

# CSE P 504

Advanced topics in Software Systems  
Fall 2022

## Mutation-based Testing

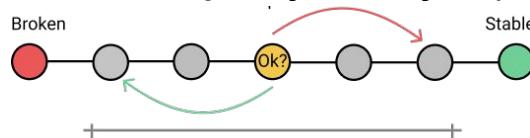
October 24, 2022

## Today

- Recap: Git bisect exercise
- Mutation-based testing
  - The basics
  - Productive mutants
  - Mutant subsumption
- Coverage-based vs. mutation-based testing
- In-class exercise 3

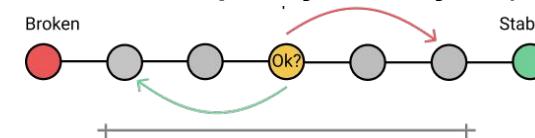
## Recap: Git bisect

- **Git bisect run-time complexity is always  $O(\log(n))$**

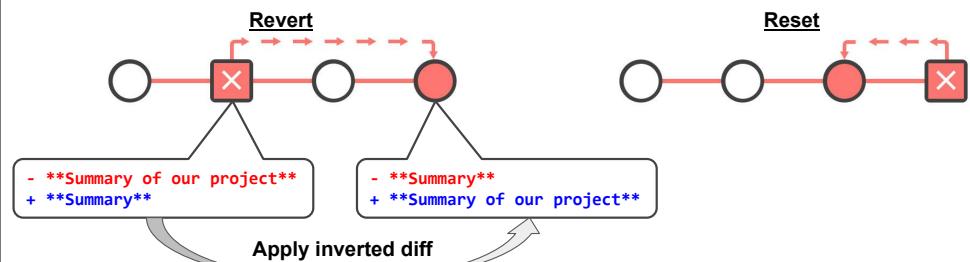


## Recap: Git bisect

- **Git bisect run-time complexity is always  $O(\log(n))$**

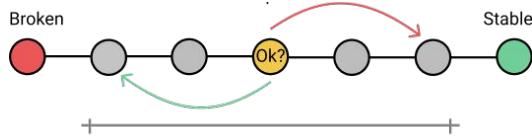


- **Git revert vs. git reset**



## Recap: Git bisect

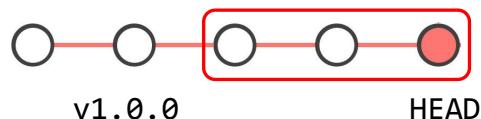
- Git bisect run-time complexity is always  $O(\log(n))$



- Git revert vs. git reset

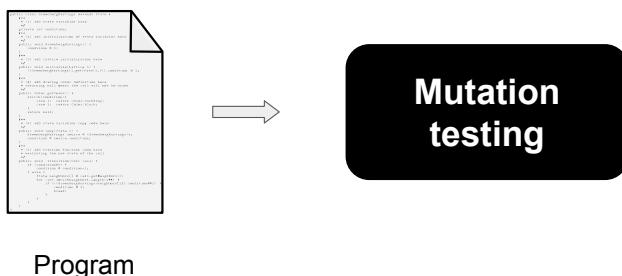


- git rev-list v1.0.0..HEAD (or HEAD ^v1.0.0)

