# **CSE P 590**

# **Building Data Analysis Pipelines**

Fall 2024



Statistical modeling

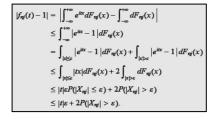


# **Today**

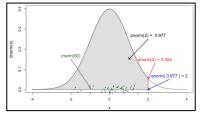
- Uniform vs. stratified sampling
- Statistical vs. practical significance
- Parametric vs non-parametric statistics
- CLT: Central Limit Theorem

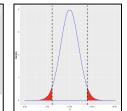
# 3 ways to understand and apply statistics

#### Math/Proofs



#### **Simulations/Visualizations**





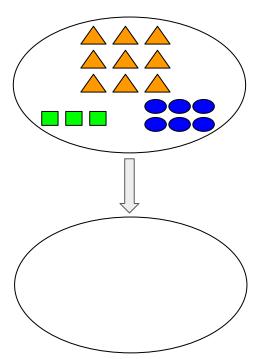
#### **Decision diagrams**



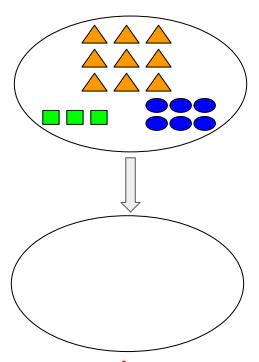
Uniform random vs. stratified random

# Sampling: uniform random vs. stratified random

#### **Uniform random**



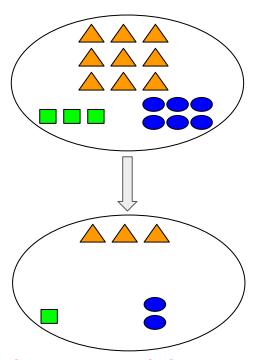
#### **Stratified random**



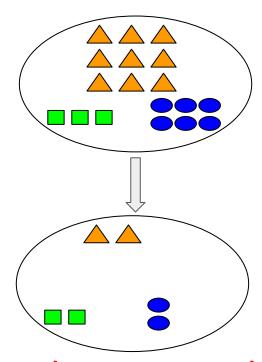
Sample six items: what are the expected outcomes?

# Sampling: uniform random vs. stratified random

### **Uniform random**



#### **Stratified random**



When would you use which sampling approach?

Statistical vs. practical significance

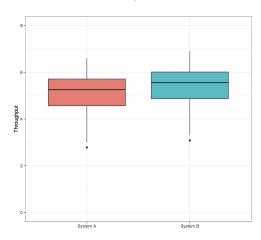
# Hypothetical study on system performance

- Compare normalized throughput of two systems.
- Statistical test for the difference in mean throughput.

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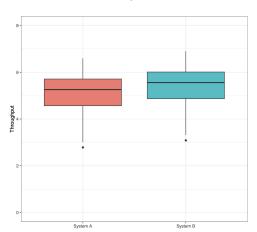
**Scenario 1**: p = 0.2137



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**Scenario 1**: p = 0.2137

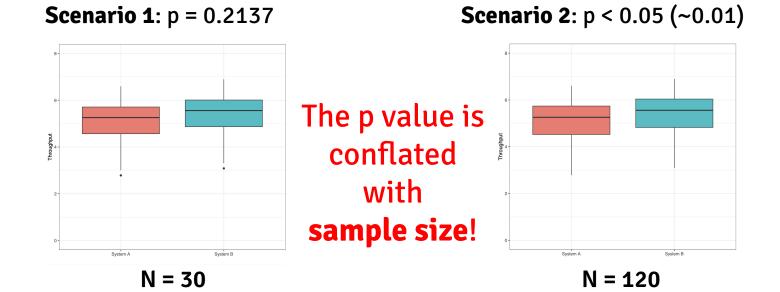


**Scenario 2**: p < 0.05 (~0.01)

What plot do you expect for Scenario 2?

### Hypothetical study on system performance

- Compare normalized throughput of two systems.
- Statistical test for the difference in mean throughput.



# A little quiz



- 1. What is the difference between statistical and practical significance?
- 2. What is the interpretation of the p value?
- 3. What is an effect size?

#### Small-group brainstorming

- Explain the answer to a group member.
- Come up with open questions.

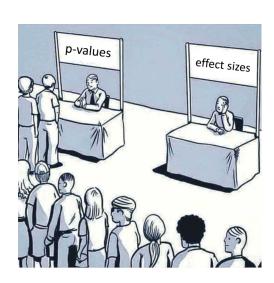
# Statistical vs. practical significance

## **Statistical significance**

- Is the difference due to chance?
- p value

## **Practical significance**

- Does the difference matter in practice?
- Effect size



# Effect size measures: examples

#### **Correlation coefficients**

- Pearson's r
- Kendall's tau (rank based)
- Spearman's rho (rank based)

# "Raw" differences in central tendency

- Difference in means
- Difference in medians

# Effect size measures: distinction

#### **Distinction**

- Parametric vs. non-parametric
  - Parametric: Pearson's r, Cohen's d
  - Non-parametric: Spearman's rho, A<sub>12</sub>
- Standardized vs. non-standardized
  - Non-standardized: Difference in means  $\Delta_{M}$
  - $\circ$  Standardized:  $\Delta_{M}$  divided by the (pooled) standard deviation
- Variable types
  - Continuous: Cohen's d, A<sub>12</sub>
  - Ordinal: A<sub>12</sub>. Cliff's delta, Somers' D
  - Dichotomous: Odds ratio

# Interpreting effect sizes

# **Example (Cohen's d):**

- < 0.2: negligible
- >= 0.2: small
- >= 0.5: medium
- >= 0.8: large

# Interpreting effect sizes: it's your job!

# **Example (Cohen's d):**

- < 0.2: negligible
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# (Standardized) effect sizes are a good starting point, but:

- Is an effect practically significant? Depends on context and domain!
- Raw differences may be easier to interpret (in context).

