the screen.
  - Declare variables and functions.
  - Define constraints.
  - Check satisfiability and obtain a model.
  - 0 ...

```
(echo "Running Z3...")
(declare-const a Int)
(assert (> a 0))
(check-sat)
(get-model)
```

Which question does this code answer?

## A first example

```
1 int simpleMath(int a, int b) {
2   assert(b>0);
3   if(a + b == a * b) {
4     return 1;
5   }
6   return 0;
7 }
```

## A first example

```
int simpleMath(int a, int b) {
   assert(b>0);
   if(a + b == a * b) {
     return 1;
   }
   return 0;
}
```

```
(declare-const a Int)
  (declare-const b Int)
  (assert (> b 0))
  (assert (= (+ a b) (* a b)))
  (check-sat)
  (get-model)
```

Does this method ever return 1? Let's ask Z3...

### A more complex example

```
int getNumber(int a, int b, int c) {
  if (c==0) return 0;
  if (c==4) return 0;
  if (a + b < c) return 1;
  if (a + b > c) return 2;
  if (a * b == c) return 3;
  return 4;
}
```



Does this method ever return 3? What constraints must be satisfied?

```
1 int add1(int a, int b) {
2   return a + b;
3 }
4 
5 int add2(int a, int b) {
6   return a * b;
7 }
```

Are these two methods semantically equivalent?

```
1 int add1(int a, int b) {
2   return a + b;
3 }
4 
5 int add2(int a, int b) {
6   return a * b;
7 }
```

```
(declare-const a Int)
(declare-const b Int)
(declare-const add1 Int)
(declare-const add2 Int)
(assert (= add1 (+ a b)))
(assert (= add2 (* a b)))
(assert (= add1 add2))
(check-sat)
(get-model)
```

Are these two methods semantically equivalent?

```
1 int add1(int a, int b) {
2   return a + b;
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5 int add2(int a, int b) {
6   return a * b;
7 }
```

```
(declare-const a Int)
(declare-const b Int)

(declare-const add1 Int)
(declare-const add2 Int)

(assert (= add1 (+ a b)))
(assert (= add2 (* a b)))
(assert (= add1 add2))
(check-sat)
(get-model)
```

Yes, for a=2 and b=2. What have we actually proven here?

```
1 int add1(int a, int b) {
2   return a + b;
3 }
4 
5 int add2(int a, int b) {
6   return a * b;
7 }
```

```
(declare-const a Int)
(declare-const b Int)
(declare-const add1 Int)
(declare-const add2 Int)
(assert (= add1 (+ a b)))
(assert (= add2 (* a b)))
(assert (not (= add1 add2)))
(check-sat)
(get-model)
```

For **universal claims**, our goal is to **prove** the absence of counter examples (i.e., the defined constraints are **unsat**)!

## Summary

- Solver-aided reasoning is used for testing and verification.
- SMT solvers:
  - Provide one solution, if one exists.
  - Are commonly used to find counter-examples (or prove unsat).
  - Support many theories that can model program semantics.
  - Usually support a standard language (SMT-lib).
- The challenge is to model a problem as a constraint system.

#### A few examples:

- Statistical test selection
- Data-structure synthesis
- Program synthesis
- Many higher-level DSLs and language bindings exist.