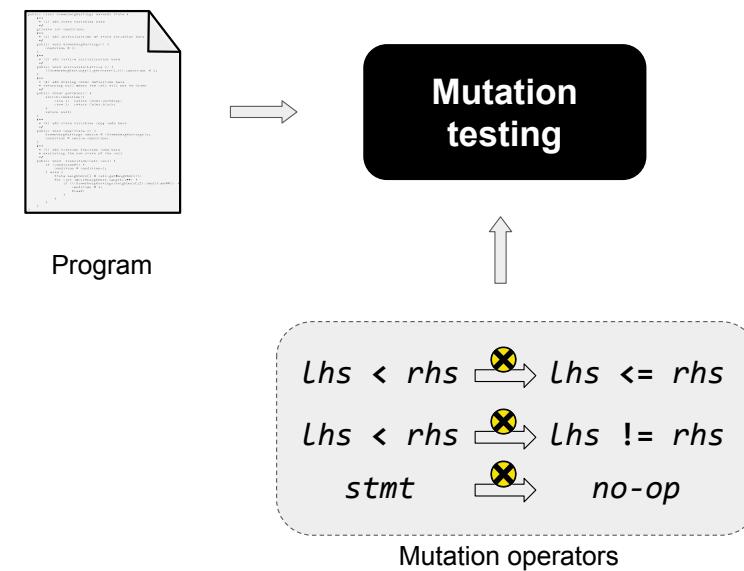


## Mutation-based testing: the basics

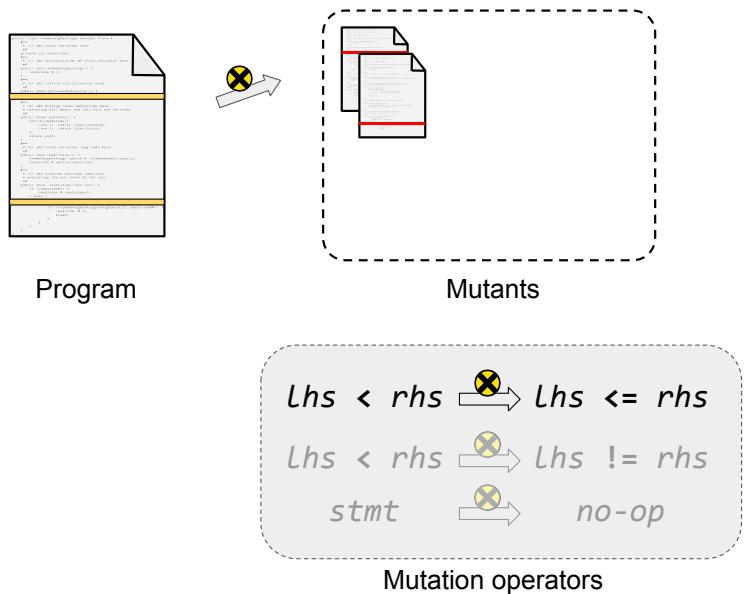
### Mutation testing



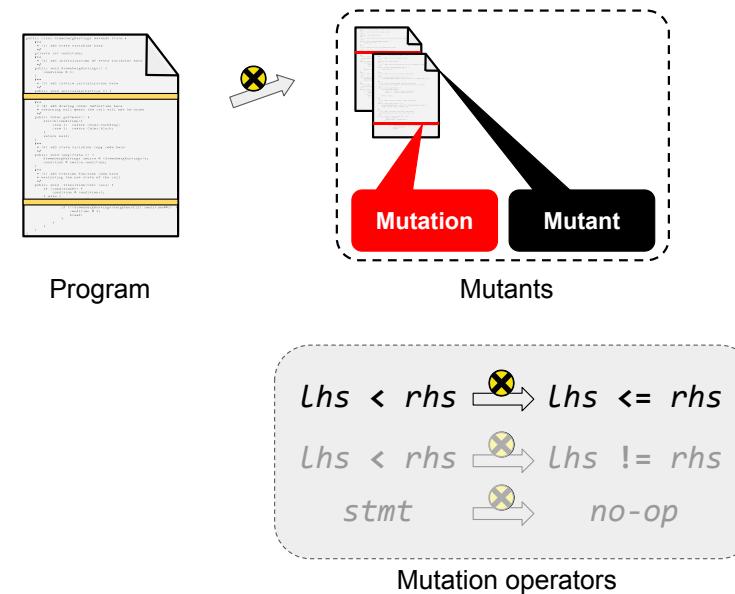
### Mutation testing: mutant generation



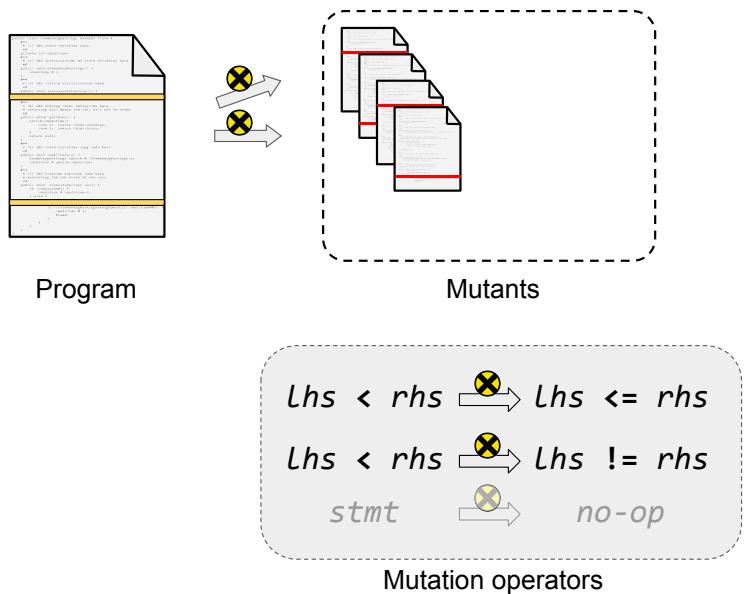
## Mutation testing: mutant generation



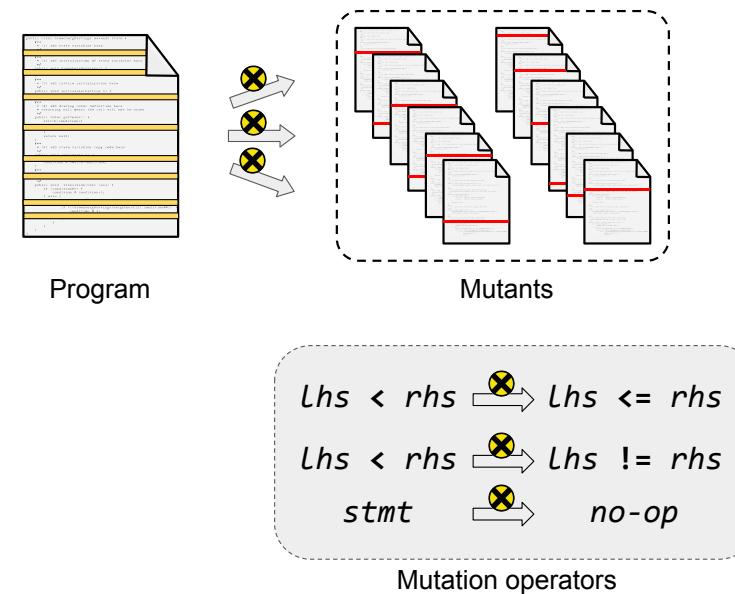
## Mutation testing: mutant generation



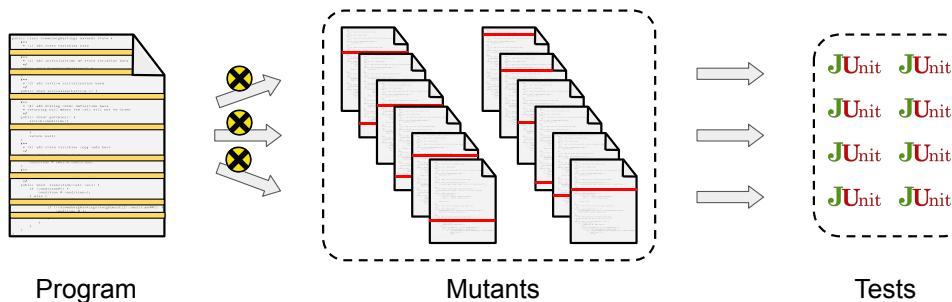
## Mutation testing: mutant generation



## Mutation testing: mutant generation



## Mutation testing: test creation



### Assumptions

- Mutants are coupled to real faults
- Mutant detection is correlated with real-fault detection

[https://homes.cs.washington.edu/~rjust/publ/mutants\\_real\\_faults\\_fse\\_2014.pdf](https://homes.cs.washington.edu/~rjust/publ/mutants_real_faults_fse_2014.pdf)  
[https://homes.cs.washington.edu/~rjust/publ/mutation\\_testing\\_practices\\_icse\\_2021.pdf](https://homes.cs.washington.edu/~rjust/publ/mutation_testing_practices_icse_2021.pdf)

## Mutation testing: a concrete example

### Original program:

```
public int min(int a, int b) {  
    return a < b ? a : b;  
}
```

### Mutant 1:

```
public int min(int a, int b) {  
    return a;  
}
```

## Mutation testing: another example

### Original program:

```
public int min(int a, int b) {  
    return a < b ? a : b;  
}
```

### Mutant 2:

```
public int min(int a, int b) {  
    return b;  
}
```

## Mutation testing: yet another example

### Original program:

```
public int min(int a, int b) {  
    return a < b ? a : b;  
}
```

### Mutant 3:

```
public int min(int a, int b) {  
    return a >= b ? a : b;  
}
```

## Mutation testing: last example (I promise)

### Original program:

```
public int min(int a, int b) {  
    return a < b ? a : b;  
}
```

### Mutant 4:

```
public int min(int a, int b) {  
    return a <= b ? a : b;  
}
```



## Mutation testing: exercise

### Original program:

```
public int min(int a, int b) {  
    return a < b ? a : b;  
}
```

### Mutants:

M1: return a;  
M2: return b;  
M3: return a >= b ? a : b;  
M4: return a <= b ? a : b;