Generic effect sizes don't provide specific answers!

# Contextualizing effect sizes

# A statistically significant (large) effect may not be practically relevant:

- System response time: 20ms vs. 10ms
- Analysis runtime: 8h vs. 6h
- Top-5 vs. top-10 ranking
- Magnitude vs. location shift (superiority)

# Parametric vs. non-parametric statistics

# Parametric vs. non-parametric statistics

#### **Parametric statistics**

- Assumptions about the underlying distribution.
  - **Examples for common assumptions:** 
    - Normal distribution.
    - Equal variance.
- Parametric because of the reliance on distribution parameters.
- Example: Student's t-test, Welch's t-test.

#### Non-parametric statistics

- Fewer assumptions about the underlying distribution.
- Rank-based -> more robust to outliers.
- Example: Mann Whitney u test (Wilcoxon rank sum test).

### Two common statistical tests

# Student's/Welch's t test

- Assumes normality
- Hypothesis is related to equality of mean(s).

#### Mann Whitney u test

- Agnostic to the underlying distribution
- Hypothesis is related to location shift.

# A little quiz



- 1. Why not always use non-parametric statistics (fewer assumptions)?
- 2. Is the following statement true? "If a parametric test is not significant, then a non-parametric test cannot be significant either due to less statistical power."
- 3. What conclusions can you draw from the Cohen's d vs.  $A_{12}$  effect sizes?

# My new awesome system

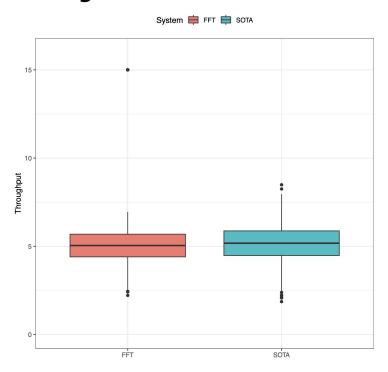
#### **Evaluate system performance**

- System: A new system (A) for fast file transfers: FFT.
- Goal: Compare the throughput against the state of the art (B): SOTA.

#### **Results:**

- Conclusion: FFT significantly outperforms SOTA:
   On average, its throughput of 5.29 files/ms -- a 2.3% increase over SOTA (5.17 files/ms).
- **Statistical significance:** The Mann Whitney U test showed that the difference is significant at the 0.05 significance level (p=0.0071).
- Practical significance: While a relative increase of 2.3% may seem modest, we argue that this is a big achievement, given how optimized the state of the art is.

# My new awesome system



Does this change your perception of the results? What went wrong?

# Statistical analysis: best practices

#### **General advice:**

- Be explicit about hypotheses and measures of interest (mean, median, location shift, proportions, etc.).
- Select appropriate statistical tests for a given hypothesis.
- Use data visualization to complement statistical tests.
- Be explicit about the effect size of interest.
- Contextualize effect size (requires domain knowledge).

# Working with distributions in R

# Let's take a big step back!

# And answer questions like the following (over 2 lectures)

- What are PDF (probability density function) and CDF (cumulative distribution function)?
- Do I need to encode PDF and CDF (for common distributions) in R?
- What is the difference between population, sample, and sampling distribution?
- What is the CLT (Central Limit Theorem)?
- How is the CLT related to NHST?
- How is the CLT related to p values, confidence, and power?
- What are the downsides of NHST (frequentist vs. bayesian statistics)?

## The normal distribution

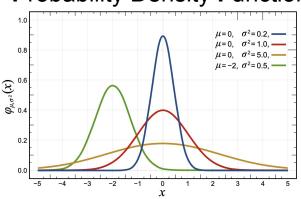
#### **Characterized by**

PDF: Probability Density Function

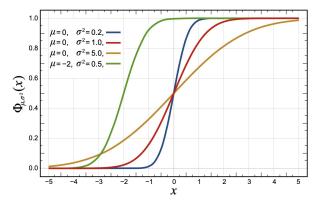
CDF: Cumulative Distribution Function

$$f(x)=rac{1}{\sqrt{2\pi\sigma^2}}e^{-rac{(x-\mu)^2}{2\sigma^2}}$$

#### **Probability Density Function**



#### **C**umulative **D**istribution Function



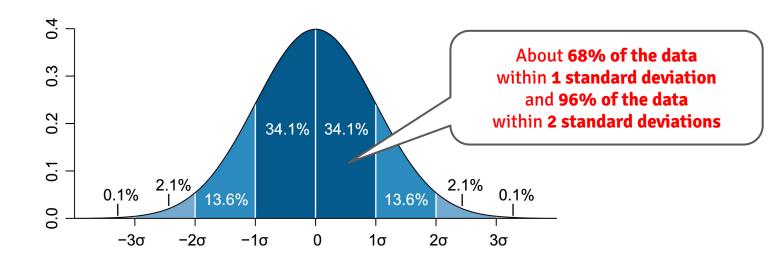
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# The normal distribution in R

#### **Key functions**

dnorm: PDF

pnorm: CDF

qnorm: quantile function

• quomi. quantile function

rnorm: randomly sample (n, mean, sd)

x) morm(50) pnorm(2) = 0.977

| Column | Column

Learn once and work with many common distributions (e.g., rnorm, rt, runif, rbinom)

# **Simulations and CLT: live demo**

# Statistical modeling: in-class exercise