**For each mutant, provide a test case that detects it  
(i.e., passes on the original program but fails on the mutant)**

## Mutation testing: exercise

### Original program:

```
public int min(int a, int b) {  
    return a < b ? a : b;  
}  
  
Mutants:  
M1: return a;  
M2: return b;  
M3: return a >= b ? a : b;  
M4: return a <= b ? a : b;
```

**M4 cannot be detected (equivalent mutant).**

a	b	Original	M1	M2	M3	M4
1	2	1	1	2	2	1
1	1	1	1	1	1	1
2	1	1	2	1	2	1

## Mutation testing: exercise

### Original program:

```
public int min(int a, int b) {  
    return a < b ? a : b;  
}  
  
Mutants:  
M1: return a;  
M2: return b;  
M3: return a >= b ? a : b;  
M4: return a <= b ? a : b;
```

**Which mutant(s) should we show to a developer?**

a	b	Original	M1	M2	M3	M4
1	2	1	1	2	2	1
1	1	1	1	1	1	1
2	1	1	2	1	2	1

## Mutation testing: summary

### Original program:

```
public int min(int a, int b) {
    return a < b ? a : b;
}
```

### Mutants:

```
M1: return a;
M2: return b;
M3: return a >= b ? a : b;
M4: return a <= b ? a : b;
```

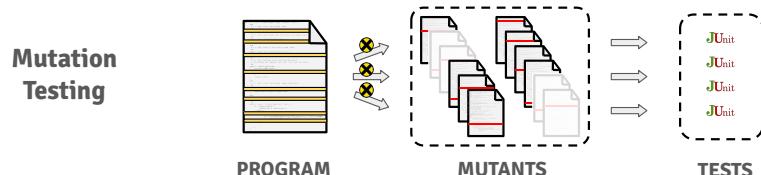
a	b	Original	Redundant		Equivalent	
			M1	M2	M3	M4
1	2	1	1	2	2	1
1	1	1	1	1	1	1
2	1	1	2	1	2	1

## Mutation testing: challenges

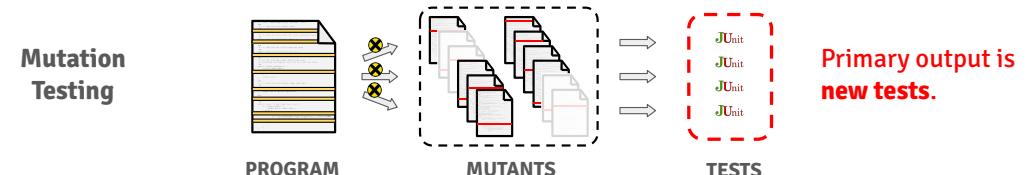
- Redundant mutants
  - Inflate the mutant detection ratio
  - Hard to assess progress and remaining effort
- Equivalent mutants
  - Max mutant detection ratio != 100%
  - Waste resources (CPU and human time)

a	b	Original	M1	M2	M3	M4
1	2	1	1	2	2	1
1	1	1	1	1	1	1
2	1	1	2	1	2	1

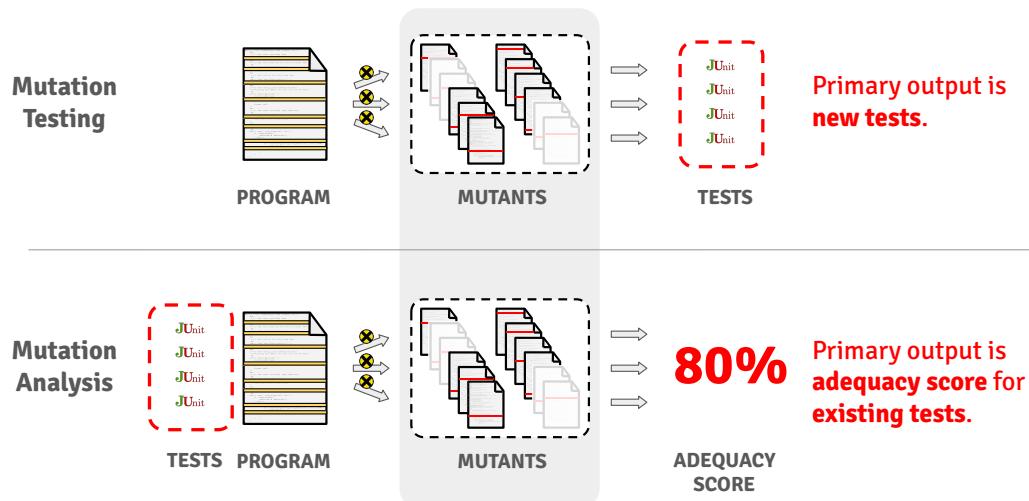
## Mutation Testing vs. Mutation Analysis



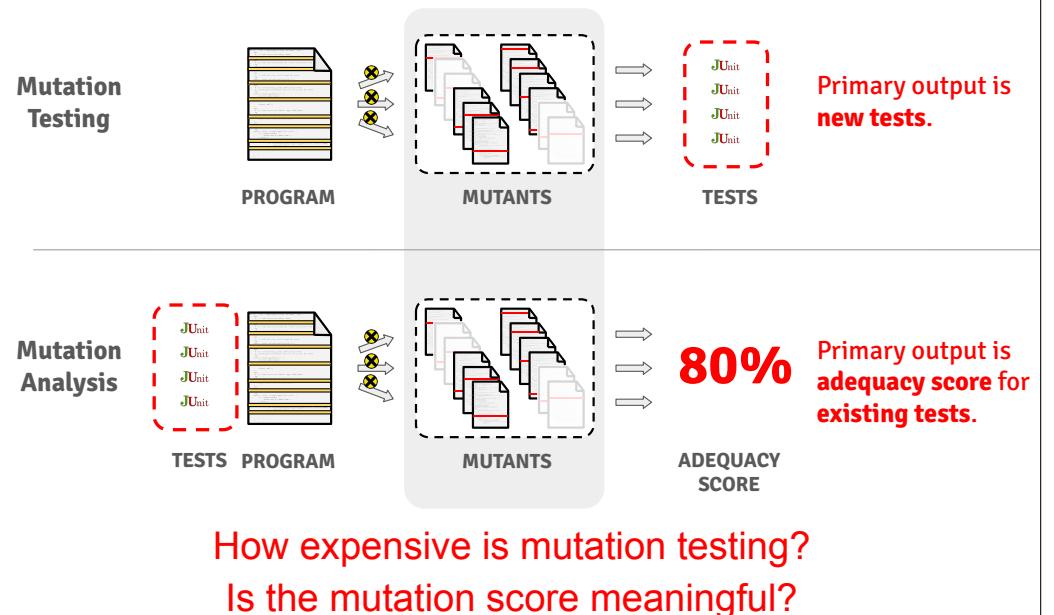
## Mutation Testing vs. Mutation Analysis



## Mutation Testing vs. Mutation Analysis



## Mutation Testing vs. Mutation Analysis



## Mutation-based testing: productive mutants

### Detectable vs. productive mutants

#### Historically

- Detectable mutants are good → tests
- Equivalent mutants are bad → no tests

#### A more nuanced view

- Detectable vs. equivalent is too simplistic
- **Productive mutants** elicit effective tests, but
  - detectable mutants can be useless, and
  - equivalent mutants can be useful!

The core question here concerns test-goal utility  
(applies to any adequacy criterion).

## Detectable vs. productive mutants

### Historically

- Detectable mutants are **good** → tests
- Equivalent mutants are **bad** → no tests

### A more nuanced view

- Detectable vs. equivalent is **too simplistic**
- Productive mutants elicit effective tests, but
  - detectable mutants can be useless, and
  - equivalent mutants can be useful!

The notion of productive mutants is fuzzy!

A mutant is **productive** if it is

1. **detectable** and **elicits an effective test** or
2. **equivalent** and **advances code quality or knowledge**

An Industrial Application of Mutation Testing: Lessons, Challenges, and Research Directions ([Reading 1](#))

## Productive mutants: mutation testing at Google

```
int RunMe(int a, int b) {  
    if (a == b || b == 1) {  
  
        ▼ Mutants  Changing this 1 line to  
        14:25, 28 Mar  
        if (a != b || b == 1) {  
  
            does not cause any test exercising them to fail.  
            Consider adding test cases that fail when the code is mutated to  
            ensure those bugs would be caught.  
  
            Mutants ran because goranpetrovic is whitelisted  
  
    }  
}
```

[Please fix](#)      [Not useful](#)

## Productive mutants: mutation testing at Google

```
int RunMe(int a, int b) {  
    if (a == b || b == 1) {  
  
        ▼ Mutants  Changing this 1 line to  
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            Consider adding test cases that fail when the code is mutated to  
            ensure those bugs would be caught.  
  
            Mutants ran because goranpetrovic is whitelisted  
  
    }  
}
```

[Please fix](#)

[Not useful](#)

Practical Mutation Testing at Scale: A view from Google ([Reading 3](#))

## Detectable vs. productive mutants (1)

### Original program

```
public double getAvg(double[] nums) {  
    double sum = 0;  
    int len = nums.length;  
  
    for (int i = 0; i < len; ++i) {  
        sum = sum + nums[i];  
    }  
  
    return sum / len;  
}
```

### Mutant

```
public double getAvg(double[] nums) {  
    double sum = 0;  
    int len = nums.length;  
  
    for (int i = 0; i < len; ++i) {  
        sum = sum * nums[i];  
    }  
  
    return sum / len;  
}
```

Is the mutant is **detectable**?

## Detectable vs. productive mutants (1)

### Original program

```
public double getAvg(double[] nums) {  
    double sum = 0;  
    int len = nums.length;  
  
    for (int i = 0; i < len; ++i) {  
        sum = sum + nums[i];  
    }  
  
    return sum / len;  
}
```

### Mutant

```
public double getAvg(double[] nums) {  
    double sum = 0;  
    int len = nums.length;  
  
    for (int i = 0; i < len; ++i) {  
        sum = sum * nums[i];  
    }  
  
    return sum / len;  
}
```

The mutant is **detectable**, but is it **productive**?

## Detectable vs. productive mutants (1)

### Original program

```
public double getAvg(double[] nums) {  
    double sum = 0;  
    int len = nums.length;  
  
    for (int i = 0; i < len; ++i) {  
        sum = sum + nums[i];  
    }  
  
    return sum / len;  
}
```

### Mutant

```
public double getAvg(double[] nums) {  
    double sum = 0;  
    int len = nums.length;  
  
    for (int i = 0; i < len; ++i) {  
        sum = sum * nums[i];  
    }  
  
    return sum / len;  
}
```

The mutant is **detectable**, but is it **productive**? Yes!

## Detectable vs. productive mutants (2)

### Original program

```
public double getAvg(double[] nums) {  
    int len = nums.length;  
    double sum = 0;  
    double avg = 0;  
  
    for (int i = 0; i < len; ++i) {  
        avg = avg + (nums[i] / len);  
        sum = sum + nums[i];  
    }  
  
    return sum / len;  
}
```

### Mutant

```
public double getAvg(double[] nums) {  
    int len = nums.length;  
    double sum = 0;  
    double avg = 0;  
  
    for (int i = 0; i < len; ++i) {  
        avg = avg * (nums[i] / len);  
        sum = sum + nums[i];  
    }  
  
    return sum / len;  
}
```

Is the mutant **detectable**?

## Detectable vs. productive mutants (2)

### Original program

```
public double getAvg(double[] nums) {  
    int len = nums.length;  
    double sum = 0;  
    double avg = 0;  
  
    for (int i = 0; i < len; ++i) {  
        avg = avg + (nums[i] / len);  
        sum = sum + nums[i];  
    }  
  
    return sum / len;  
}
```

### Mutant

```
public double getAvg(double[] nums) {  
    int len = nums.length;  
    double sum = 0;  
    double avg = 0;  
  
    for (int i = 0; i < len; ++i) {  
        avg = avg * (nums[i] / len);  
        sum = sum + nums[i];  
    }  
  
    return sum / len;  
}
```

The mutant is **not detectable**, but is it **unproductive**?

## Detectable vs. productive mutants (2)

### Original program

```
public double getAvg(double[] nums) {  
    int len = nums.length;  
    double sum = 0;  
    double avg = 0;  
  
    for (int i = 0; i < len; ++i) {  
        avg = avg + (nums[i] / len);  
        sum = sum + nums[i];  
    }  
  
    return sum / len;  
}
```

### Mutant

```
public double getAvg(double[] nums) {  
    int len = nums.length;  
    double sum = 0;  
    double avg = 0;  
  
    for (int i = 0; i < len; ++i) {  
        avg = avg * (nums[i] / len);  
        sum = sum + nums[i];  
    }  
  
    return sum / len;  
}
```

The mutant is **not detectable**, but is it unproductive? No!

## Detectable vs. productive mutants (3)

### Original program

```
...  
  
Set cache = new HashSet(a * b);  
  
...
```

### Mutant

```
...  
  
Set cache = new HashSet(a + b);  
  
...
```

Is the mutant **detectable**?

## Detectable vs. productive mutants (3)

### Original program

```
...  
  
Set cache = new HashSet(a * b);  
  
...
```

### Mutant

```
...  
  
Set cache = new HashSet(a + b);  
  
...
```

The mutant is **detectable**, but is it **productive**? No!

## Detectable vs. productive mutants (3)

### Original program

```
...  
  
Set cache = new HashSet(a * b);  
  
...
```

### Mutant

```
...  
  
Set cache = new HashSet(a + b);  
  
...
```

The mutant is **detectable**, but is it **productive**? No!

## Mutation-based testing: mutant subsumption

### Mutant subsumption

Mutant MutOp	Tests			
	$t_1$	$t_2$	$t_3$	$t_4$
$m_1: < \mapsto !=$	●	●	●	●
$m_2: < \mapsto ==$	●	●	●	●
$m_3: < \mapsto <=$	★	★	★	★
$m_4: < \mapsto >$	●	●	●	●
$m_5: < \mapsto >=$	●	●	●	●
$m_6: < \mapsto \text{true}$	★	★	★	★
$m_7: < \mapsto \text{false}$	●	●	●	●
$m_8: < \mapsto !=$	●	●	●	●
$m_9: < \mapsto ==$	●	●	●	●
$m_{10}: < \mapsto <=$	●	●	●	●
$m_{11}: < \mapsto >$	●	●	●	●
$m_{12}: < \mapsto >=$	●	●	●	●
$m_{13}: < \mapsto \text{true}$	●	●	●	●
$m_{14}: < \mapsto \text{false}$	●	●	●	●

Mutant detected (assertion)

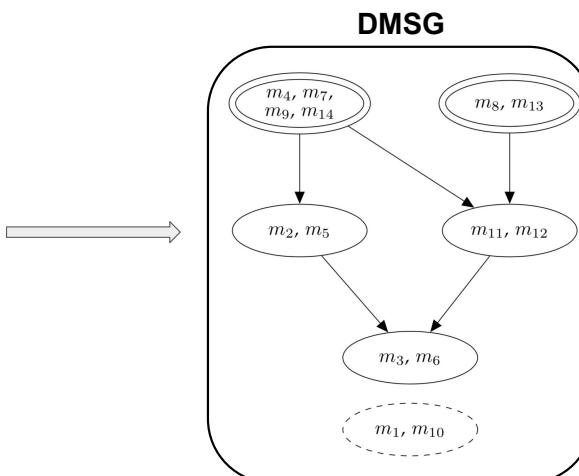
Mutant detected (exception)

Mutant not detected

Prioritizing Mutants to Guide Mutation Testing ([Reading 2](#))

## DMSG: Dynamic Mutant Subsumption Graph

Mutant MutOp	Tests			
	$t_1$	$t_2$	$t_3$	$t_4$
$m_1: < \mapsto !=$	●	●	●	●
$m_2: < \mapsto ==$	●	●	●	●
$m_3: < \mapsto <=$	★	★	★	★
$m_4: < \mapsto >$	●	●	●	●
$m_5: < \mapsto >=$	●	●	●	●
$m_6: < \mapsto \text{true}$	★	★	★	★
$m_7: < \mapsto \text{false}$	●	●	●	●
$m_8: < \mapsto !=$	●	●	●	●
$m_9: < \mapsto ==$	●	●	●	●
$m_{10}: < \mapsto <=$	●	●	●	●
$m_{11}: < \mapsto >$	●	●	●	●
$m_{12}: < \mapsto >=$	●	●	●	●
$m_{13}: < \mapsto \text{true}$	●	●	●	●
$m_{14}: < \mapsto \text{false}$	●	●	●	●



## Coverage-based vs. mutation-based testing

See dedicated [Slides \(4 pages\)](#).

Prioritizing Mutants to Guide Mutation Testing ([Reading 2](#))